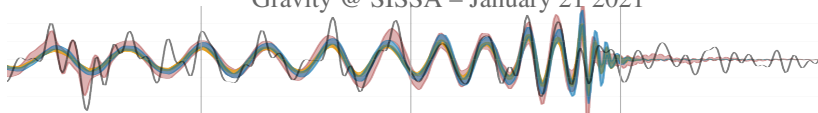


The Binary Universe In Gravitational Waves

Frank Ohme

Max Planck Institute for Gravitational Physics
(Albert Einstein Institute)
Hannover, Germany

Gravity @ SISSA – January 21, 2021

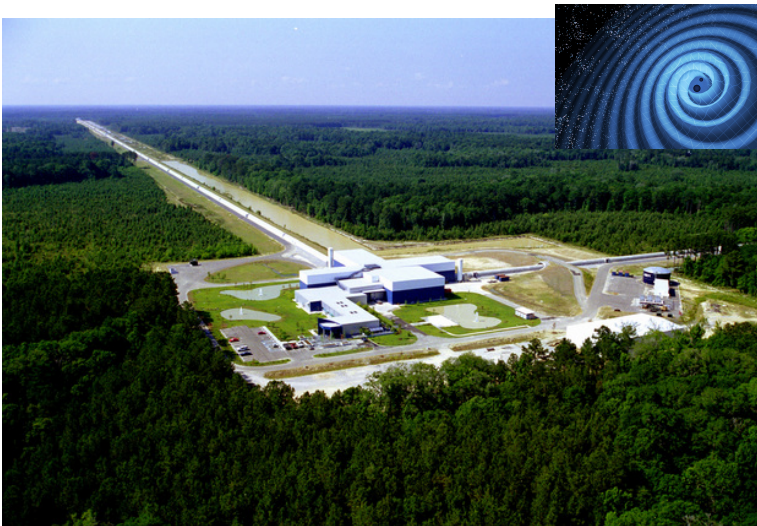


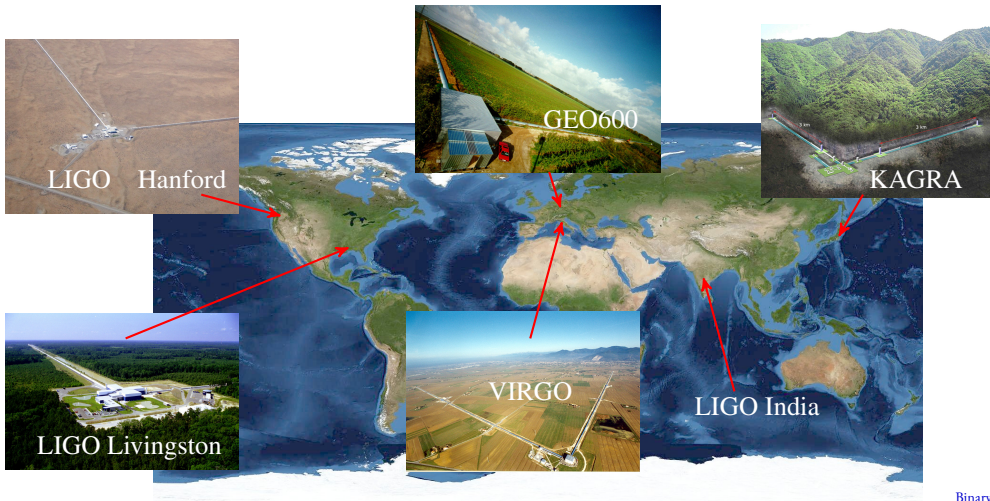
LIGO-G2002166v1



LIGO Scientific Collaboration







[GWTC-2, 2010.14527]

O1 09/2015 – 01/2016

3 binary black holes (BBHs)

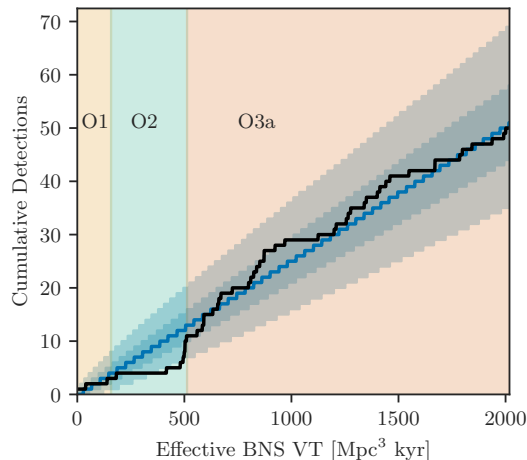
O2 10/2016 – 08/2017

7 BBHs + 1 binary neutron star (BNS)

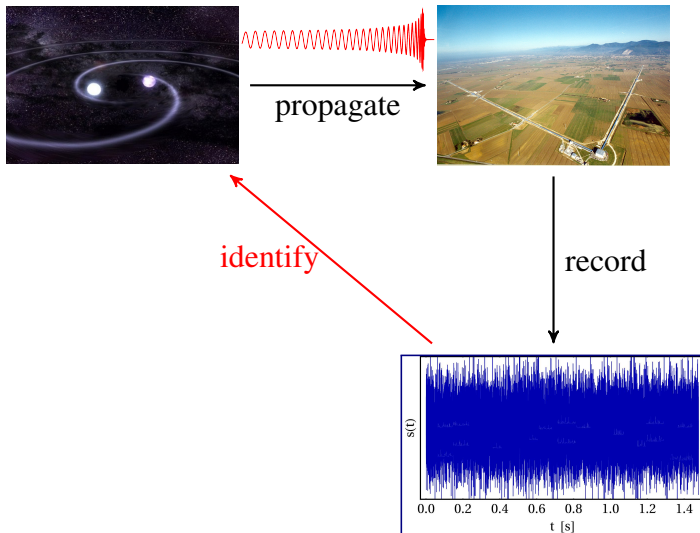
O3 04/2019 – 03/2020 (suspended)

O3a 37 BBHs + 1 BNS + 1 NSBH
(candidates)

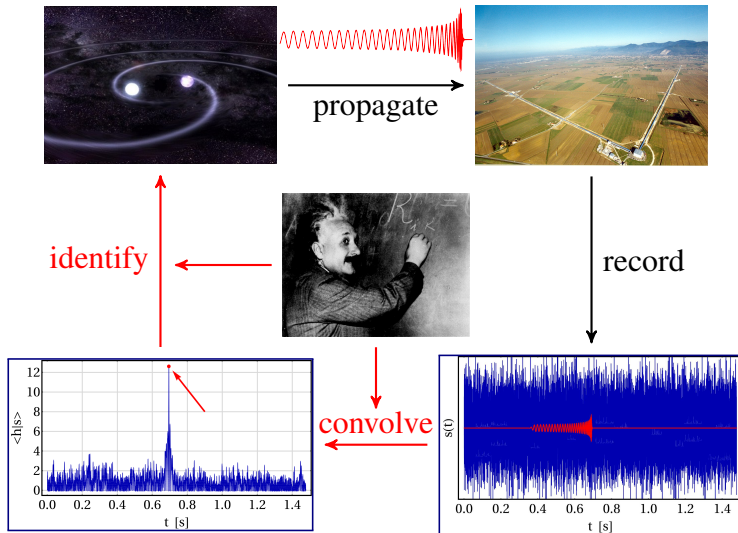
O3b □ BBHs + □ BNSs + “#..;’?@

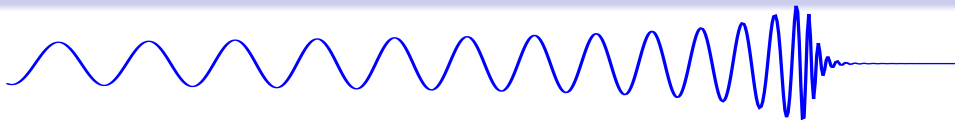
see also [Zackay+ 1902.10331, 1910.09528; Venumadhav+
1904.07214; Nitz+ 1910.05331, 1811.01921]

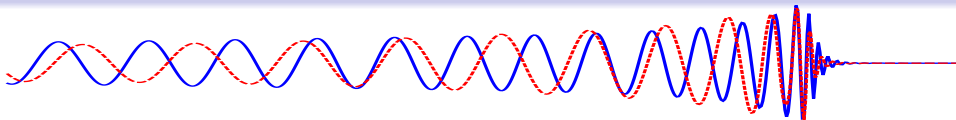
The Analysis Challenge



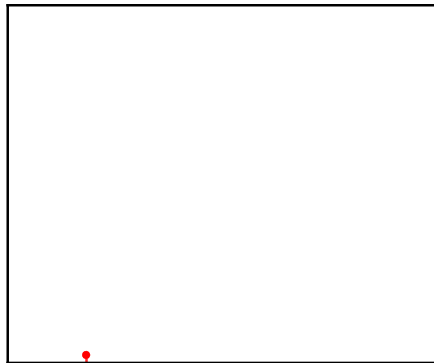
The Analysis Challenge





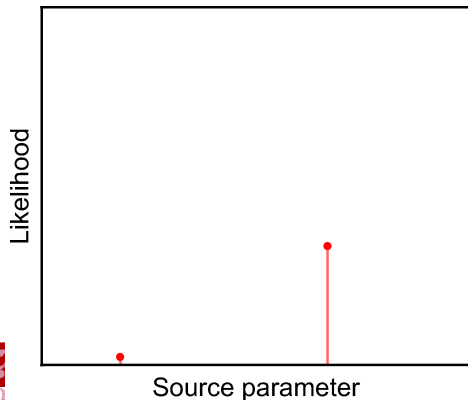
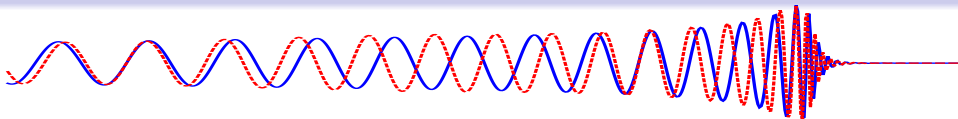


Likelihood

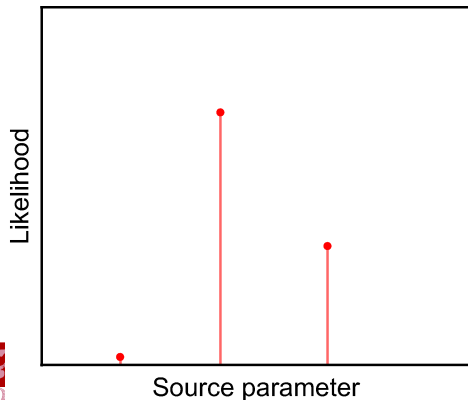
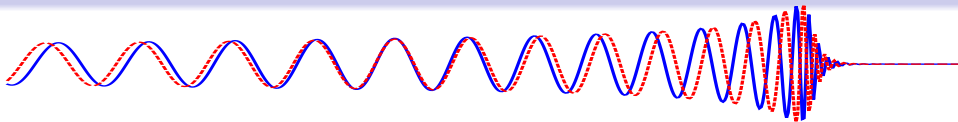


Source parameter

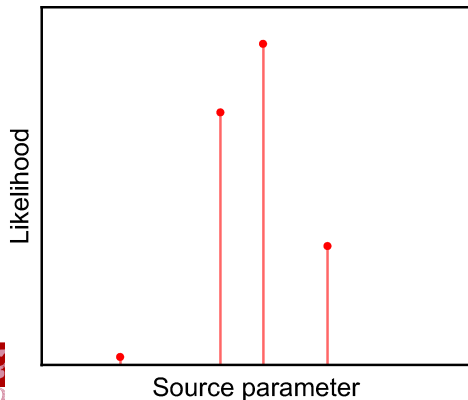
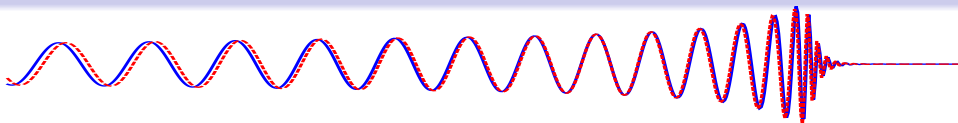
- $\langle h|s \rangle = 4 \operatorname{Re} \int \frac{\tilde{h}(f) \tilde{s}^*(f)}{S_n(f)} df$
- $\boldsymbol{\vartheta}$: Source parameters
- $\Lambda(s|\boldsymbol{\vartheta}) \sim \exp(-\frac{1}{2} \|s - h(\boldsymbol{\vartheta})\|^2)$
- **Posterior probability** $(\boldsymbol{\vartheta}|s)$
 $\sim \Lambda(s|\boldsymbol{\vartheta}) \times \text{prior}(\boldsymbol{\vartheta})$



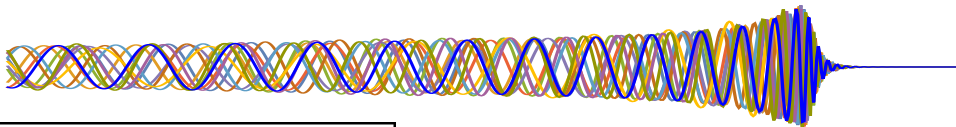
- $\langle h|s \rangle = 4 \operatorname{Re} \int \frac{\tilde{h}(f) \tilde{s}^*(f)}{S_n(f)} df$
- ϑ : Source parameters
- $\Lambda(s|\vartheta) \sim \exp(-\frac{1}{2} \|s - h(\vartheta)\|^2)$
- **Posterior probability** $(\vartheta|s)$
 $\sim \Lambda(s|\vartheta) \times \text{prior}(\vartheta)$



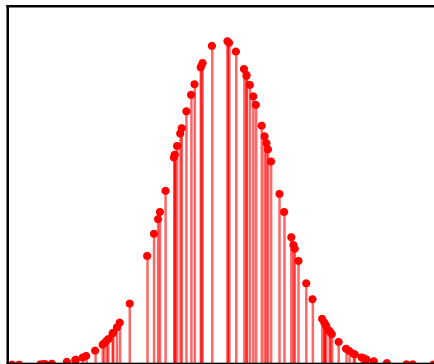
- $\langle h|s \rangle = 4 \operatorname{Re} \int \frac{\tilde{h}(f) \tilde{s}^*(f)}{S_n(f)} df$
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- **Posterior probability** $(\boldsymbol{\vartheta}|s)$
 $\sim \Lambda(s|\boldsymbol{\vartheta}) \times \text{prior}(\boldsymbol{\vartheta})$



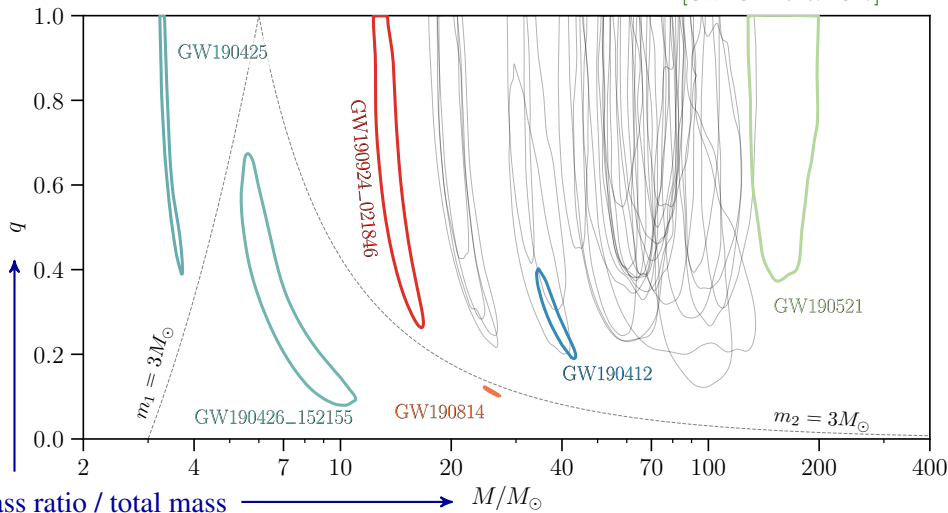
Likelihood



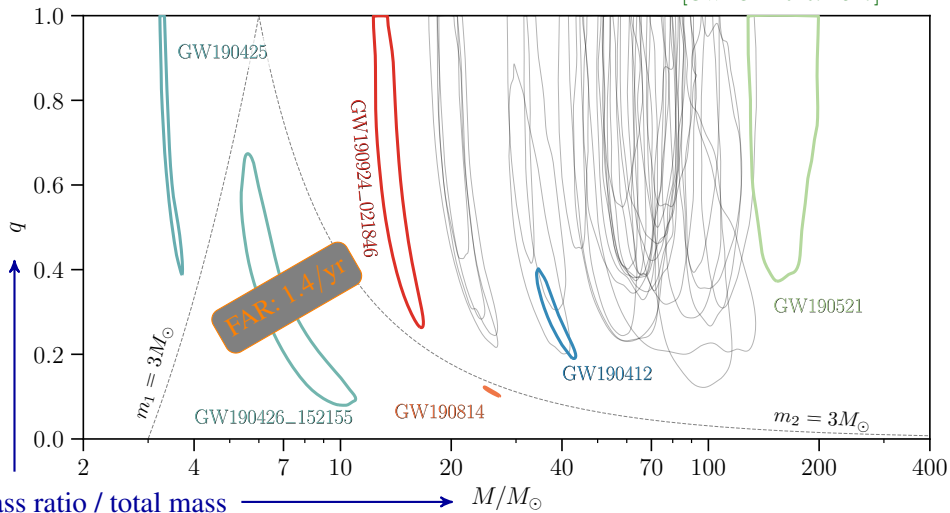
Source parameter

- $\langle h|s \rangle = 4 \operatorname{Re} \int \frac{\tilde{h}(f) \tilde{s}^*(f)}{S_n(f)} df$
- ϑ : Source parameters
- $\Lambda(s|\vartheta) \sim \exp(-\frac{1}{2} \|s - h(\vartheta)\|^2)$
- **Posterior probability** $(\vartheta|s)$
 $\sim \Lambda(s|\vartheta) \times \text{prior}(\vartheta)$

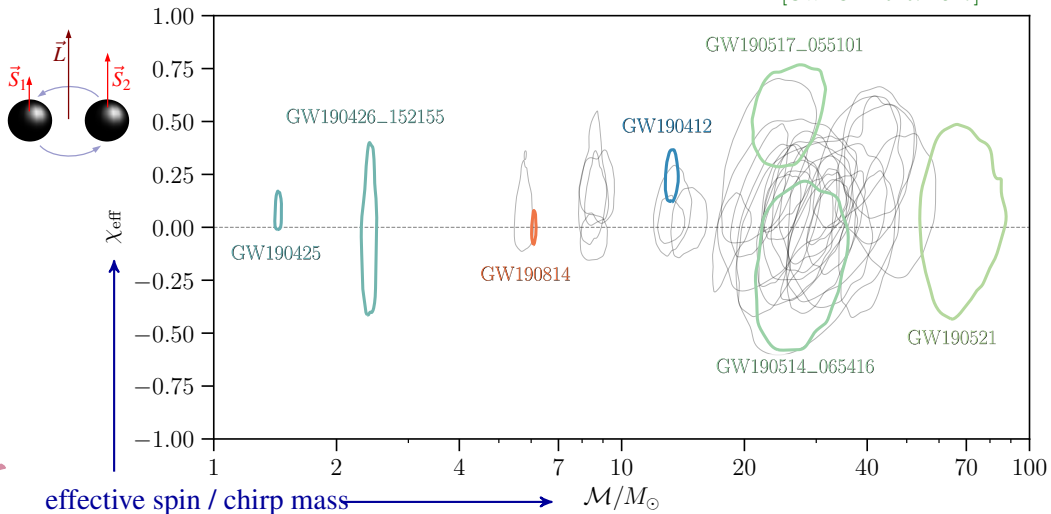
[GWTC-2 2010.14527]



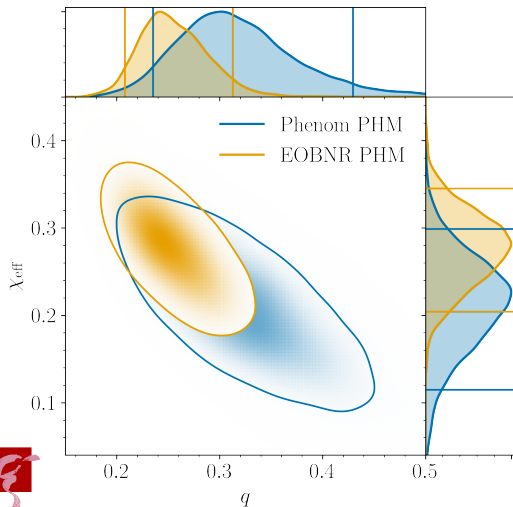
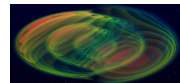
[GWTC-2 2010.14527]



[GWTC-2 2010.14527]



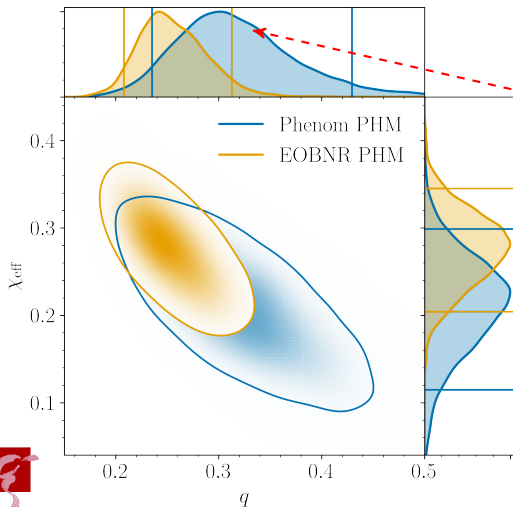
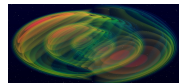
GW190412



[LVC 2004.08342]

GW190412

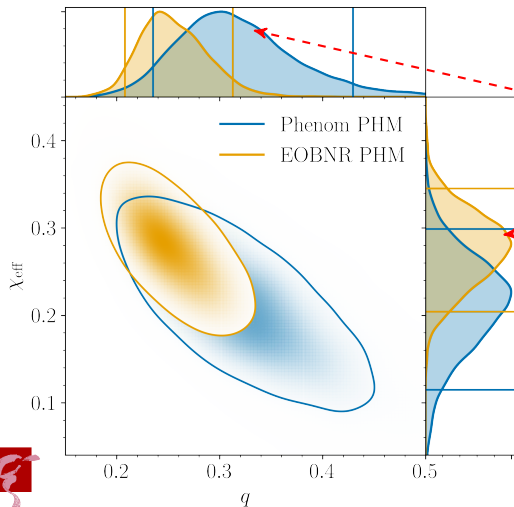
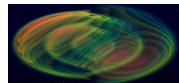
GW190412

mass ratio $q \sim 0.3$

[LVC 2004.08342]

GW190412

GW190412



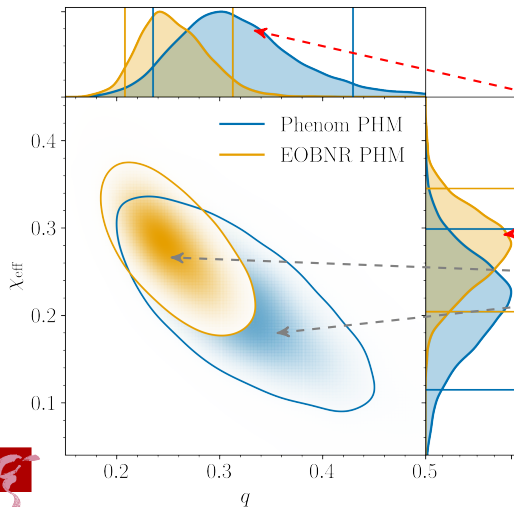
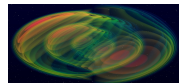
mass ratio $q \sim 0.3$

significant spin

[LVC 2004.08342]

GW190412

GW190412



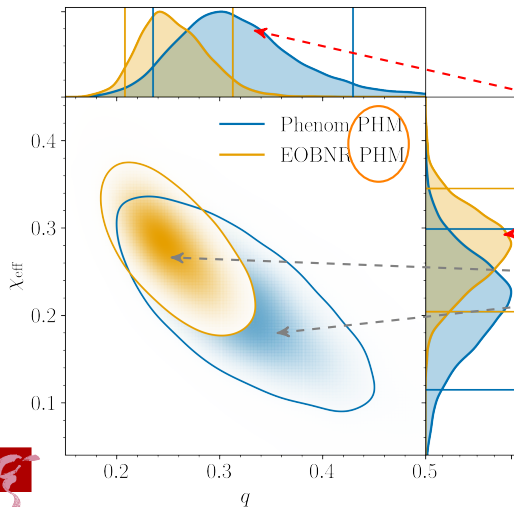
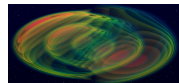
mass ratio $q \sim 0.3$

significant spin

non-negligible systematics

[LVC 2004.08342]

GW190412



mass ratio $q \sim 0.3$

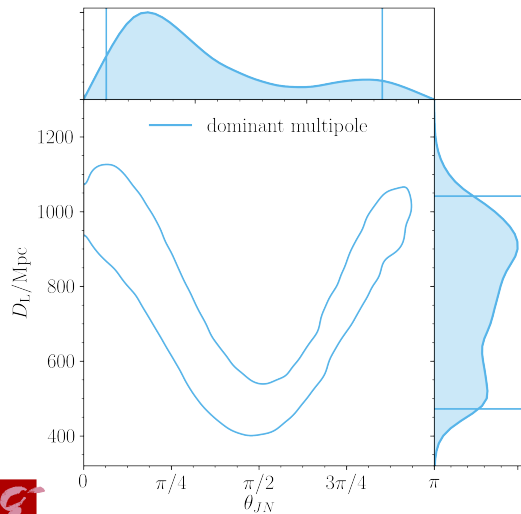
significant spin

non-negligible systematics

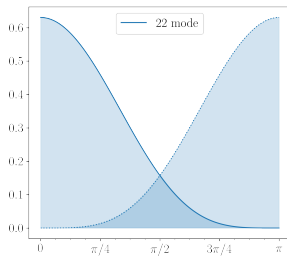
models including precession
and higher multipoles

[LVC 2004.08342]

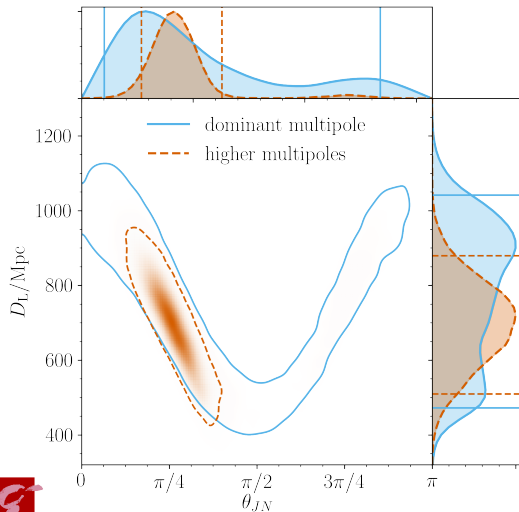
Distance and Inclination



- Inclined systems are intrinsically quieter
- degenerate with distance

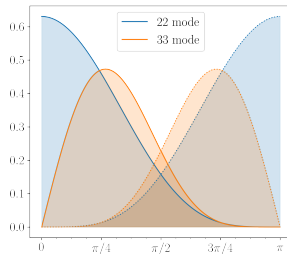


Distance and Inclination

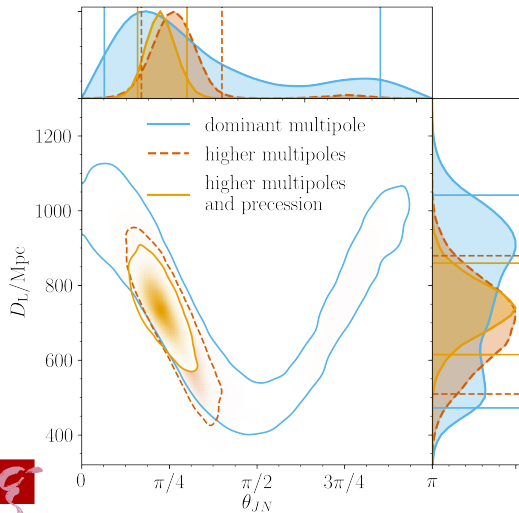


- Inclined systems are intrinsically quieter
- degenerate with distance

- $h_+ - ih_\times = \sum_{\ell,m} h_{\ell m}(t, \vartheta) {}_{-2}Y_{\ell m}(\theta, \phi)$

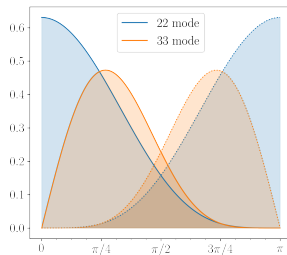


Distance and Inclination



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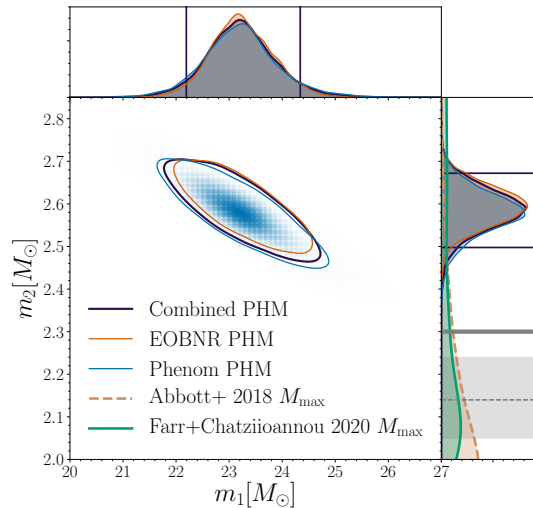
$$\bullet h_+ - ih_\times = \sum_{\ell,m} h_{\ell m}(t, \vartheta) {}_{-2}Y_{\ell m}(\theta, \phi)$$



- ✓ Strong evidence for higher multipoles
- ? Strong precession disfavoured

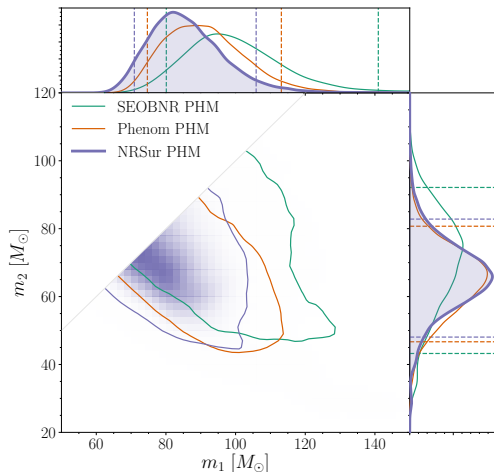
GW190814 [LVC 2006.12611]

- Loud, unambiguous detection with $\text{SNR} \approx 25$
- Most asymmetric masses observed so far, $q = 0.112^{+0.008}_{-0.009}$
- Object 1 clearly a black hole, but nature of object 2 unclear ($m_2 = 2.59^{+0.08}_{-0.09} M_\odot$)
- Strongest evidence of higher multipoles ($\rho_{33} \gtrsim 6$, Bayes factor $\sim 10^9$)
- Strong spin constraint $\chi_1 < 0.07$
- Challenging for standard formation channels



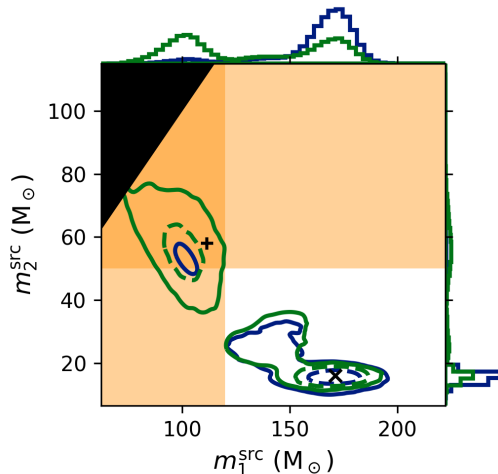
- Short (0.1 s), low frequency signal of $\text{SNR} \approx 15$, highest significance [$\text{FAR} = 1/4900 \text{ yr}$] from generic transient search
- BBH: Masses in **pair instability mass gap**
- Hints of precession
- Candidate counterpart [Graham+ 2006.14122], association inconclusive [Ashton+ 2009.12346]
- Many suggested formation mechanisms: hierarchical mergers in dense environment (globular clusters, AGN disks), stellar merger, more exotic scenarios, high-mass ratio merger

GW190521 [LVC 2009.01075, 2009.01190]



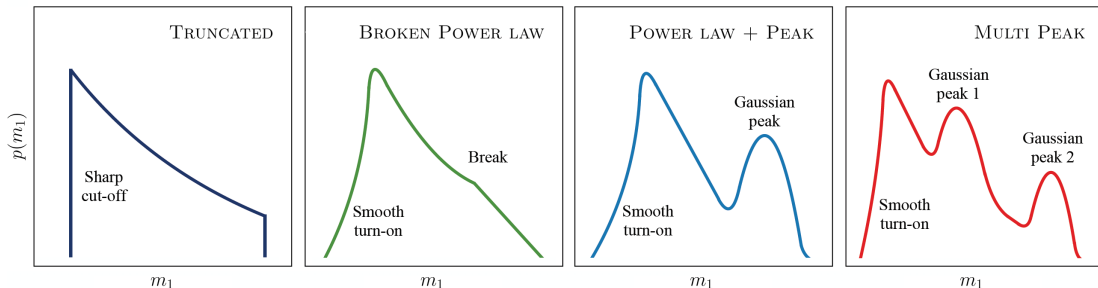
GW190521 [Nitz+ 2010.12558]

- Short (0.1 s), low frequency signal of $\text{SNR} \approx 15$, highest significance [FAR= 1/4900 yr]] from generic transient search
- BBH: Masses in **pair instability mass gap**
- Hints of precession
- Candidate counterpart [Graham+ 2006.14122], association inconclusive [Ashton+ 2009.12346]
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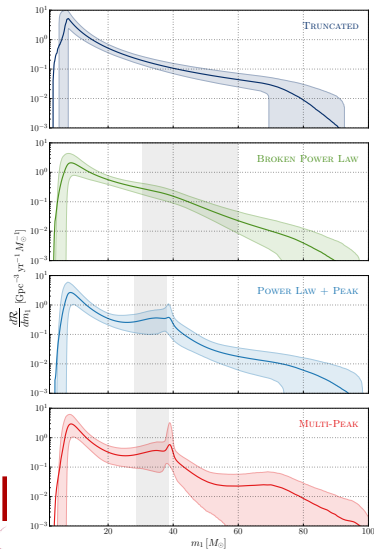


Black hole population [LVC 2010.14533]

- 1 Assume parametric model for population of black hole masses, mass ratio and spins
- 2 For each model, calculate likelihood of observing GWTC-2
- 3 Bayes' theorem: obtain posterior probabilities for population hyperparameters



Mass distribution

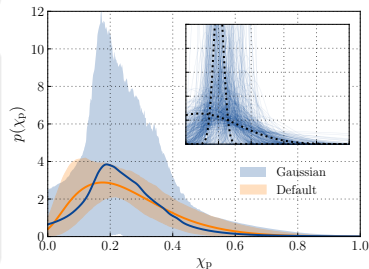
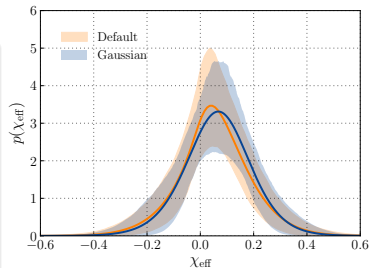


Masses

- Truncated power law insufficient
- Boundaries dominated by GW190814, GW190521
- Extra feature around $m_1 \lesssim 40M_\odot$

Spins

- Some (small) fraction of spins misaligned
- Completely aligned spin population disfavoured
- $\approx 30\%$ with $\chi_{\text{eff}} < 0$

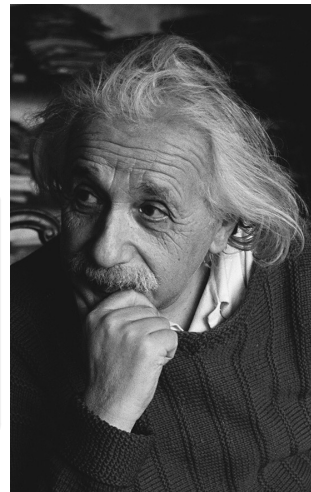


GR is the correct theory, or is it not?

Conclusively proving GR as the correct theory is impossible, only ruling it (GR or alternatives) out.

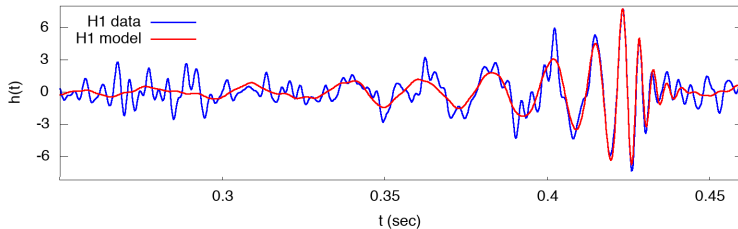
Test categories

- 1 Is what we observe consistent with GR?
Is there something we cannot explain?
- 2 Can we measure generic deviations from GR?
- 3 Can we observe features of specific alternatives to GR?



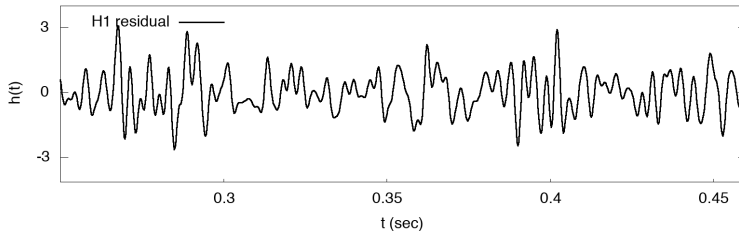
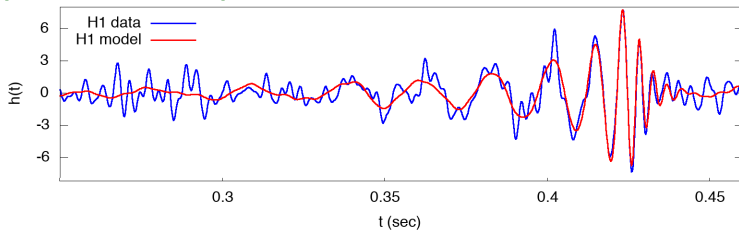
Anything unusual in the data?

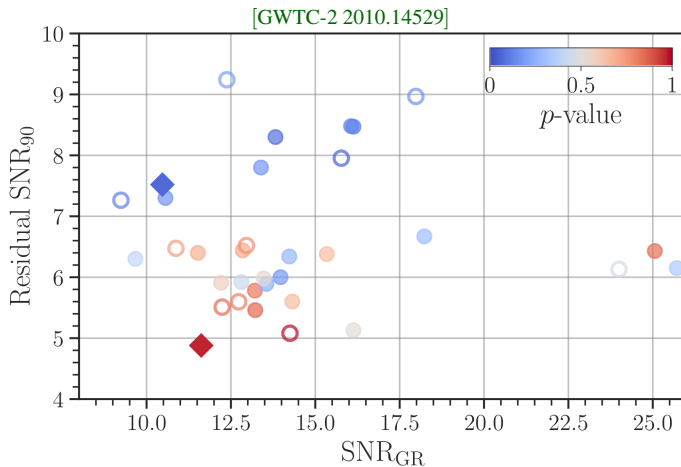
[LIGO-Virgo 1908.11170]

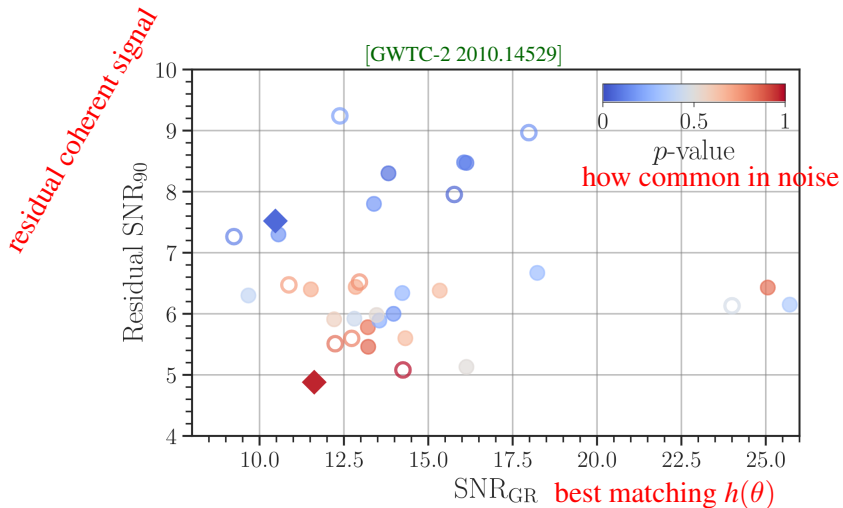


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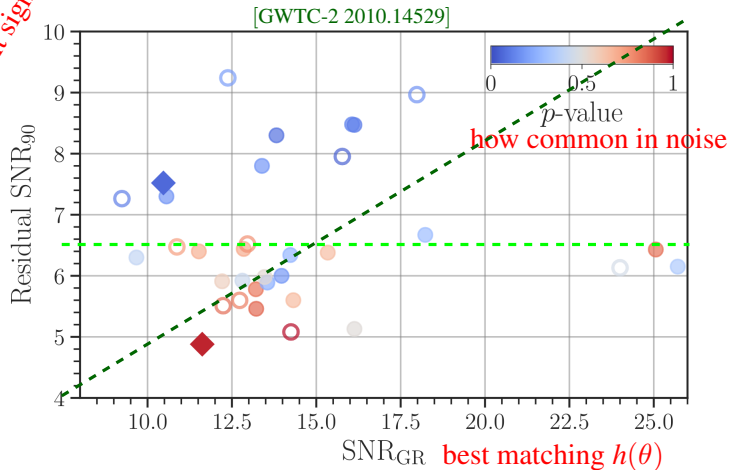
[LIGO-Virgo 1908.11170]



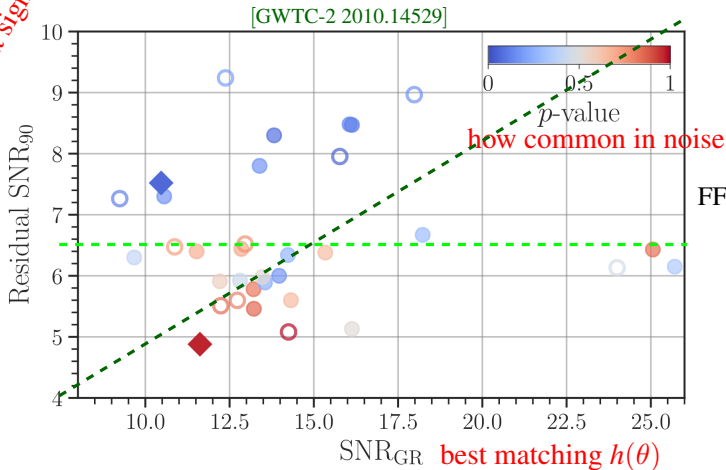




residual coherent signal



residual coherent signal



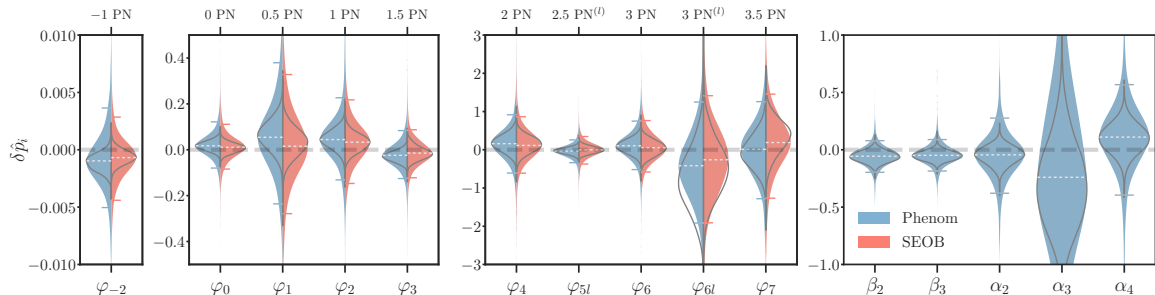
$$\text{FF} = \frac{\text{SNR}_{\text{GR}}}{\sqrt{\text{SNR}_{\text{GR}}^2 + \text{SNR}_{90}^2}}$$

$$\approx 0.8 \dots 0.9 \text{ (LIGO)}$$

$$\approx 0.9999 \text{ (ET)}$$

Post-Newtonian Phase

$$\phi(v) = \sum_{k=0} \varphi_k(\eta, \vec{s}_1, \vec{s}_2) \cdot \left(\frac{v}{c}\right)^{k-5}$$



[GWTC-2 2010.14529]

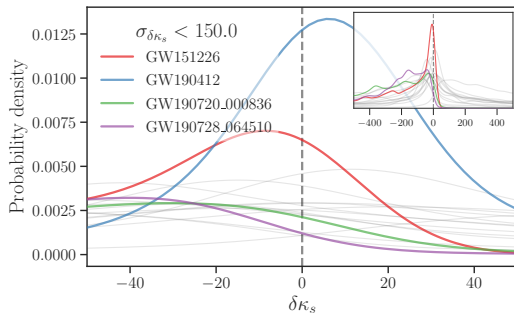
- BH mimickers react differently to their own spin and the companion's tidal field
⇒ **spin-induced quadrupole moment** coefficient entering at 2PN order can test BH nature
[Krishnendu+ 1701.06318, 1811.00317]



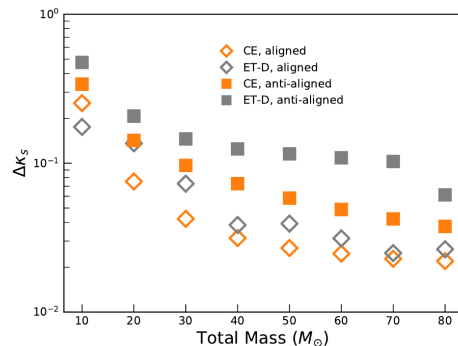
- BH mimickers react differently to their own spin and the companion's tidal field
 $\Rightarrow$ **spin-induced quadrupole moment** coefficient entering at 2PN order can test BH nature

[Krishnendu+ 1701.06318, 1811.00317]

[GWTC-2 2010.14529]



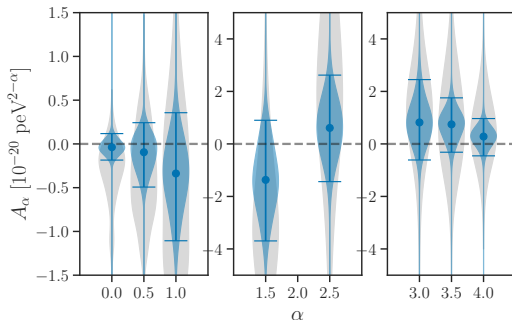
Measurement accuracy



- Modified theories may violate Lorentz invariance, leading to a modified dispersion relation

$$E^2 = p^2 c^2 + A_\alpha p^\alpha c^\alpha$$

- Modified dispersion leads to different gravitational-wave phasing [Mirshekari+ 1110.2720]



$$m_g c^2 = \sqrt{A_0} < 1.8 \times 10^{-23} \text{ eV}$$

[GWTC-2 2010.14529]

- Every Observing Run delivered new science
- Digging deeper into neutron star and black hole populations
- Binaries show (surprising?) diversity – multiple formation channels?
- Important interactions with EM observers, stellar modeling, fundamental physics communities etc.
- Groups outside the LIGO-Virgo collaborations analyze data and report new events
- Open public alerts, strain data and posterior samples released
- Stay tuned for more news from O3 and the gravitational-wave universe

