

# *The dawn of low frequency gravitational wave astronomy*

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(Universita' di Milano Bicocca)



# ***OUTLINE***

- > Pulsars as ultra-precise clocks for GW detection**
- > (super)massive black hole binaries (MBHBs)**
- > Evidence for a GW signal in PTA experiments**
- > Implications**



# COSMIC OBSERVERS

IN DEVELOPMENT

ACTIVE

LEGACY

microwaves

sub-millimetre

infrared

optical

ultraviolet

x-rays

gamma rays



ariel  
[2029]

roman  
[2026]



plato  
[2026]



einstein  
probe  
[2023]



athena  
[~2036]



webb  
[2021-]



euclid  
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hubble  
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gaia  
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cheops  
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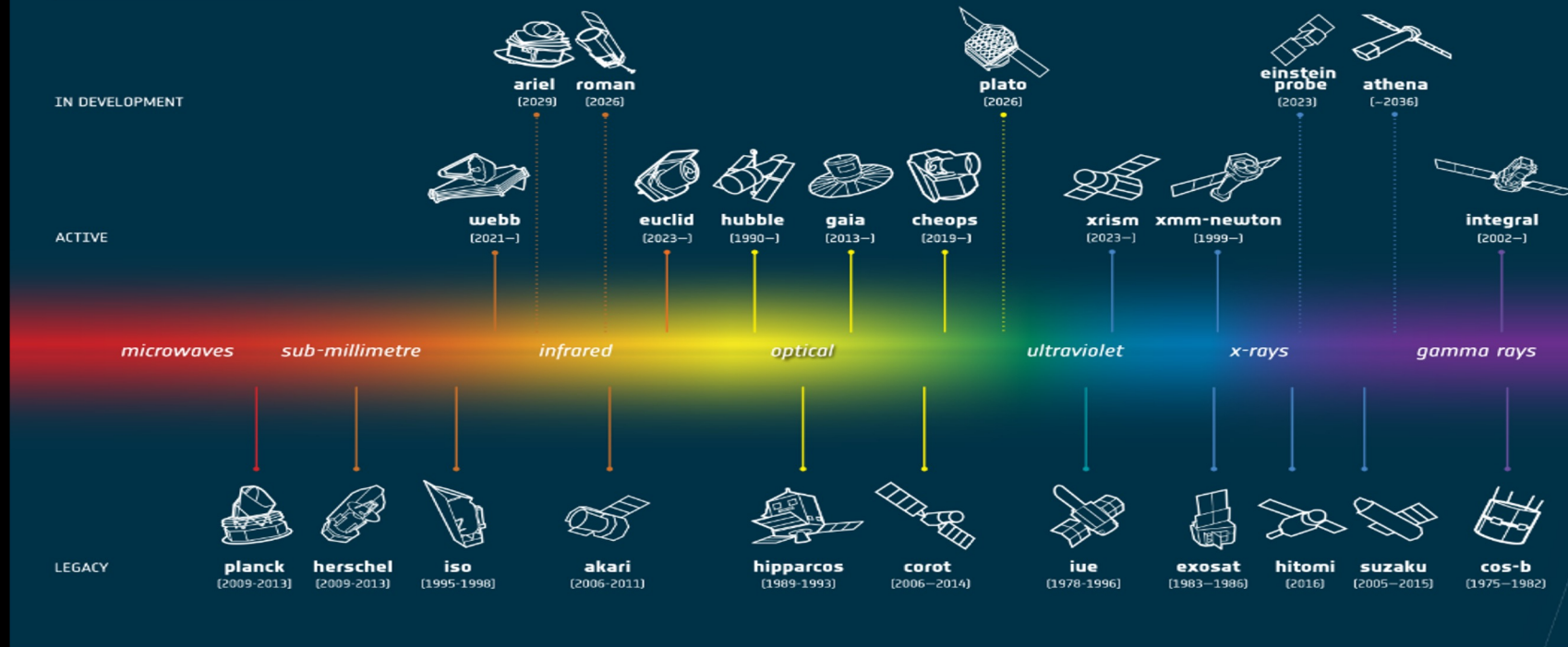


suzaku  
[2005-2015]



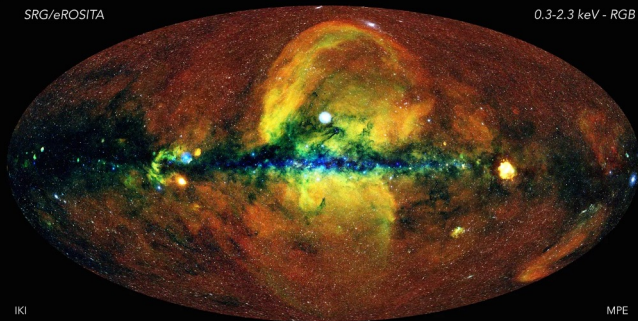
cos-b  
[1975-1982]

## COSMIC OBSERVERS



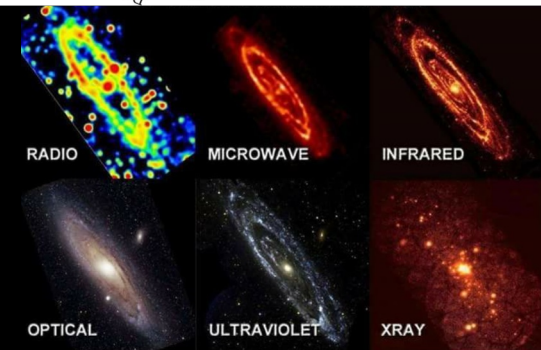
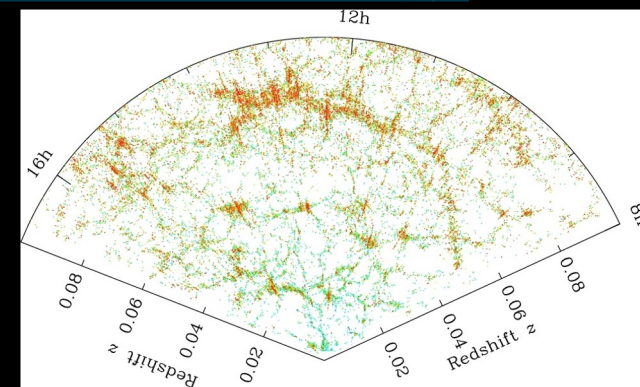
SRG/eROSITA

0.3–2.3 keV - RGB



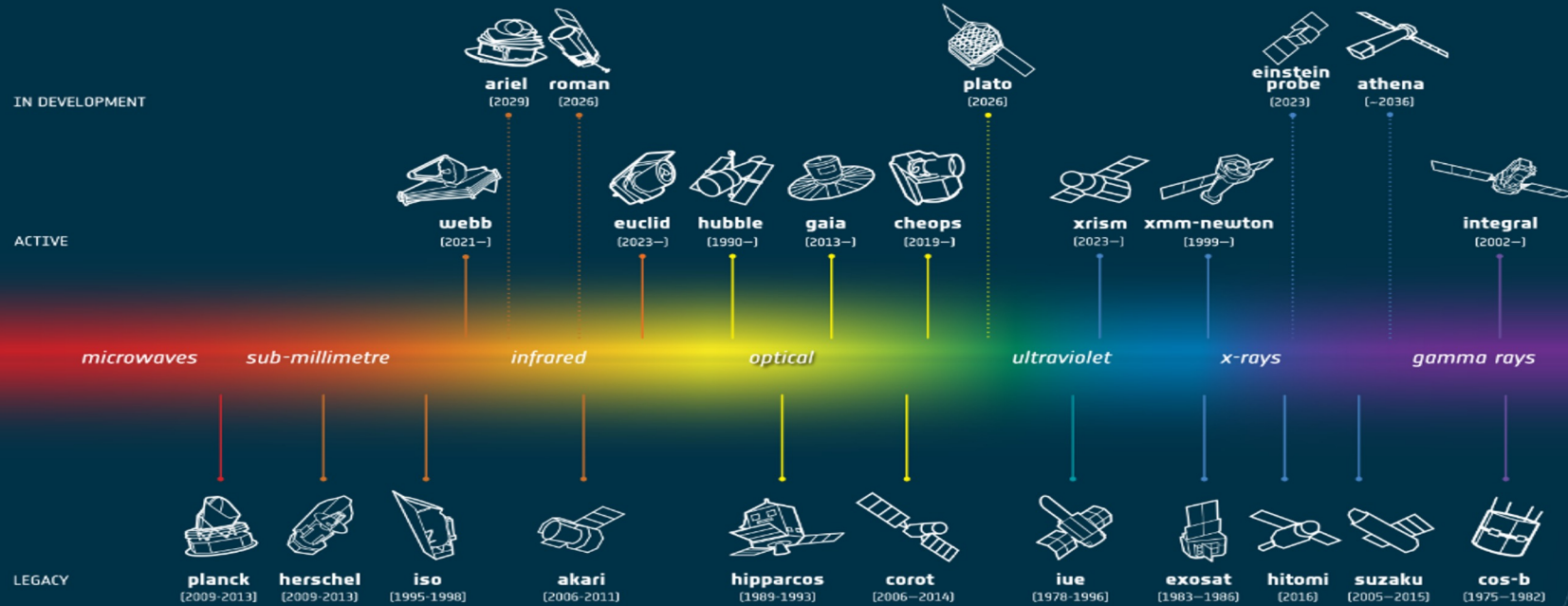
IKI

MPE





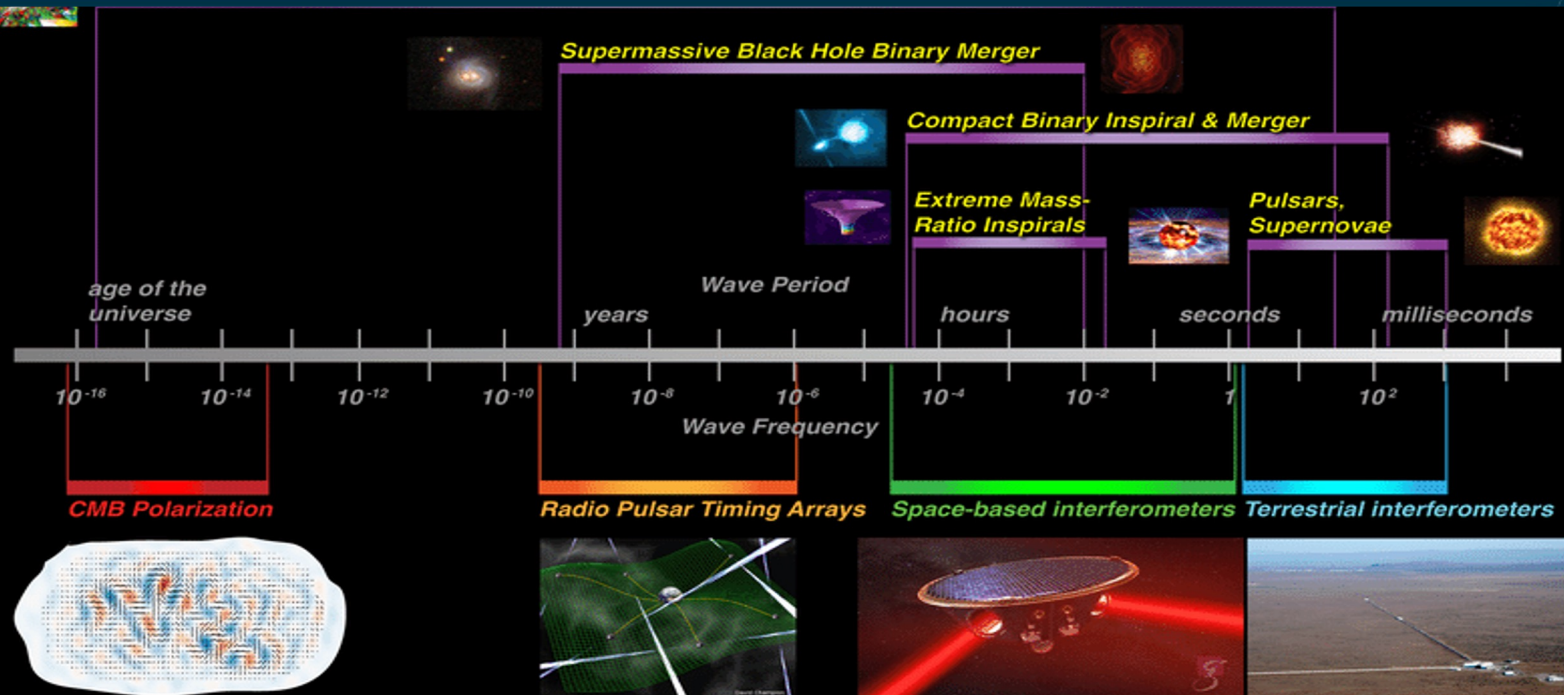
## COSMIC OBSERVERS



## The Gravitational Wave Spectrum

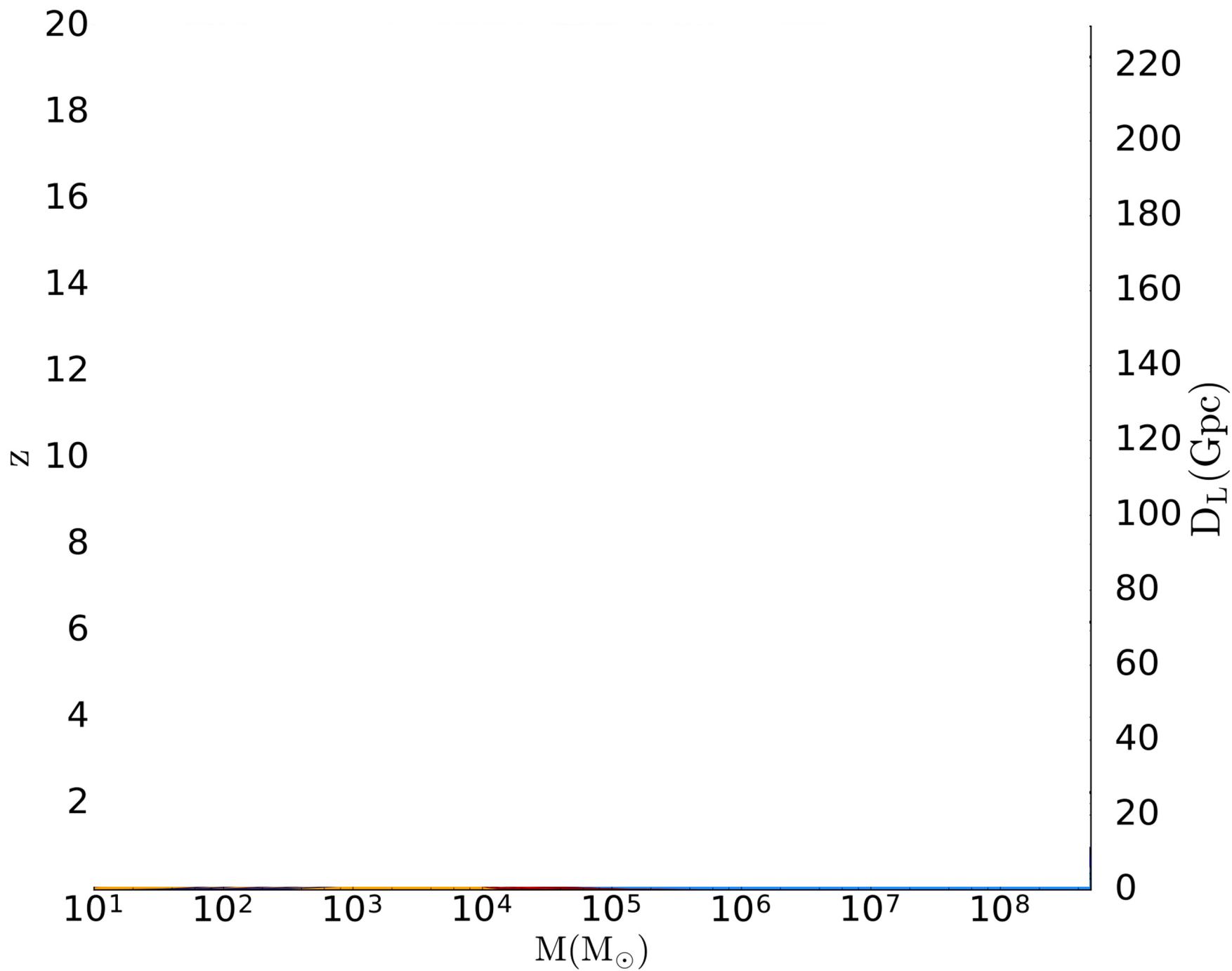
Sources

Detectors

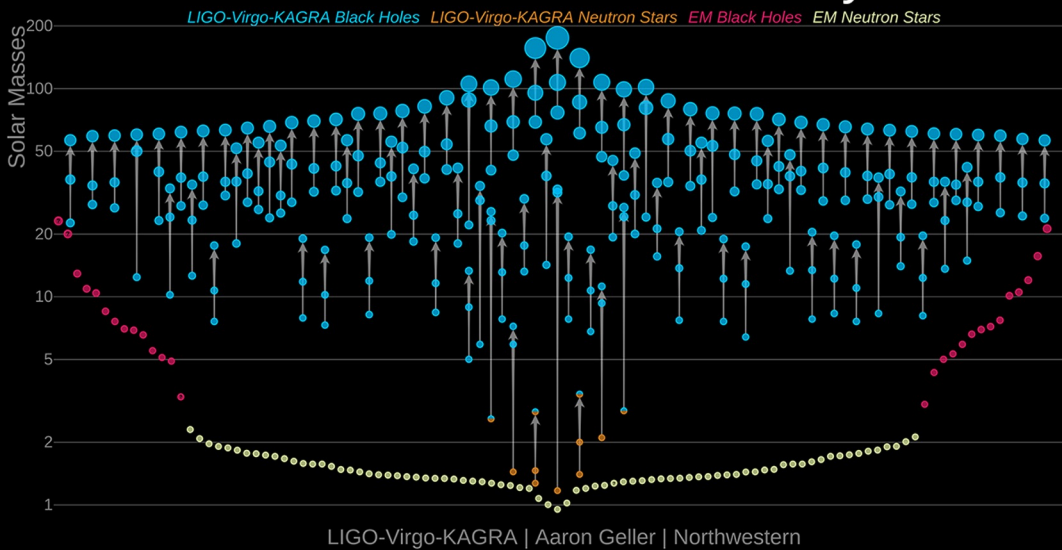




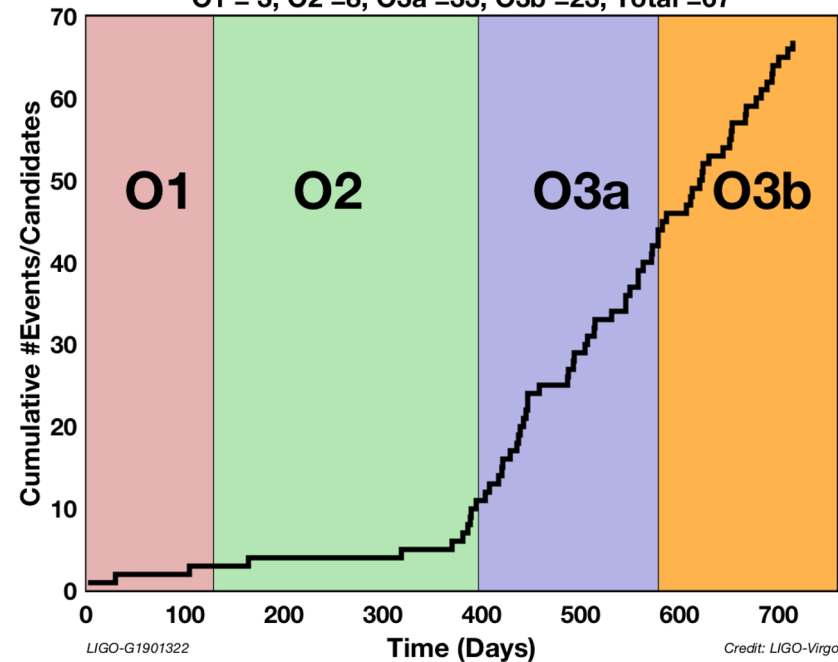
***Before 2015....***



# Masses in the Stellar Graveyard

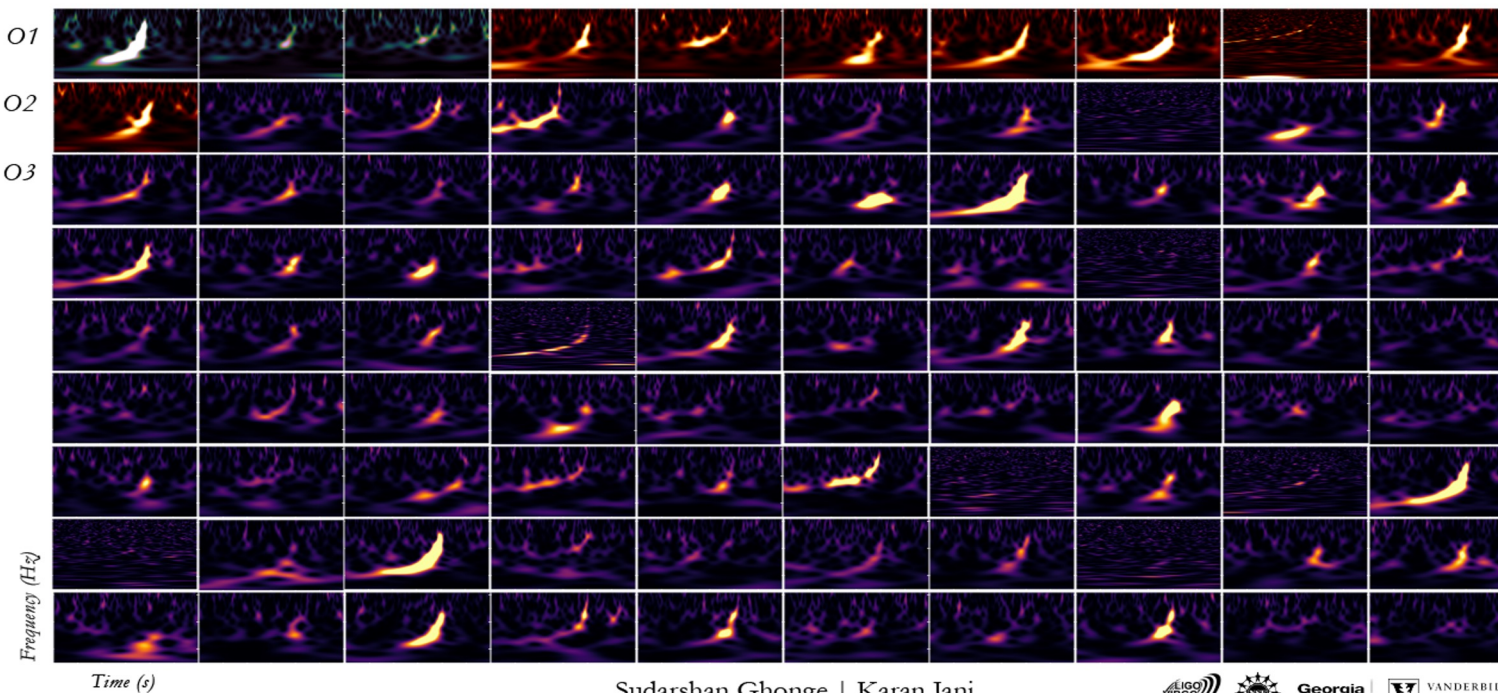


Cumulative Count of Events and (non-retracted) Alerts  
O1 = 3, O2 = 8, O3a = 33, O3b = 23, Total = 67

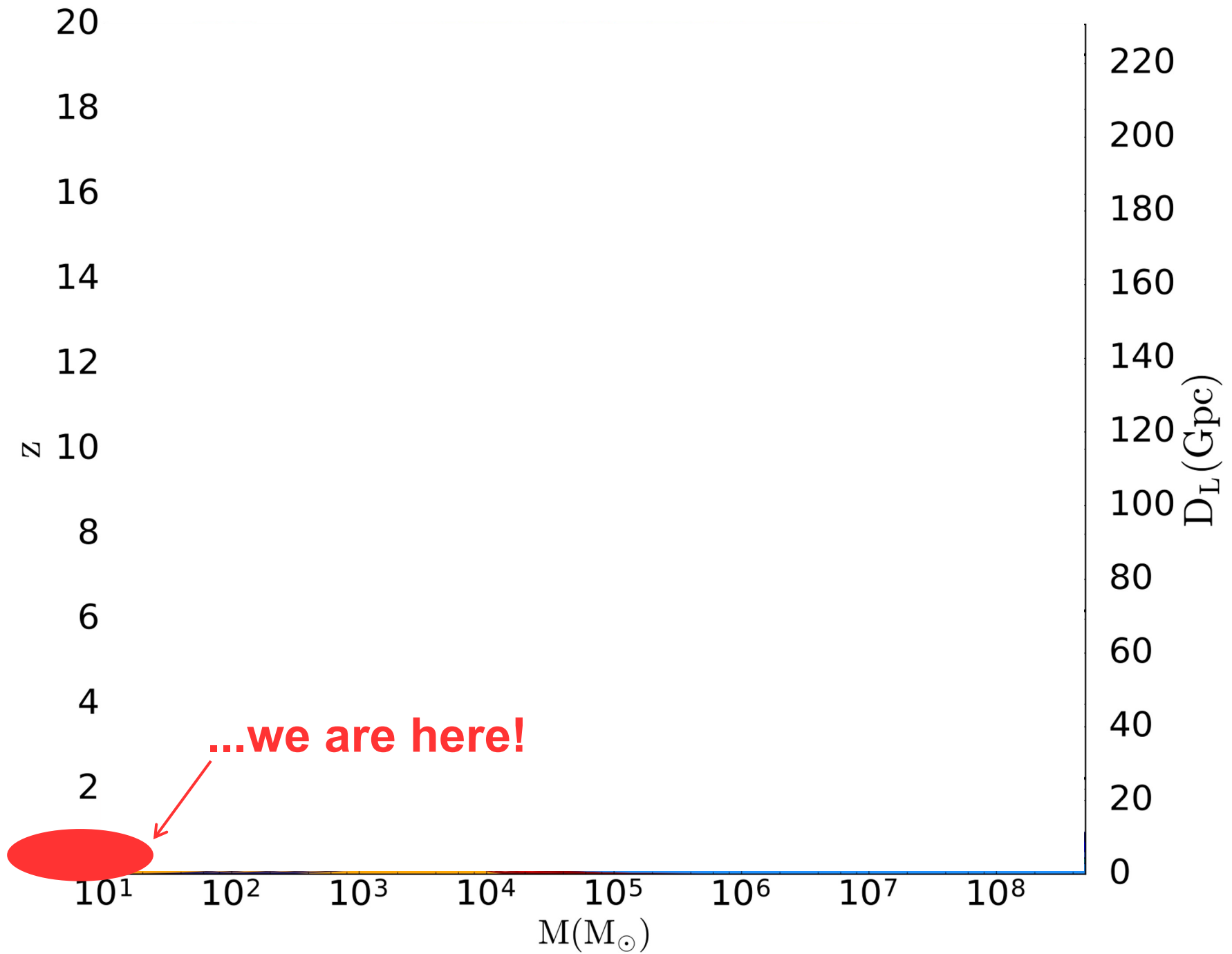


## Gravitational-Wave Transient Catalog

Detections from 2015-2020 of compact binaries with black holes & neutron stars



# After GWTC-3.....





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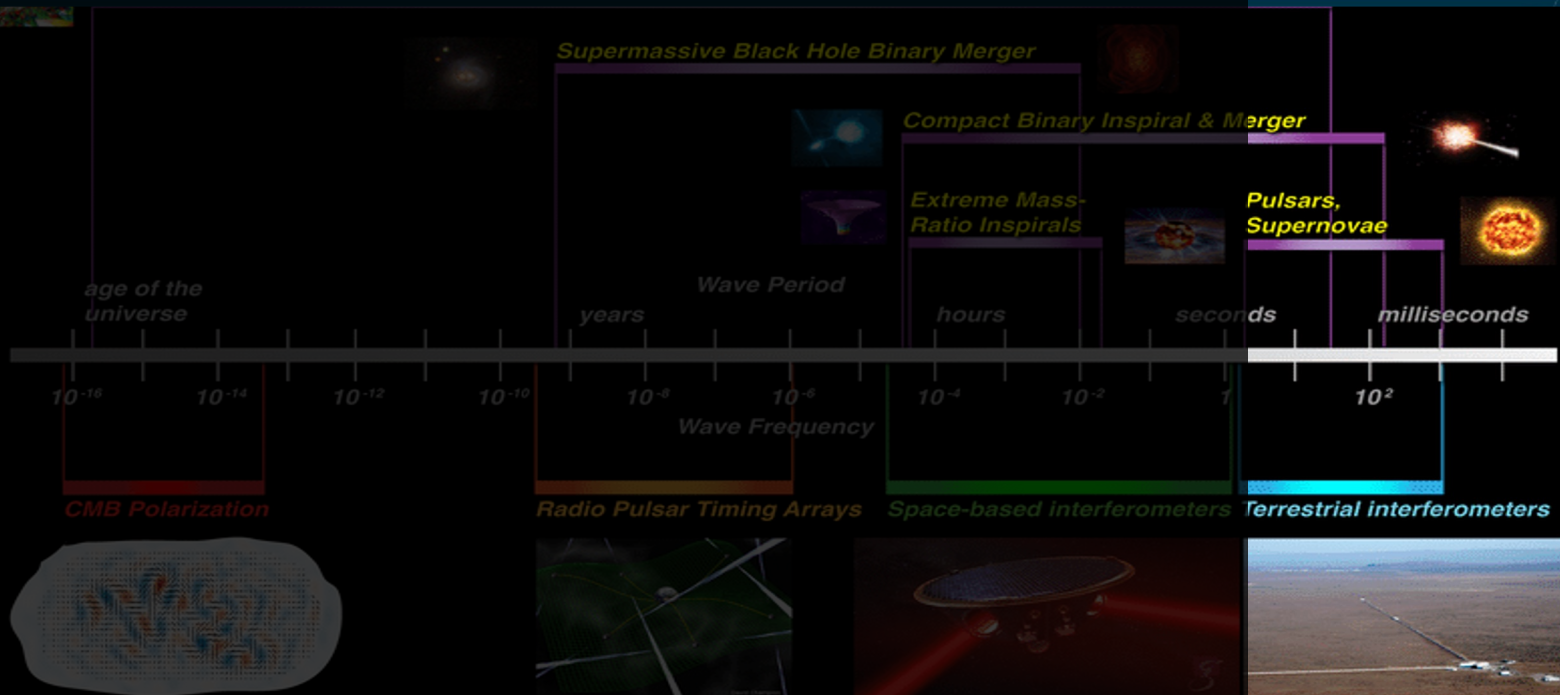
xmm-newton  
[1999-]

integral  
[2002-]

The Gravitational Wave Spectrum

Sources

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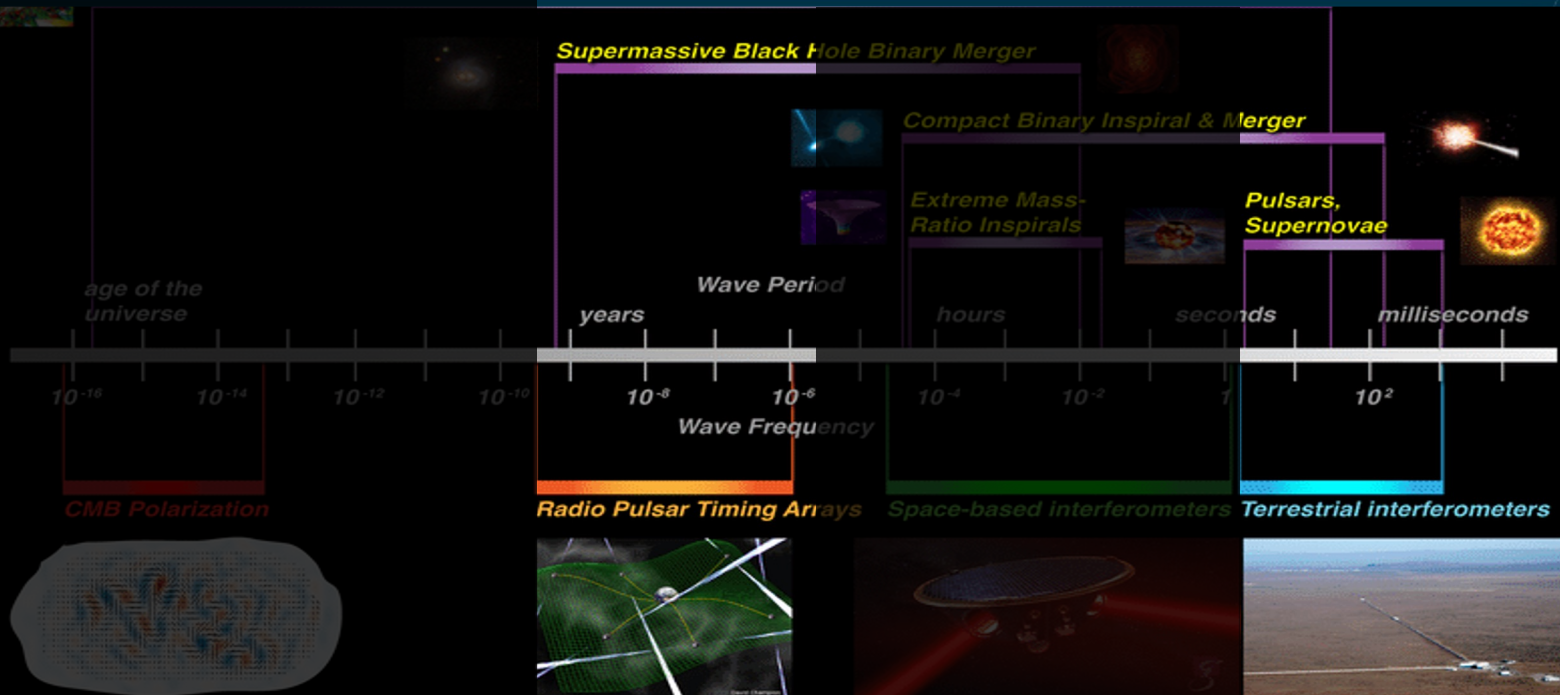
roman  
[2026]

plato  
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The Gravitational Wave Spectrum

Sources

Detectors



# *What is pulsar timing*

Pulsars are neutron stars seen through their regular radio pulses

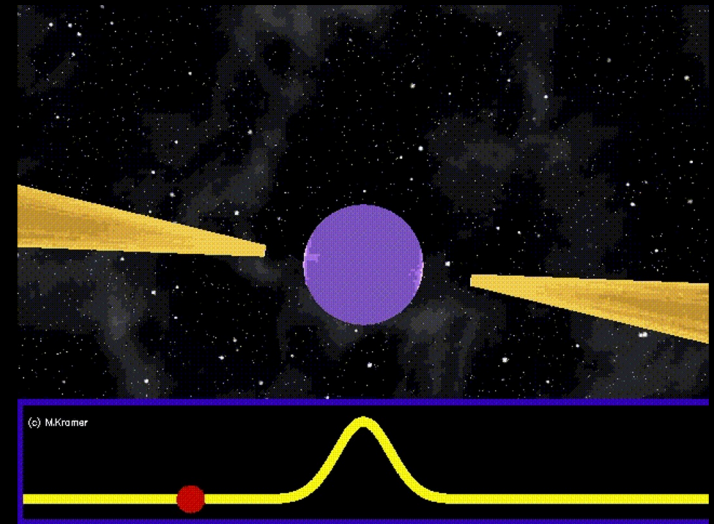
Pulsar timing is the art of measuring the time of arrival (ToA) of each pulse

1-Observable a pulsar and measure the ToAs

2-Find the model which best fits the ToAs

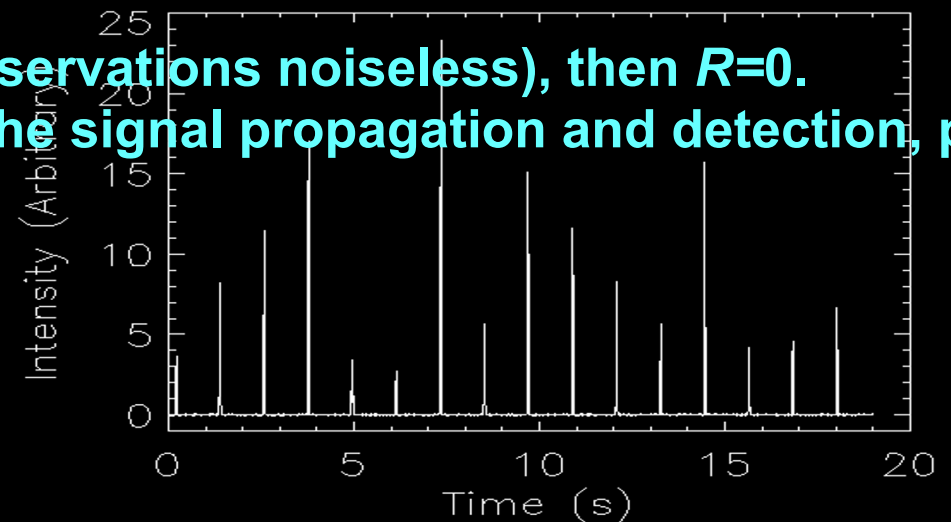
3-Compute the timing residual  $R$

$$R = \text{ToA} - \text{ToA}_m$$



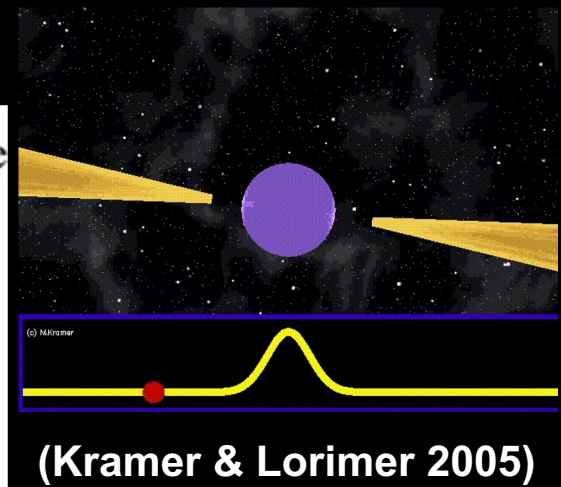
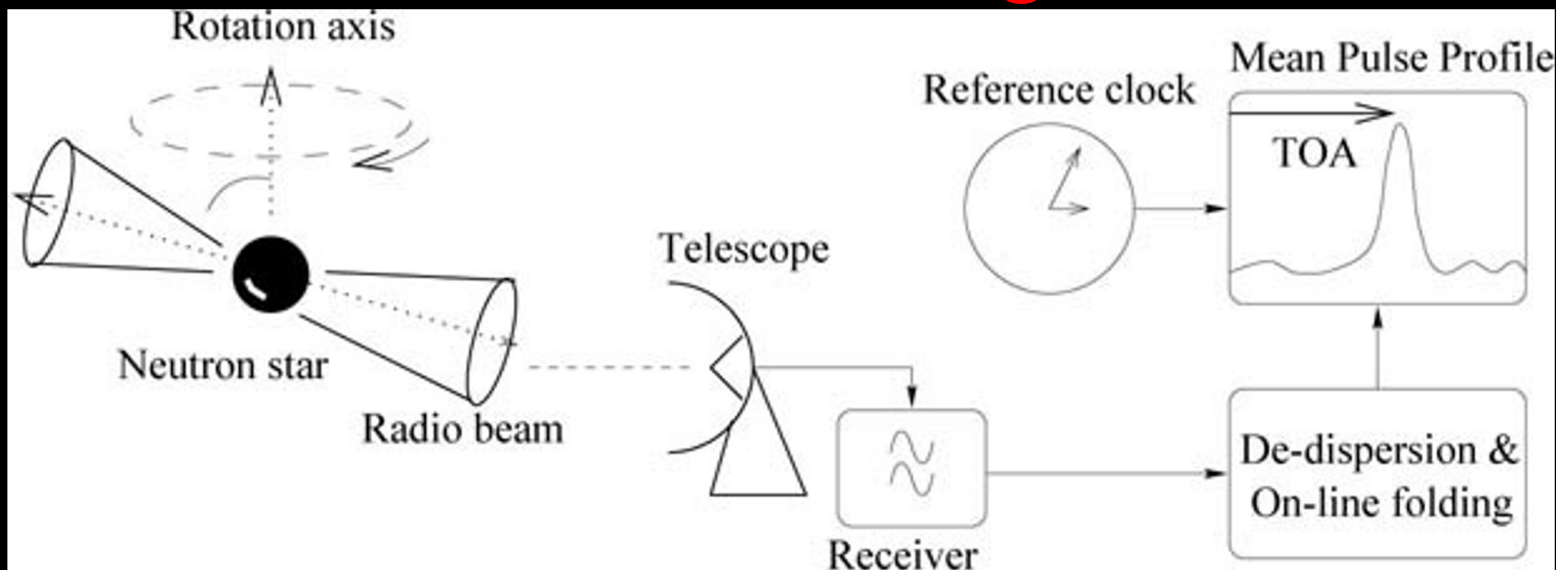
If the timing solution is perfect (and observations noiseless), then  $R=0$ .

$R$  contains all uncertainties related to the signal propagation and detection, plus





# Pulsar timing model



The N-th rotation of the pulsar is given in terms of the frequency as

$$N = N_0 + \nu\tau + \frac{1}{2}\dot{\nu}\tau^2 + \frac{1}{6}\ddot{\nu}\tau^3 + \dots$$

Which can be inverted to get the time of arrival of the N-th pulse

$$t_{\text{arr}} = \nu^{-1}N - \Delta_R(u) - \Delta_E(u) + \Delta_S(u) - \frac{1}{2}\dot{\nu}\nu^{-3}N^2 - \frac{1}{6}\ddot{\nu}\nu^{-4}N^3 + \dots$$

$$t_{\text{SSB}} = t_{\text{arr}} + t_{\text{clock}} + t_{\text{Earth}} + \text{DM}/f^2$$

(Hobbs+ 2006)

The timing model includes:

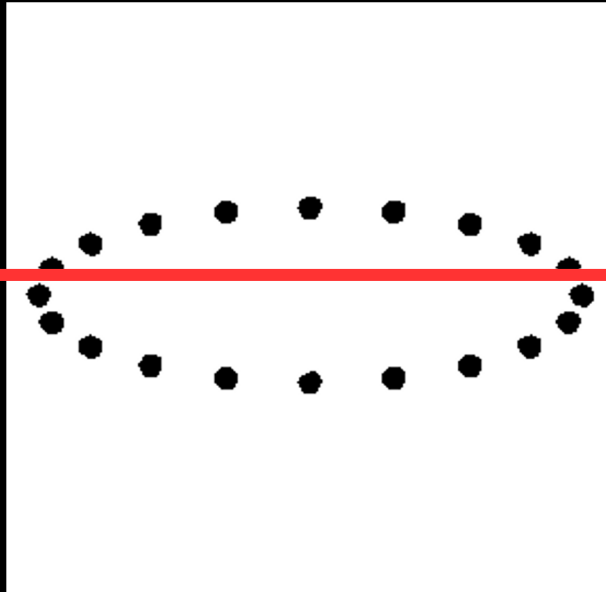
(Will 2006)

- Roemer, Einstein and Shapiro delays.
- pulsar frequency and freq derivatives
- pulsar position and proper motion
- dispersion measure
- clock corrections and Earth position wrt SSB

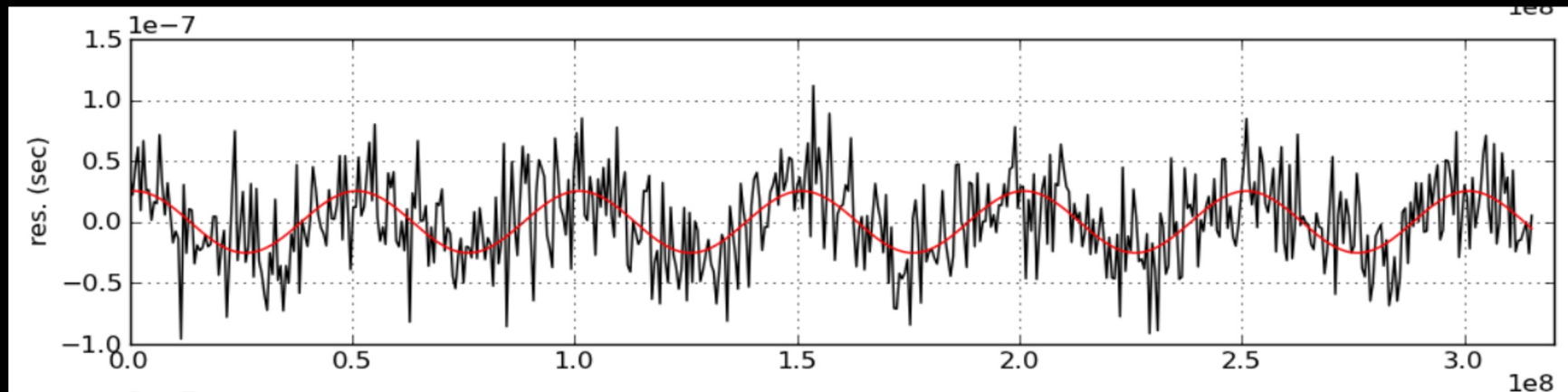
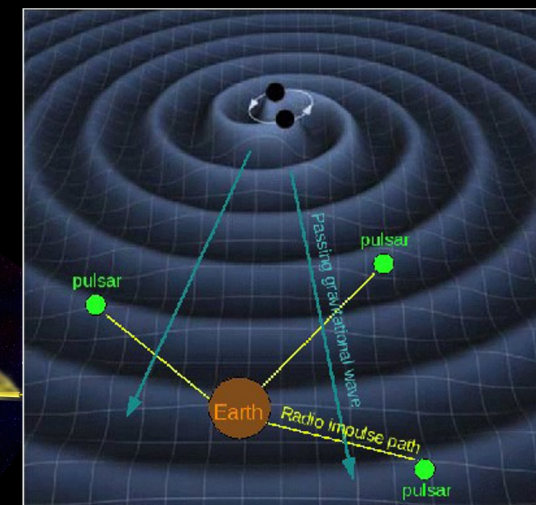
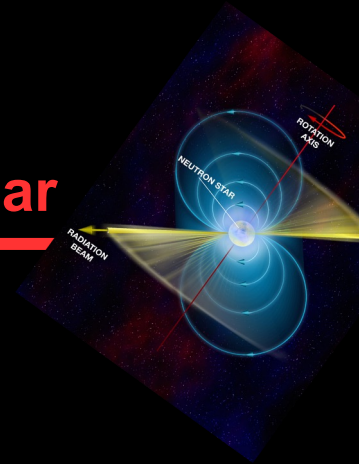
# Effect of gravitational waves



Earth



Pulsar

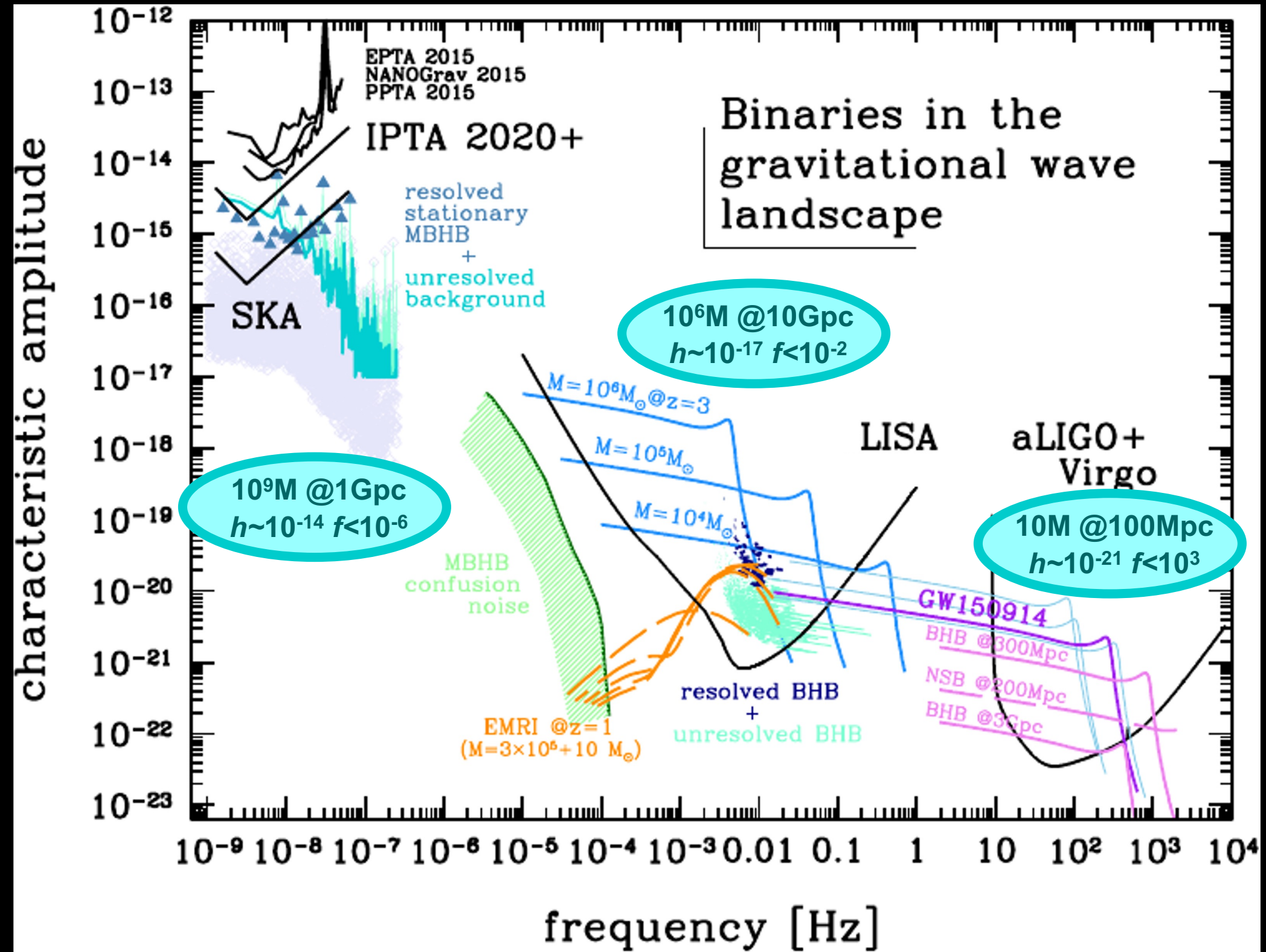


$$R \sim h / (2\pi f)$$

$$= \frac{\mathcal{M}^{5/3}}{D} [\pi f(t)]^{-1/3}$$

$$\simeq 25.7 \left( \frac{\mathcal{M}}{10^9 M_\odot} \right)^{5/3} \left( \frac{D}{100 \text{ Mpc}} \right)^{-1}$$

$$\times \left( \frac{f}{5 \times 10^{-8} \text{ Hz}} \right)^{-1/3} \text{ ns}$$





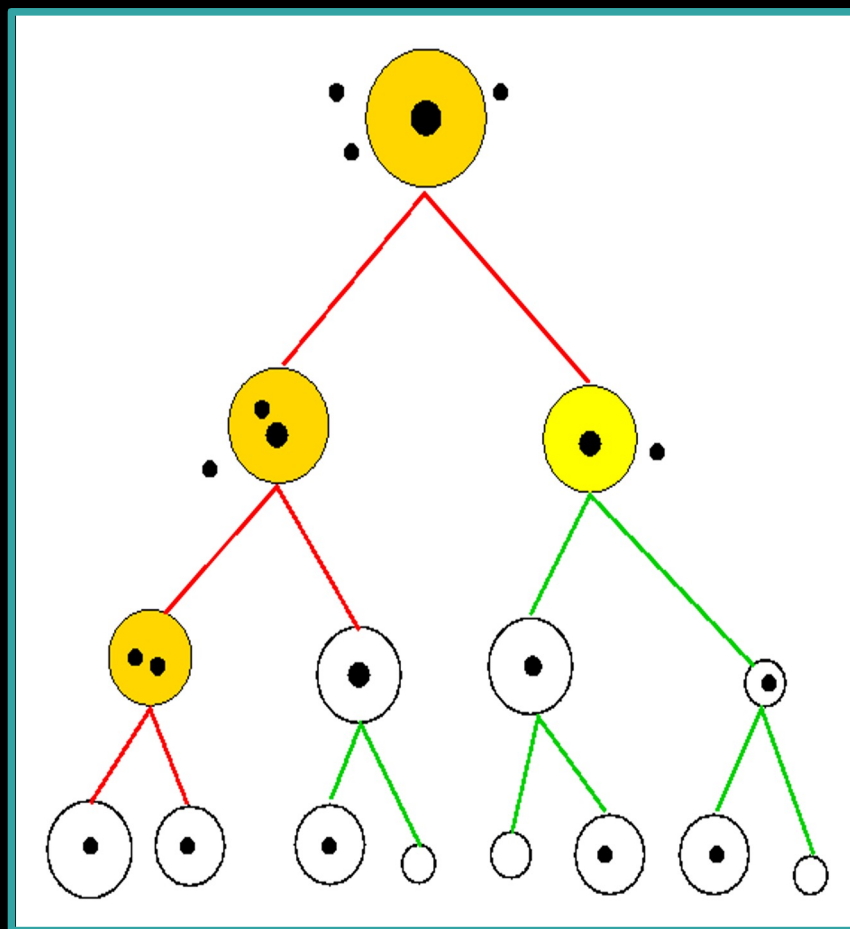
# HIERARCHICAL GALAXY & MBH EVOLUTION

## GENERAL FRAMEWORK:

Galaxies form hierarchically through a series of mergers and accretion events

Protogalaxies can host seed BH that accrete mass and merge with each other following galaxy mergers

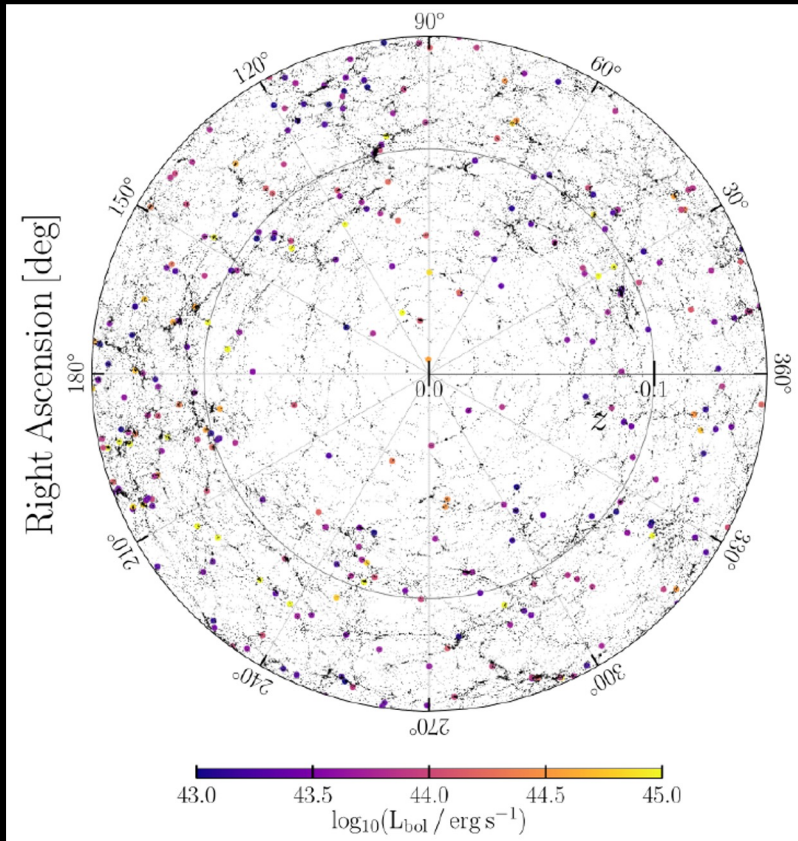
(Volonteri, Haardt & Madau 2003)



(Illustris simulation)

# The expected GW signal in the PTA band

(Izquierdo-Villalba+ 22)



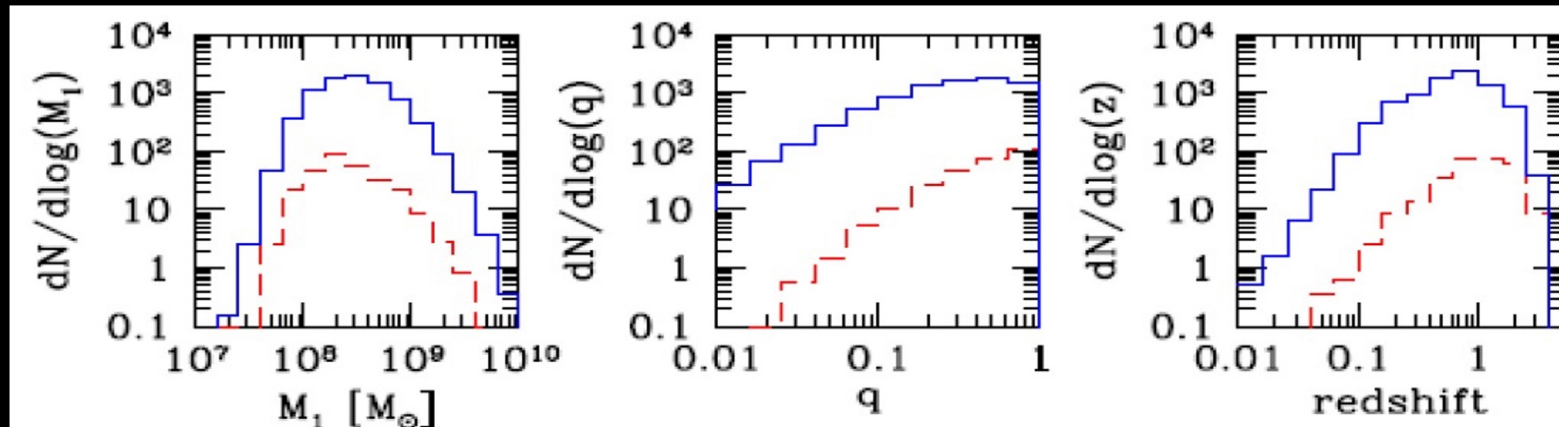
The GW characteristic amplitude coming from

$$h_c^2(f) = \int_0^\infty dz \int_0^\infty d\mathcal{M} \frac{d^3 N}{dz d\mathcal{M} d\ln f_r} h^2(f_r)$$

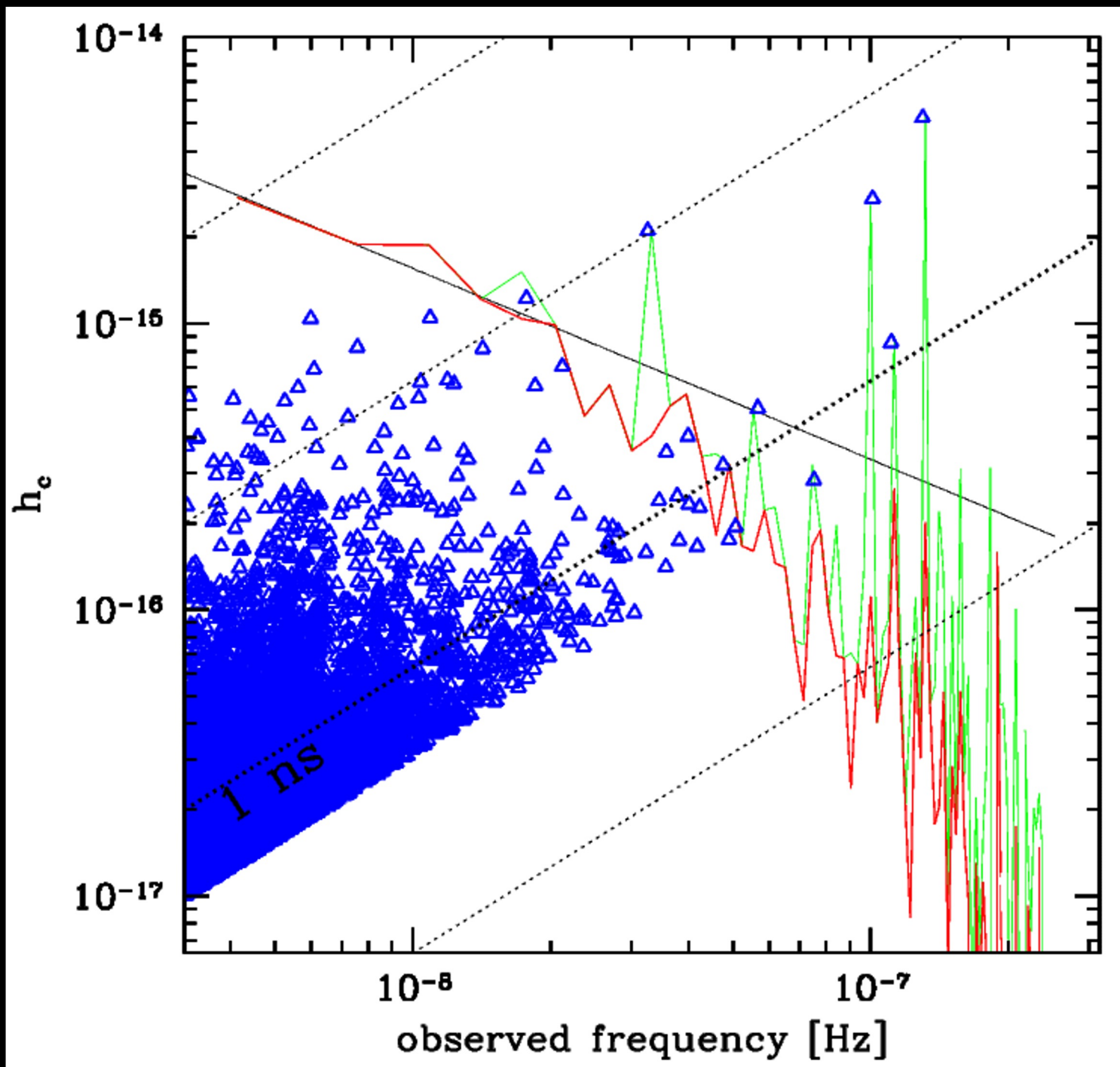
$$\delta t_{\text{bkg}}(f) \approx h_c(f)/(2\pi f)$$

Theoretical spectrum: simple power law (I)

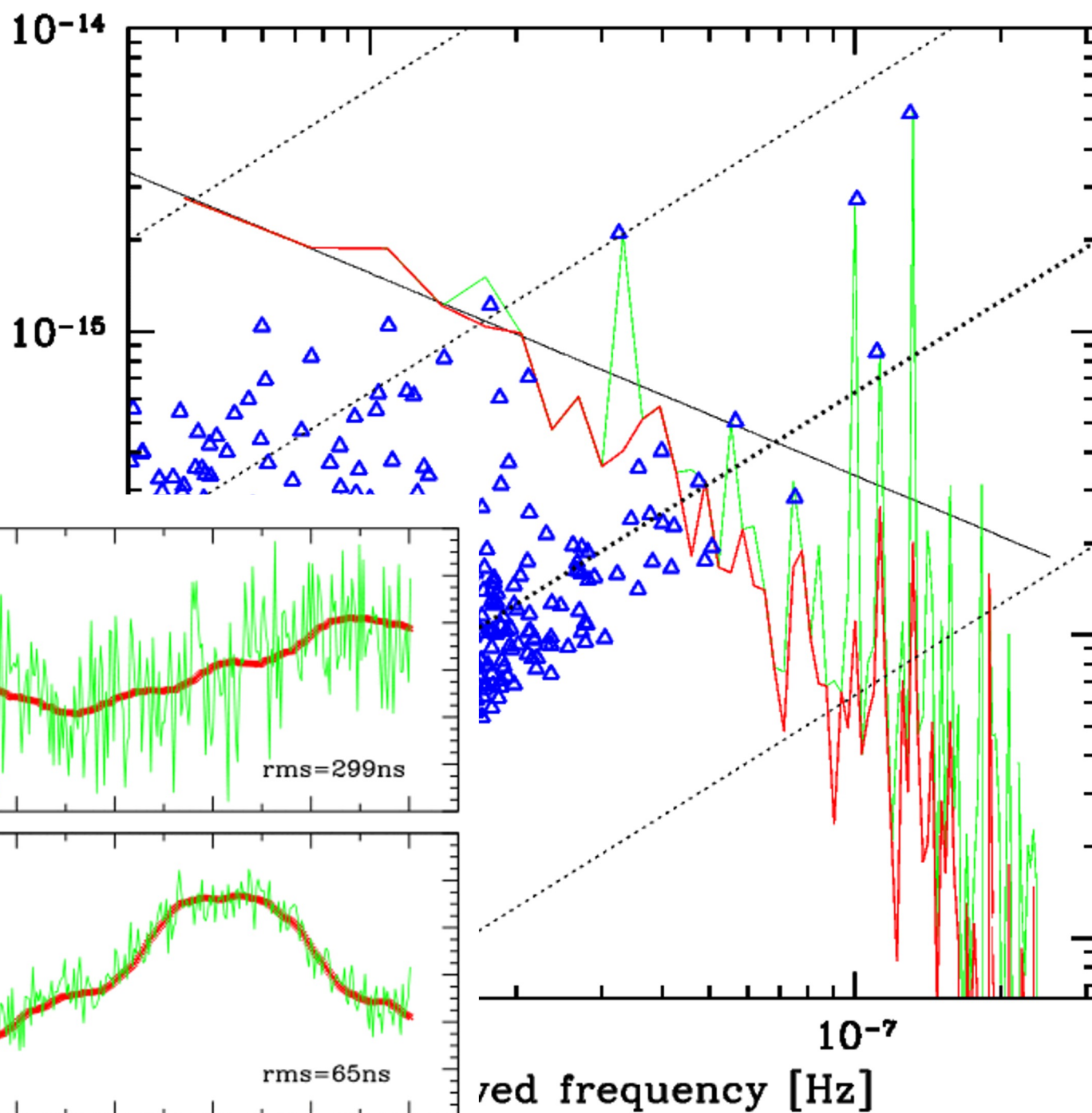
$$h_c(f) = A \left( \frac{f}{\text{yr}^{-1}} \right)^{-2/3}$$

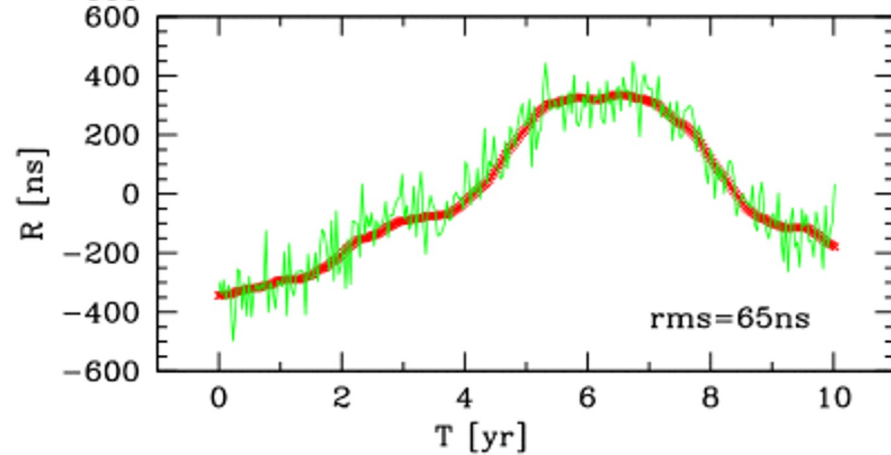
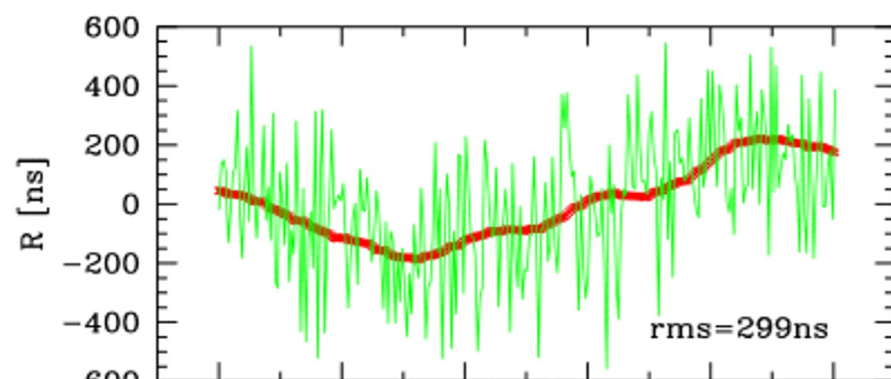
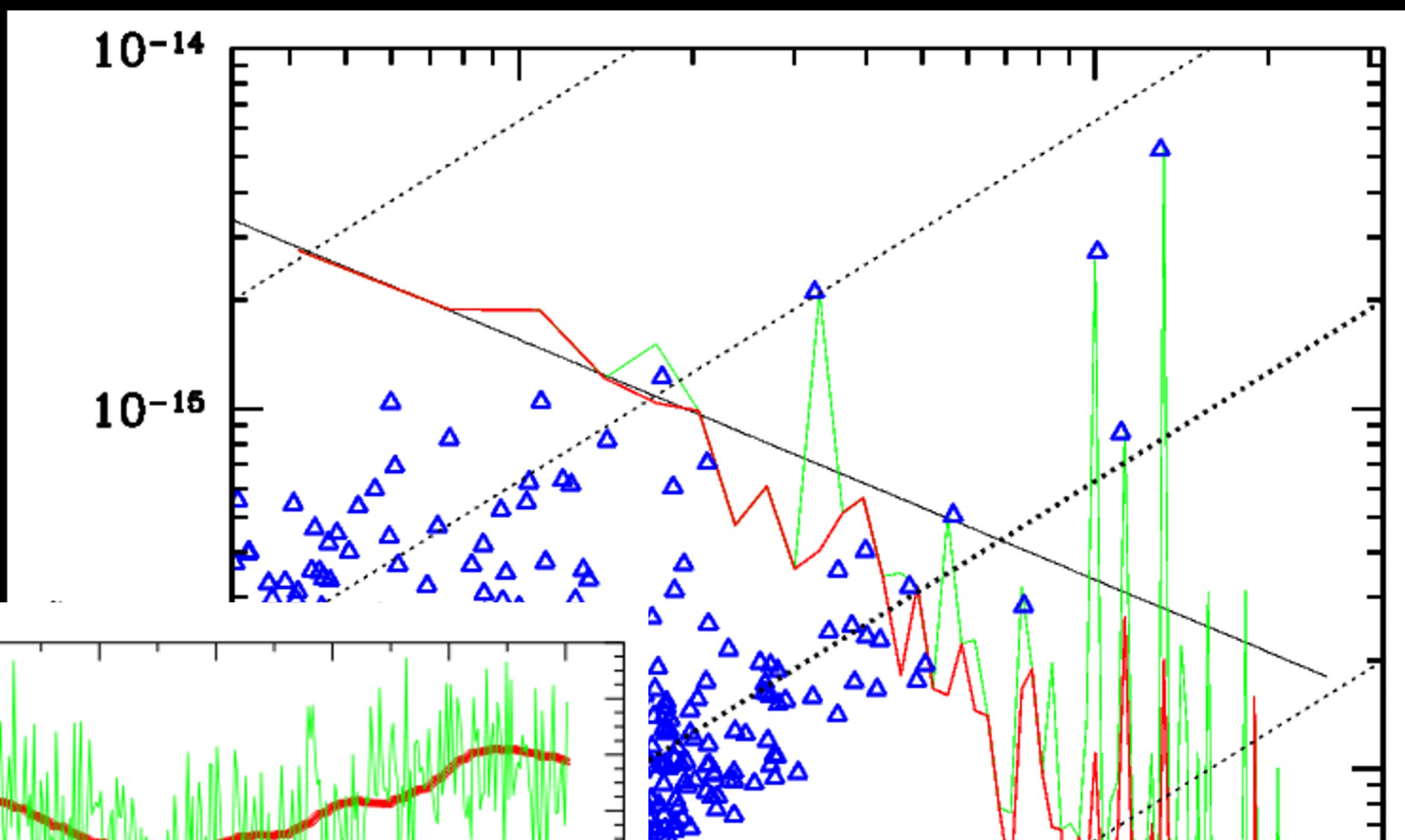


The signal is contributed by extremely massive ( $>10^8 M_\odot$ ) relatively low

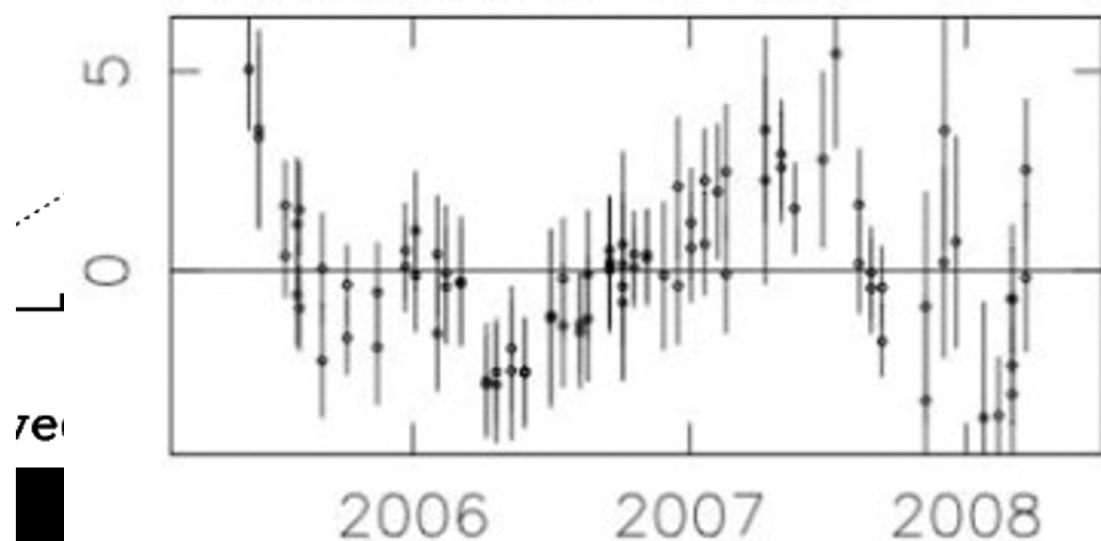






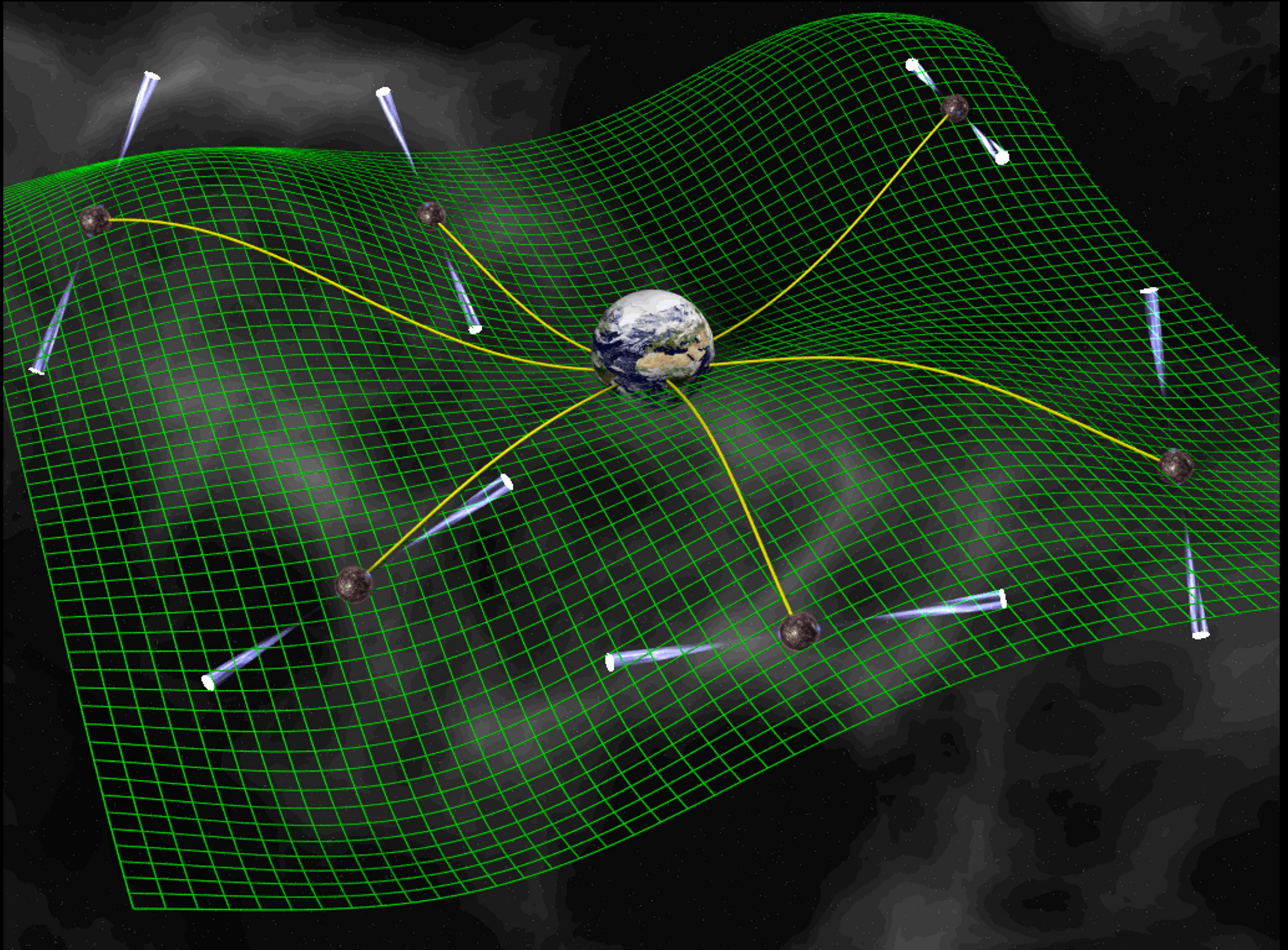


PSR J1824-2452



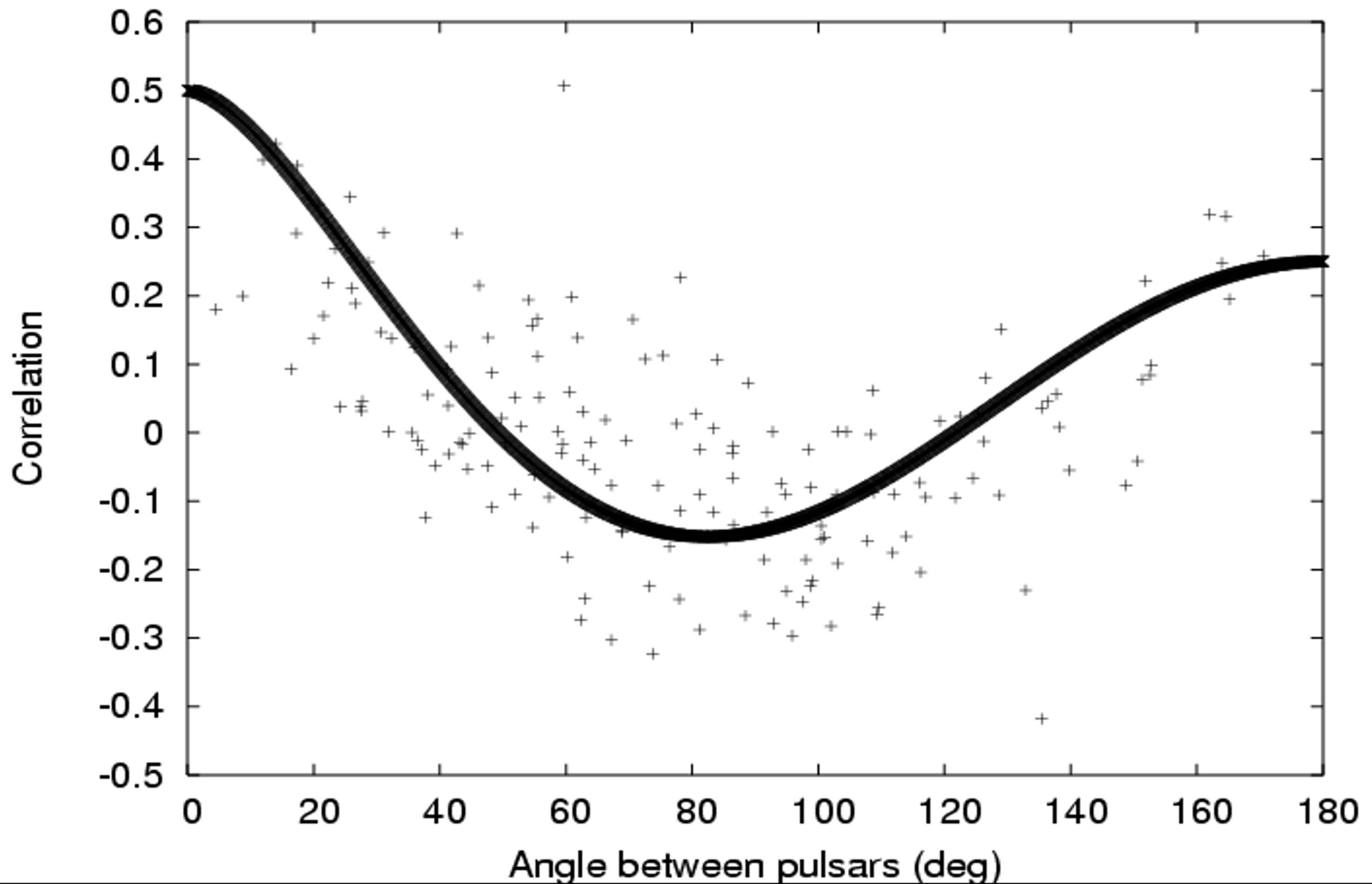


***We are looking for a correlated signal***

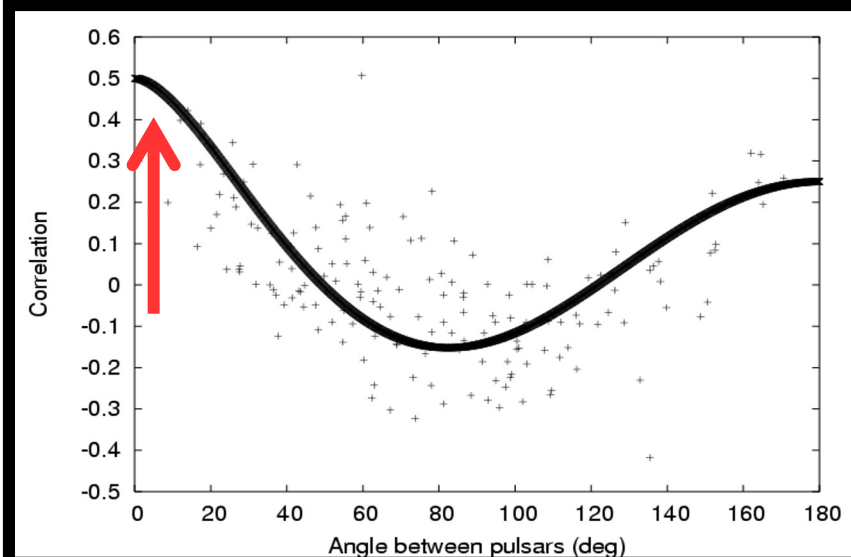
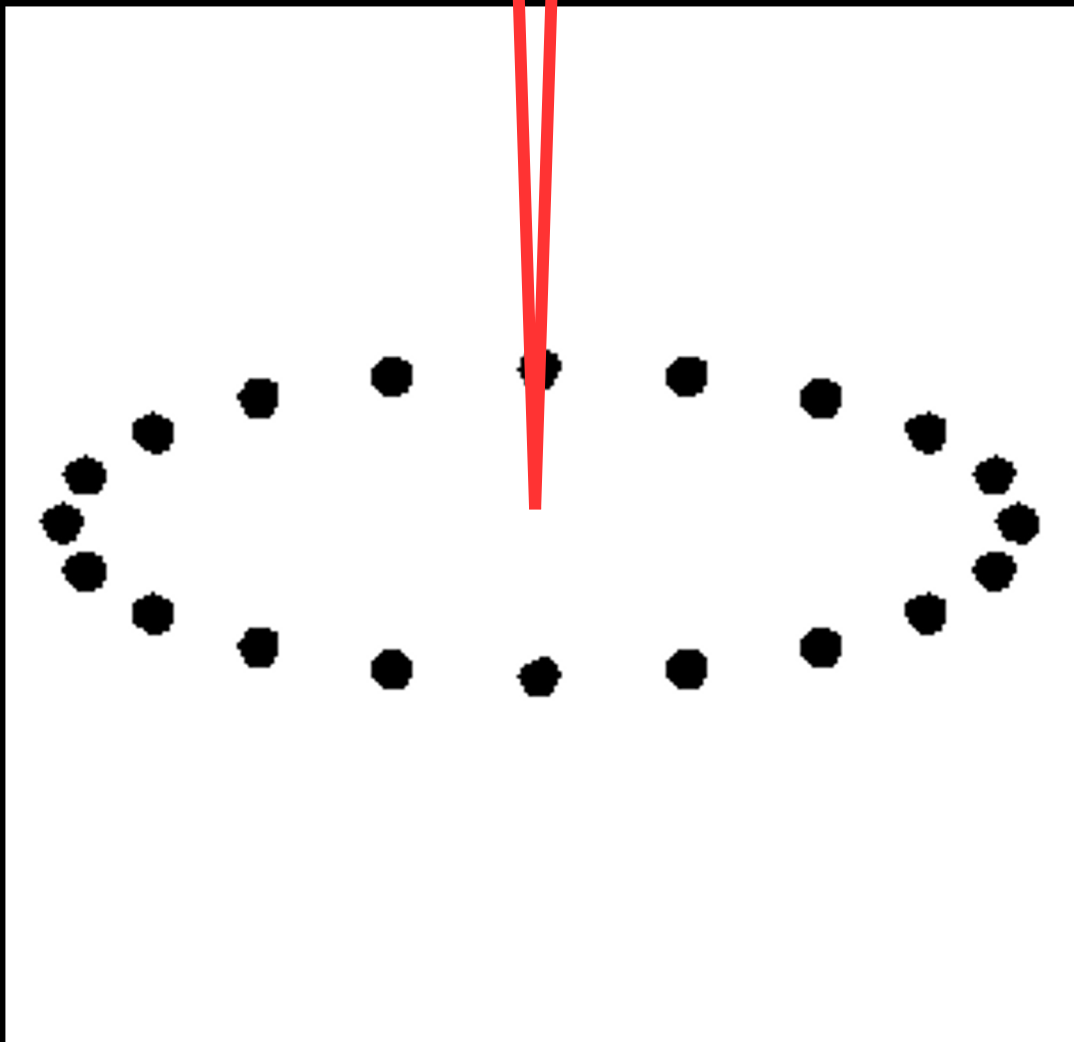


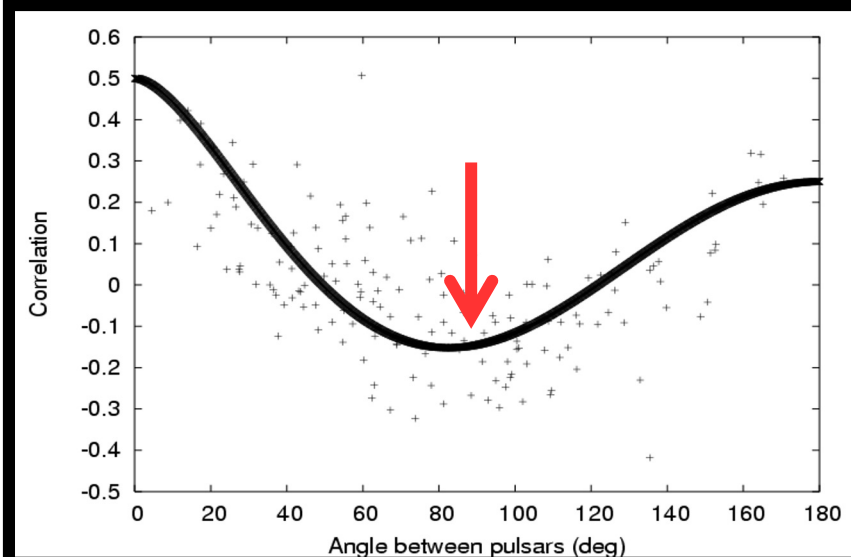
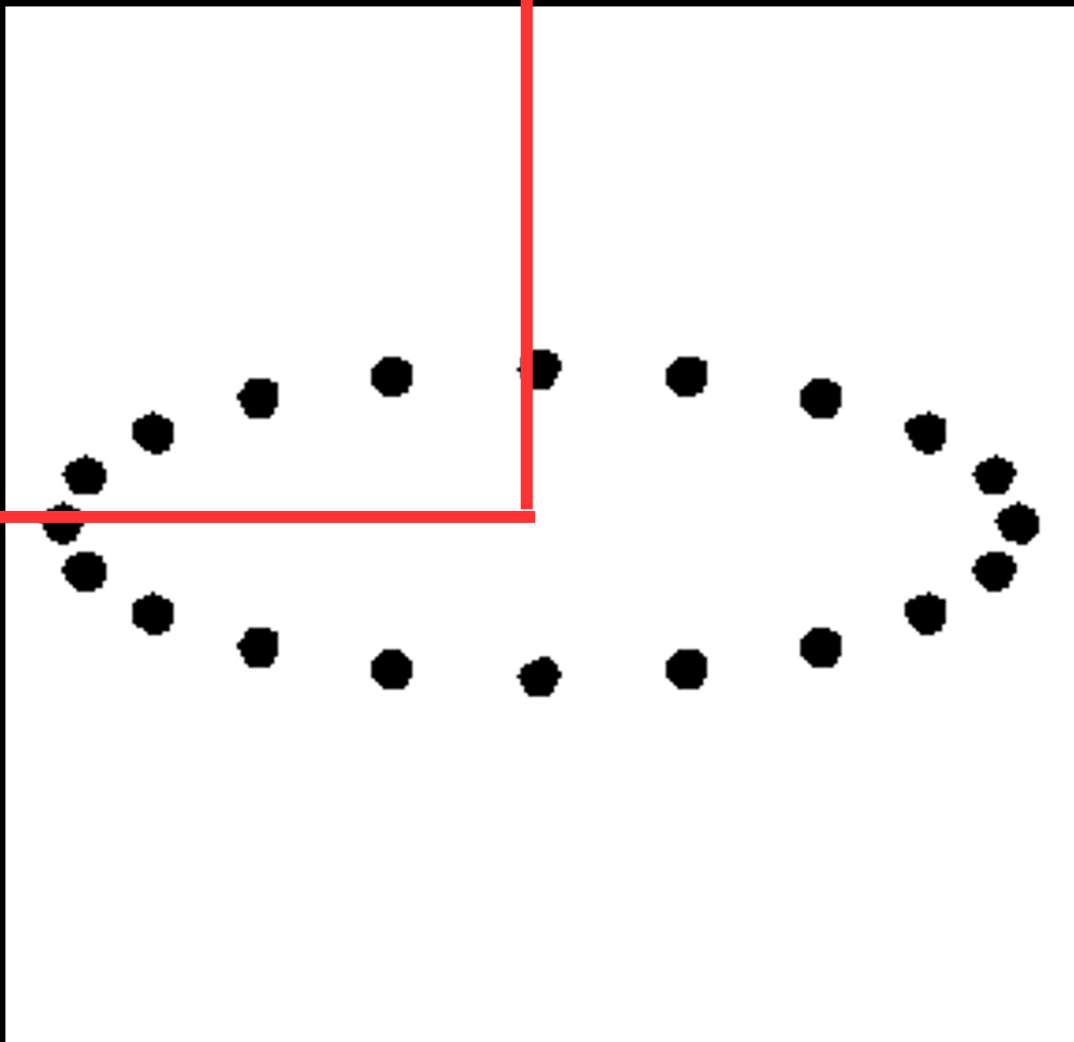


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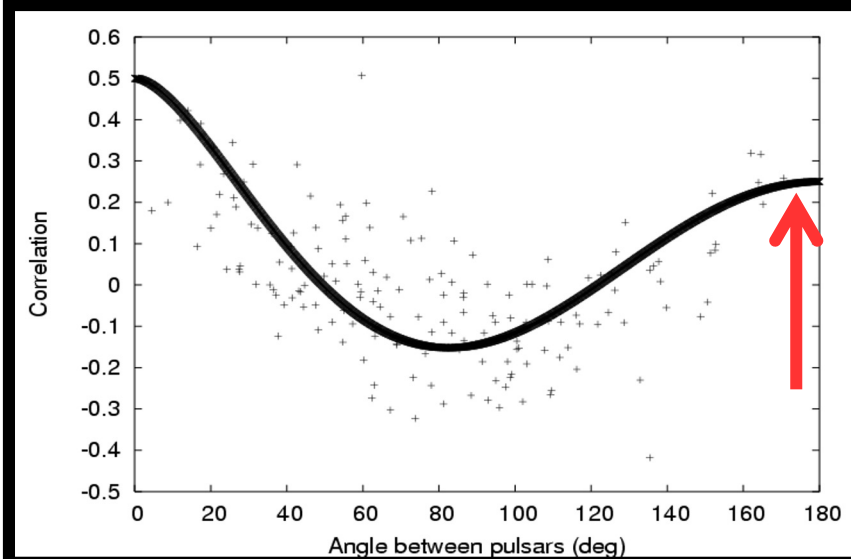
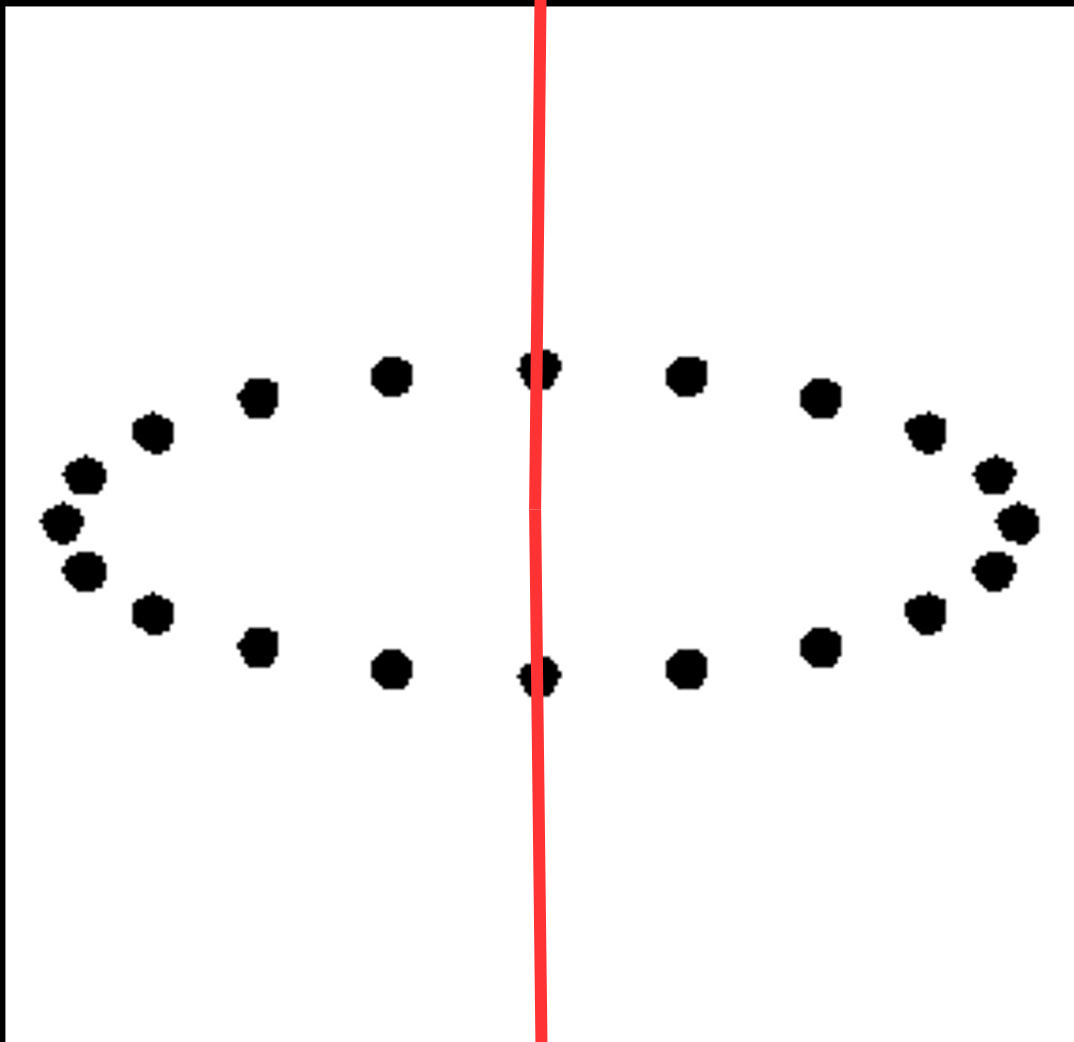


**(Hellings & Downs 1983)**







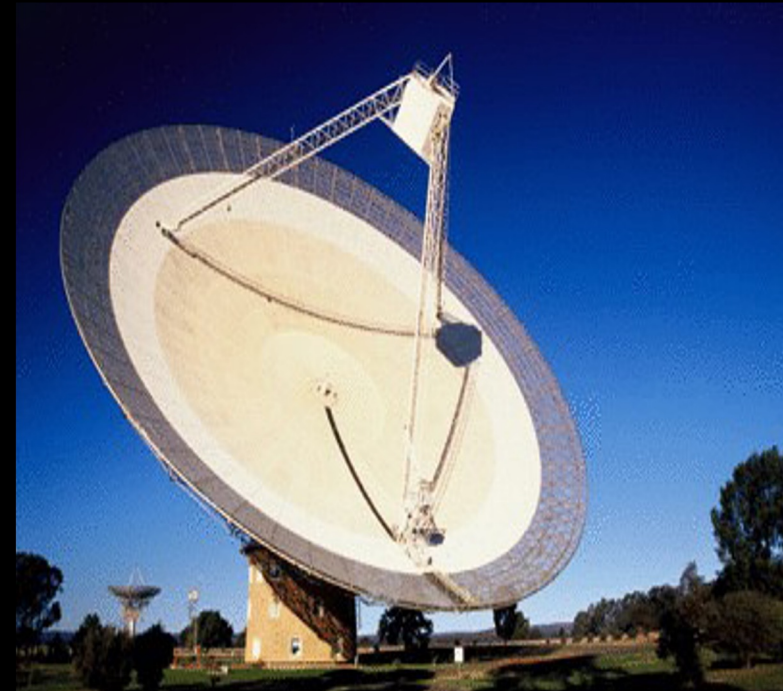


# *A worldwide observational effort*

**EPTA/LEAP** (Large European Array for Pulsars)



**NANOGrav** (North American nHz Observatory)



**PPTA** (Parkes Pulsar Timing Array)

- +InPTA (India)
- +CPTA (China)
- +MeerKAT (South Africa)



# *A worldwide observational effort*

**EPTA/LEAP** (La



**PPTA**

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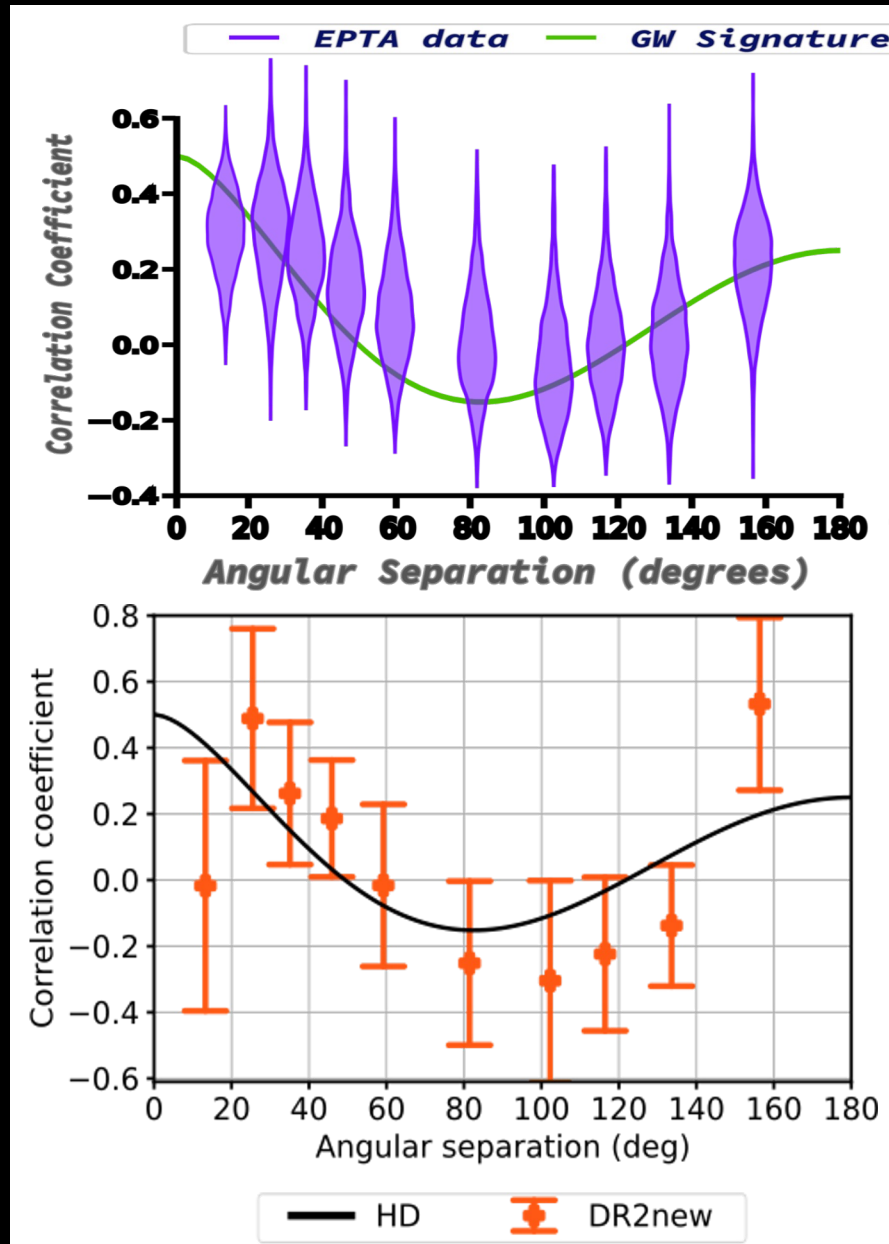


nHz Observatory

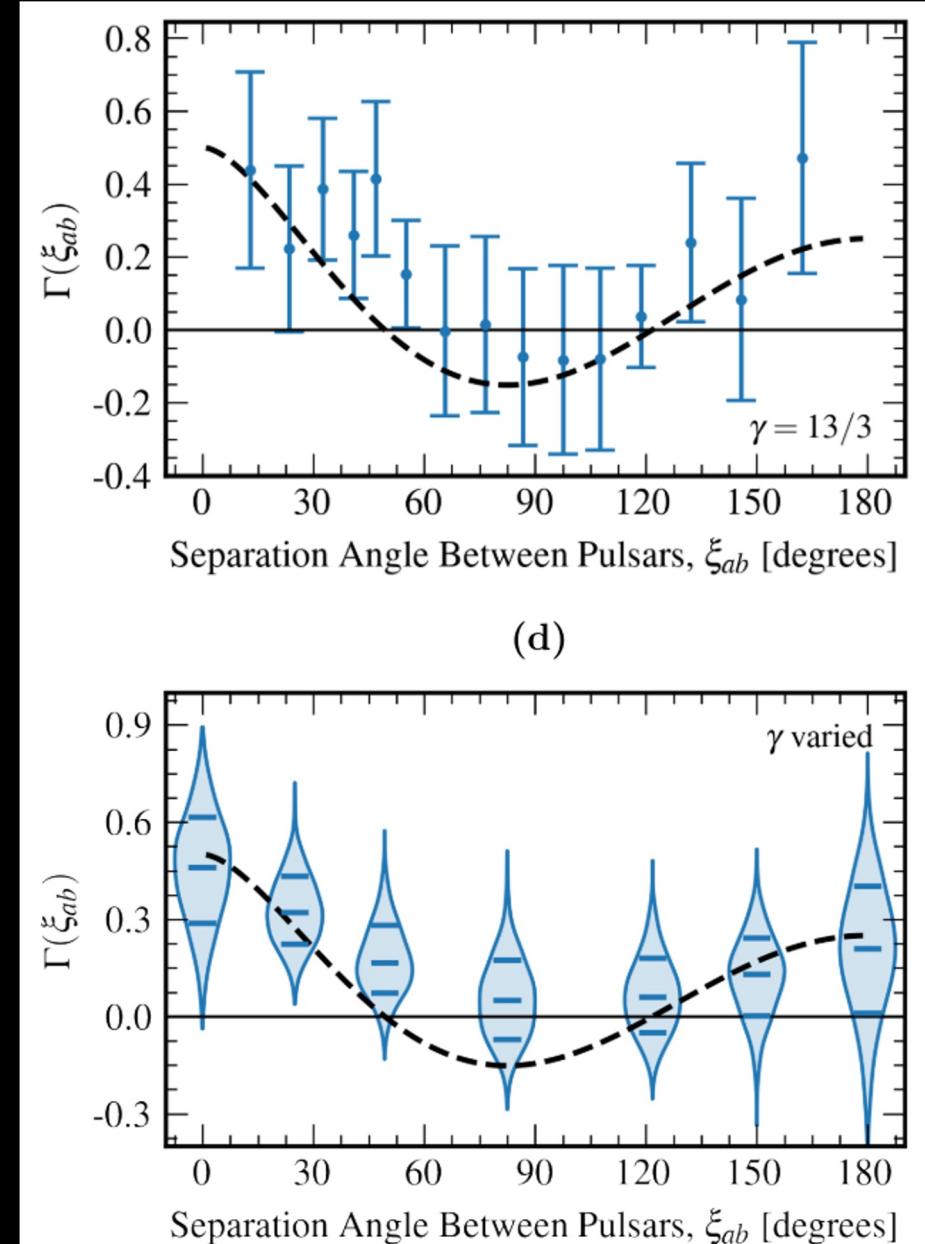




# Evidence for GW signal

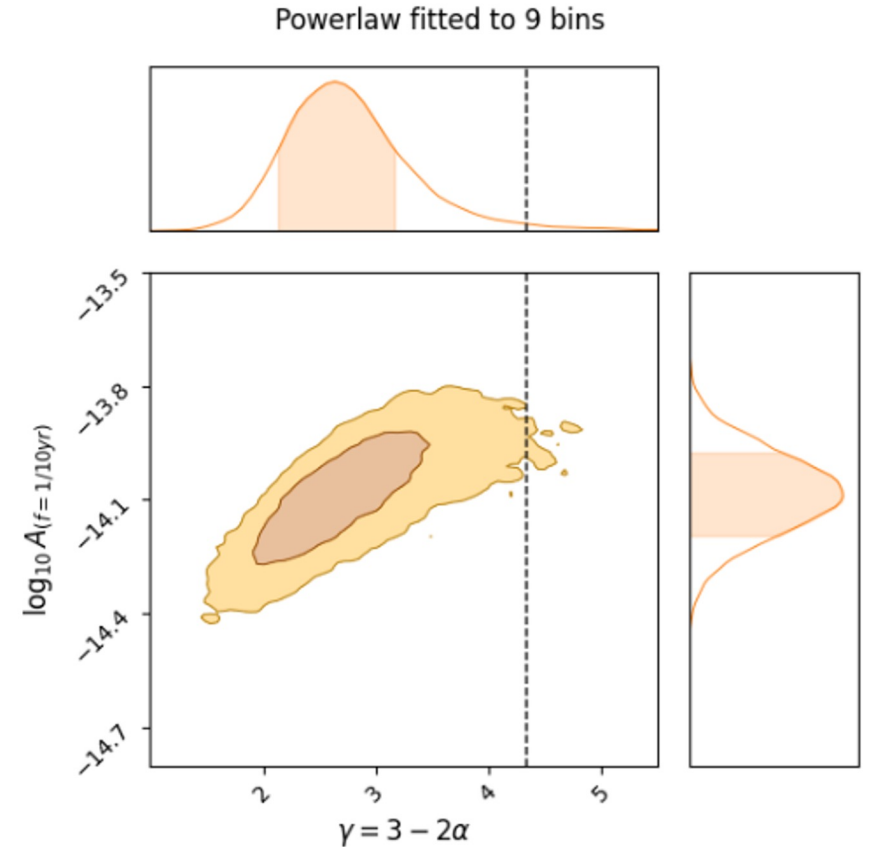
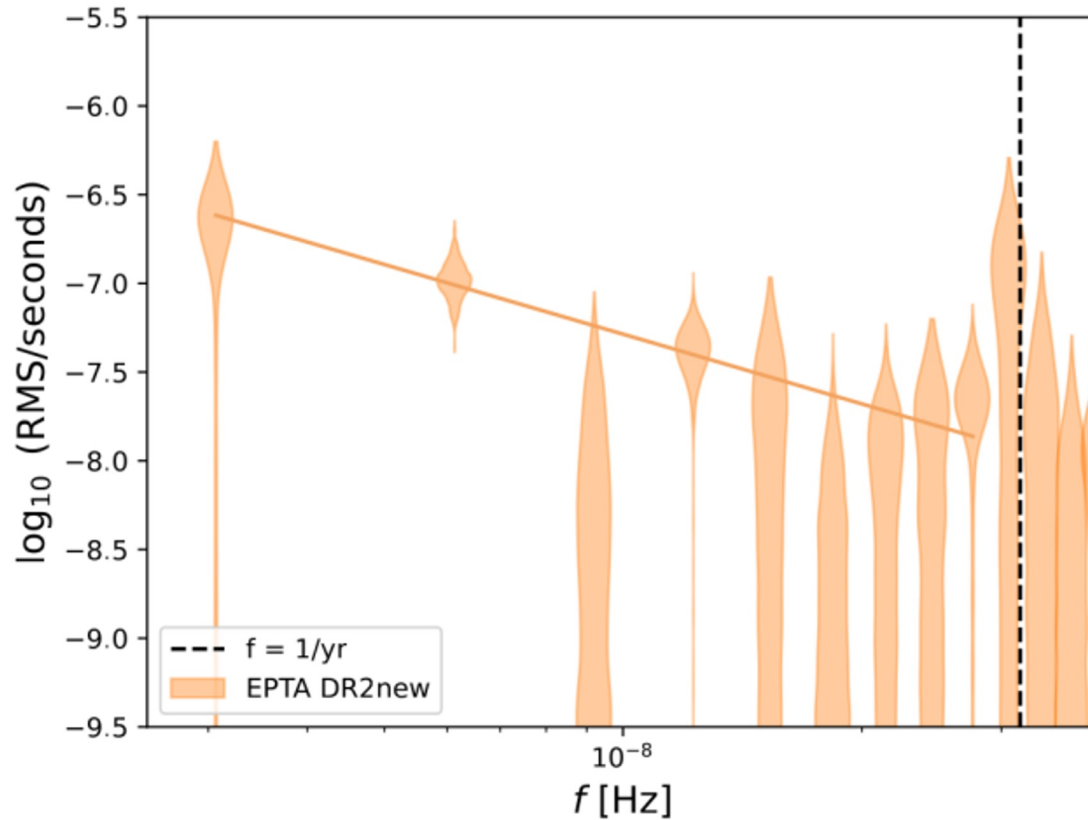


(Antoniadis+23)



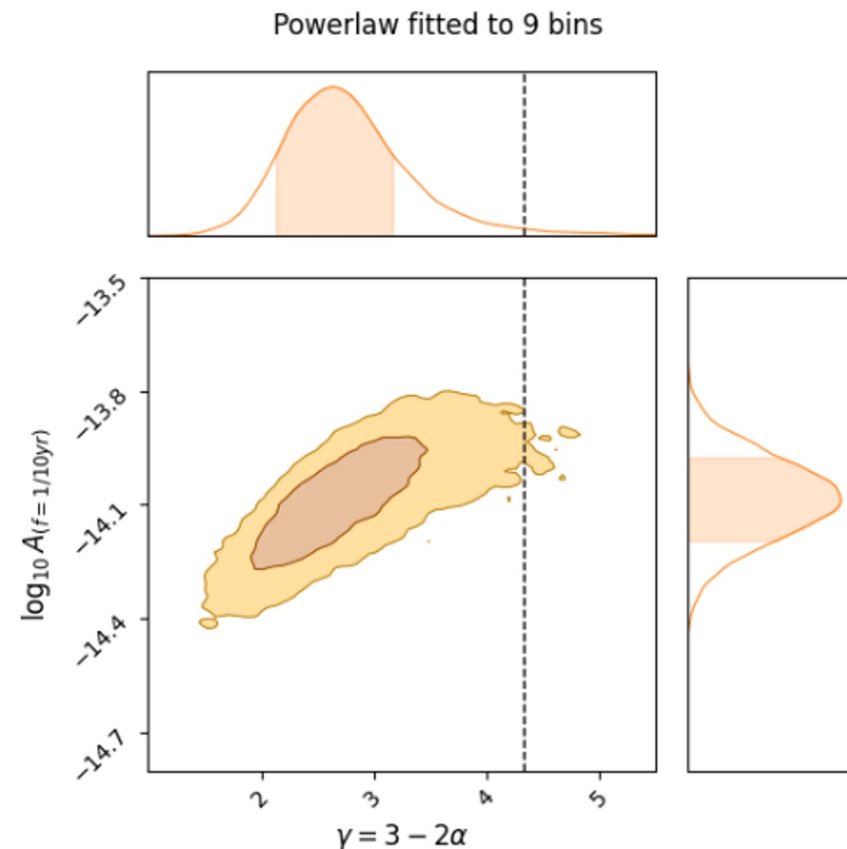
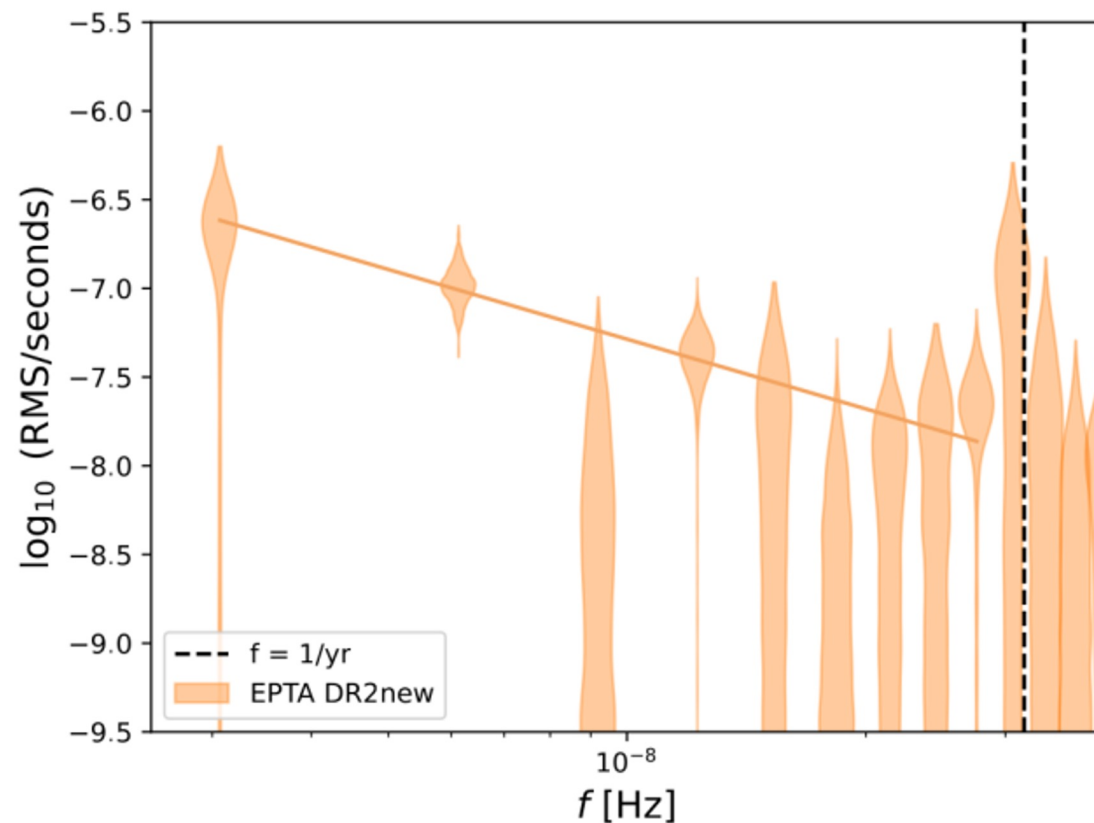
(Agazie+23)

# Results of EPTA DR2



- 4 dataset produced: using DR2new here (only new backend)
- HD correlated signal favoured with Bayes factor~60
- power constrained in few bins at low freq
- powerlaw fit:  $\gamma \sim 2.7$   $A \sim -14$  [ $A(\gamma=13/3) \sim -14.6$ ]

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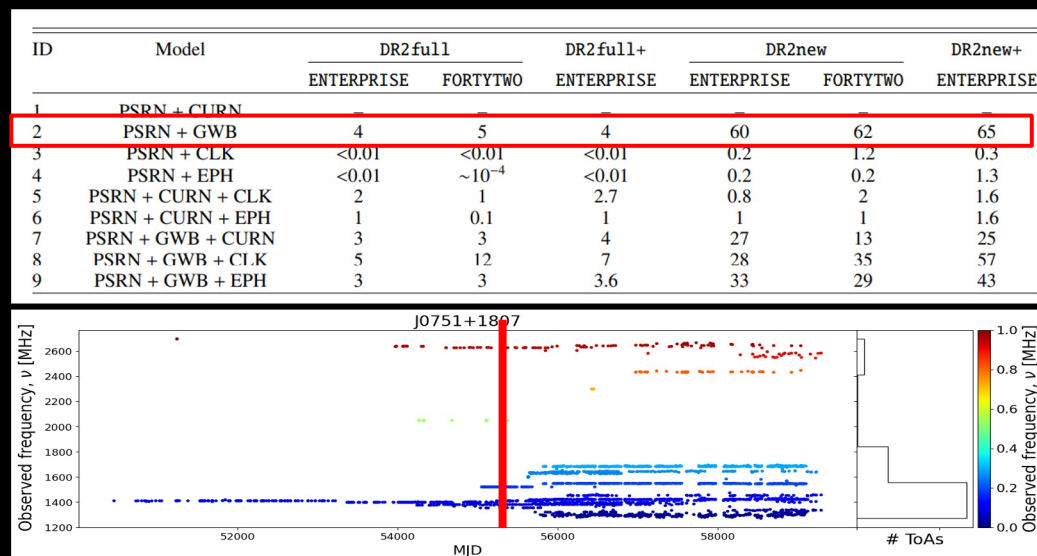
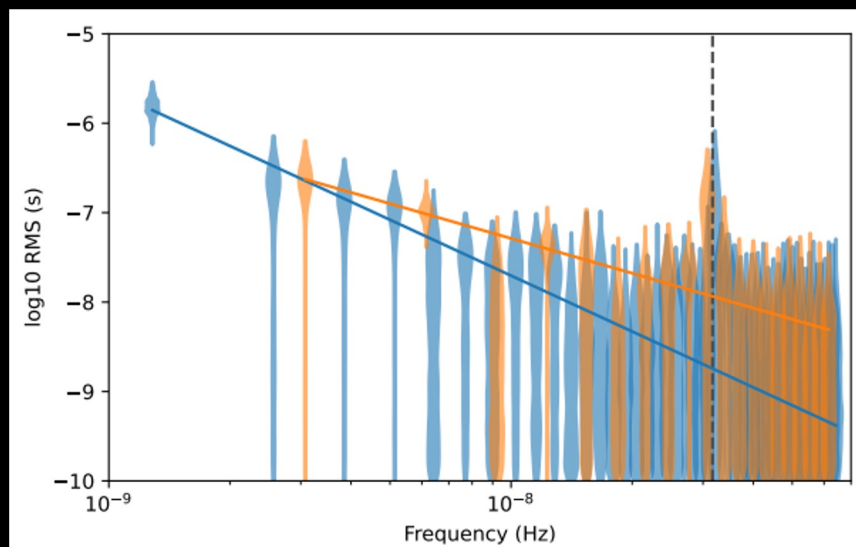


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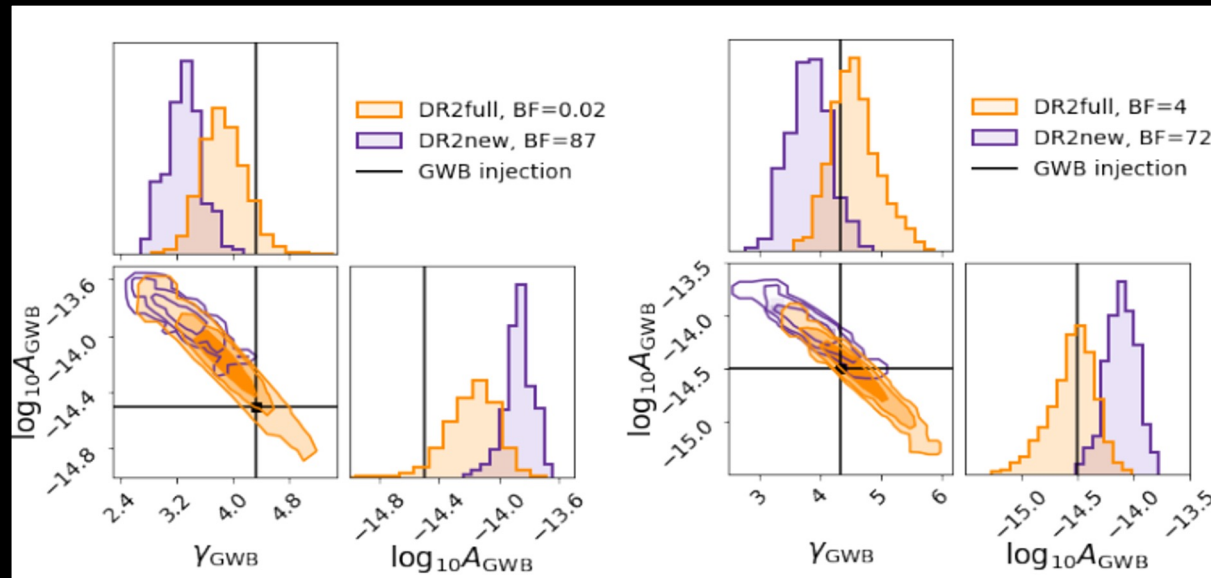
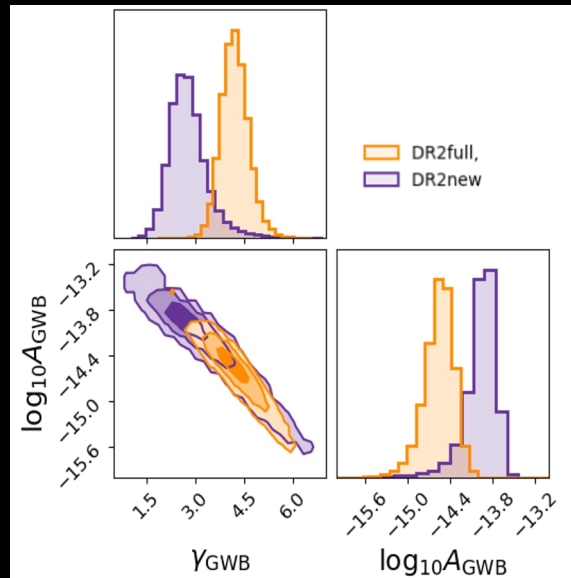
THINGS YOU HEAR: “too flat for SMBHBs [add your favorite early



# EPTA DR2full vs DR2new

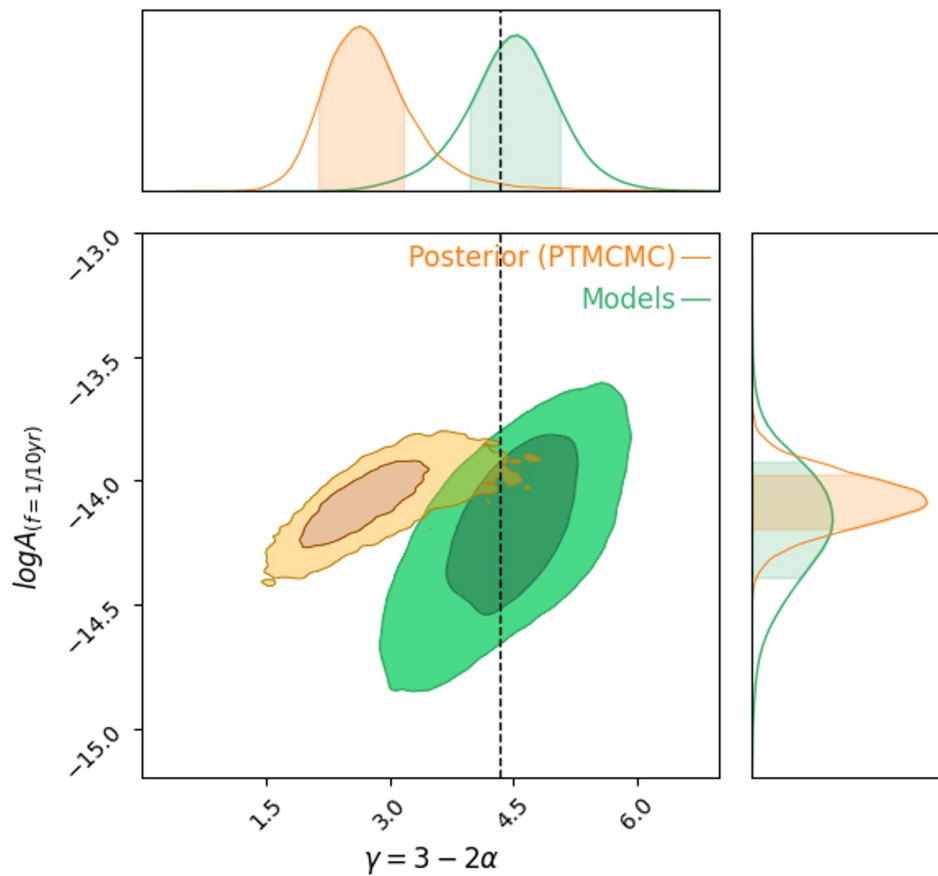


DR2new yields higher significance despite having shorter baseline!



This is possible due to lack of frequency coverage in the old data (Ferranti et al.)

Powerlaw fitted to 9 bins



**A- gamma plots broadly consistent**

**A normalized @1/10yr**

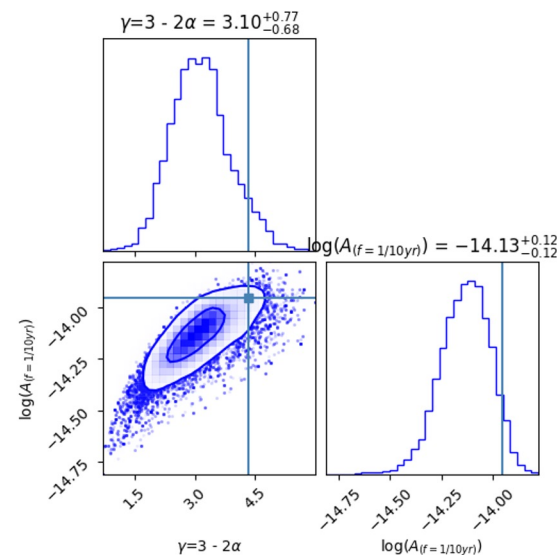
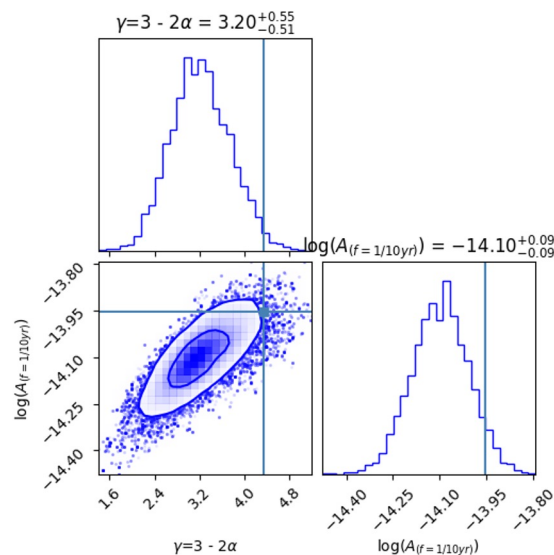
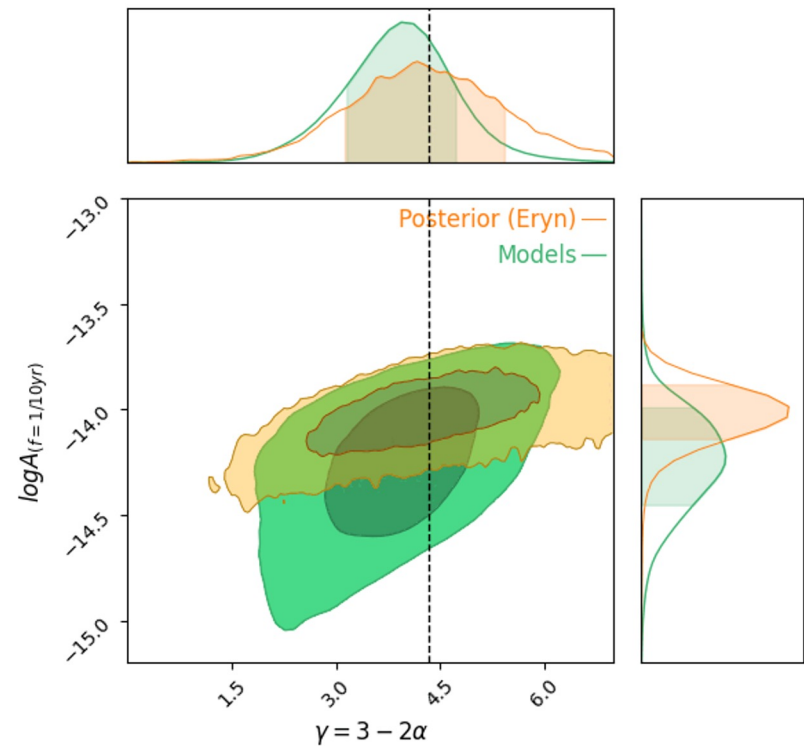
**Warning:**

-fits and measurements depend on numbers of

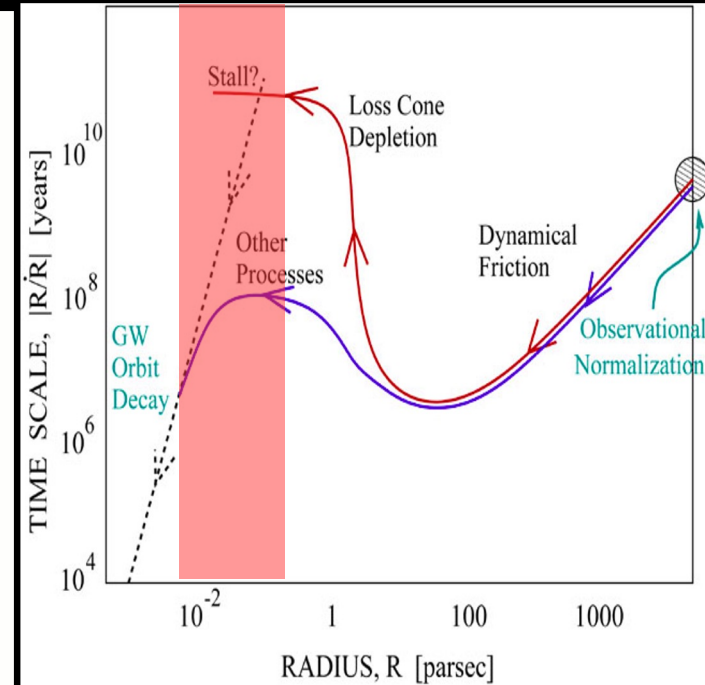
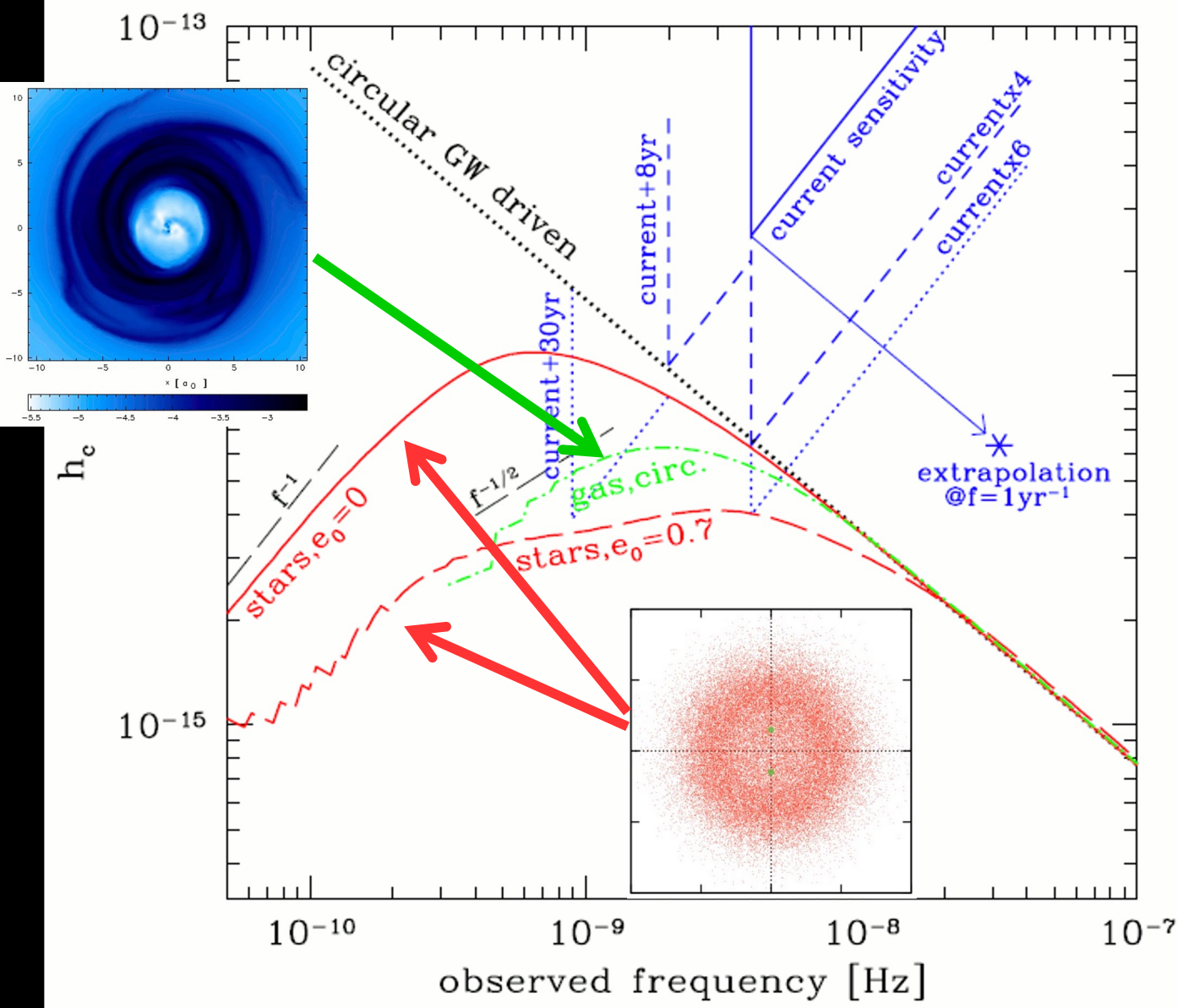
-measured flat value could be due to low SNR

(Valtolina+24)

Powerlaw fitted to 3 bins



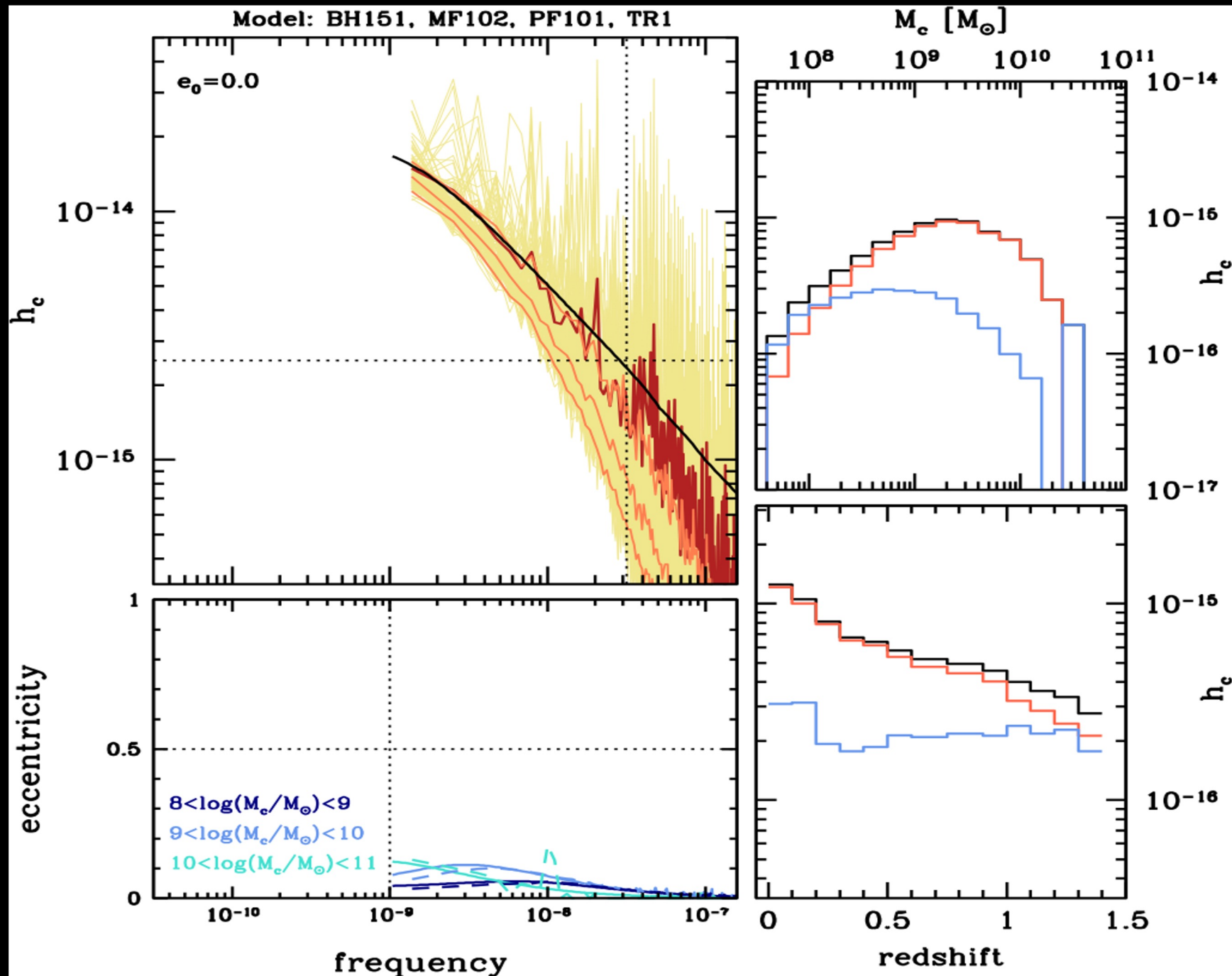
# Uncertainty in the GW background shape



(Kocsis & AS 2011, AS 2013, Ravi et al. 2014, McWilliams et al. 2014)

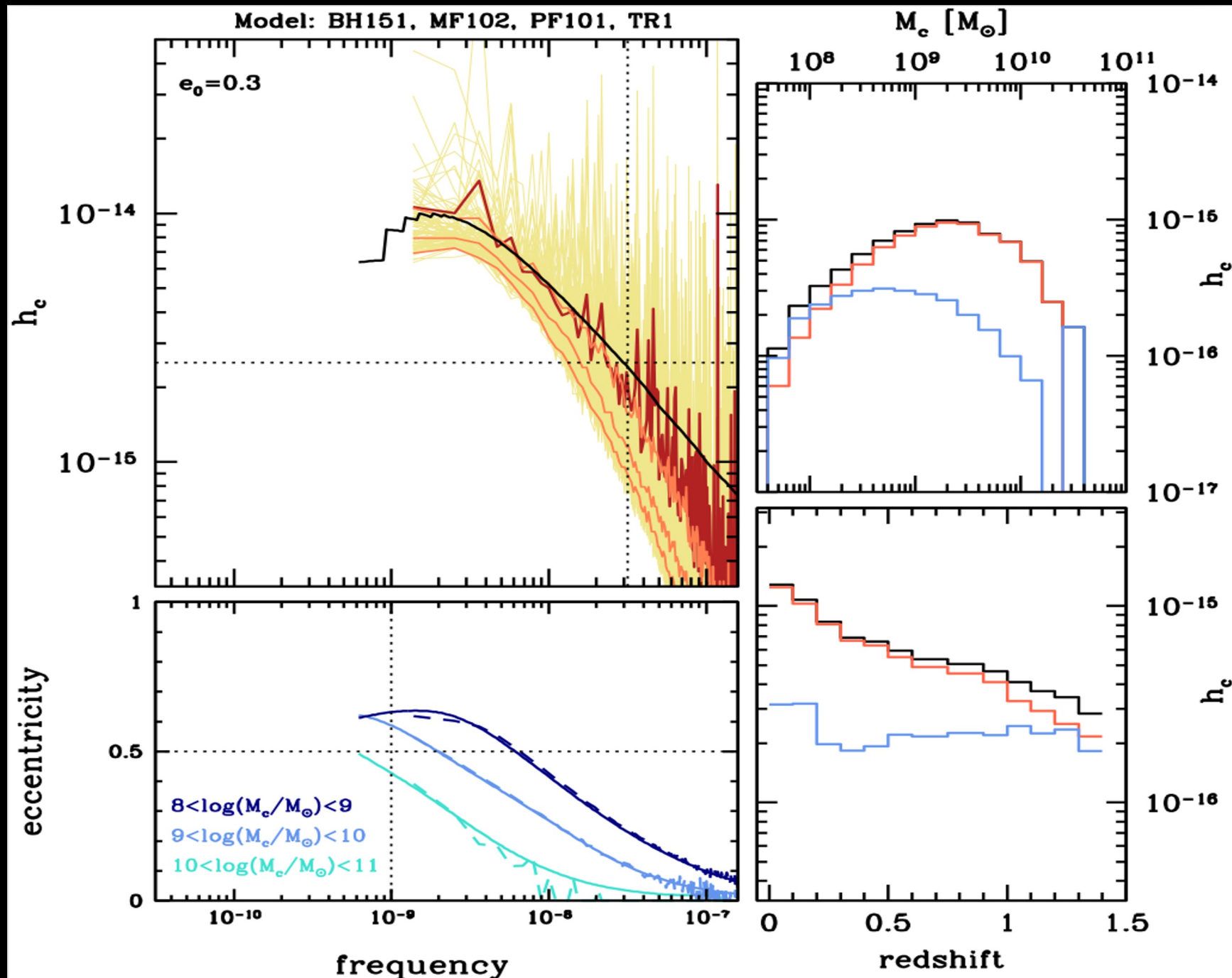


# Eccentricity



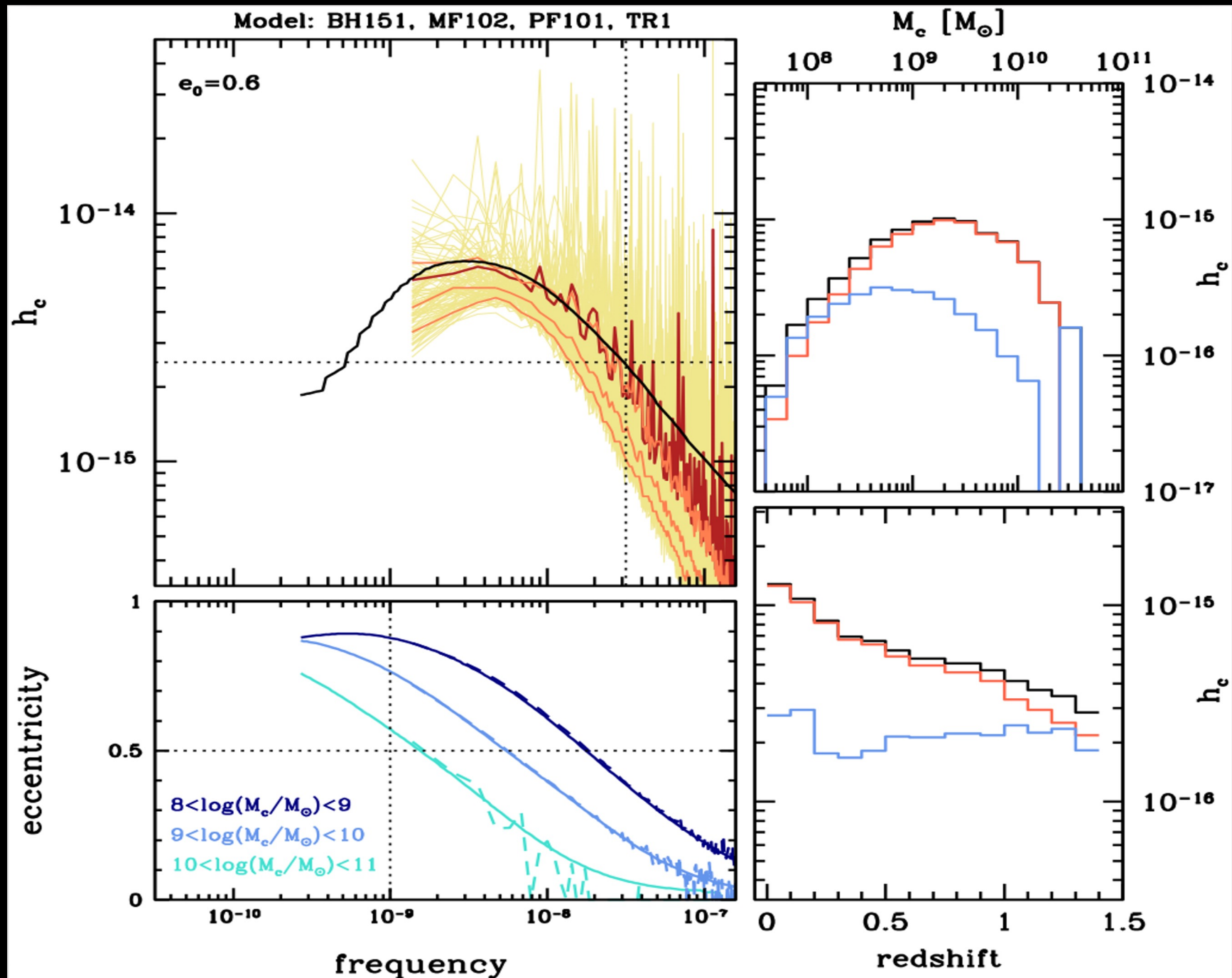
It might even be the dominant effect for flattening.

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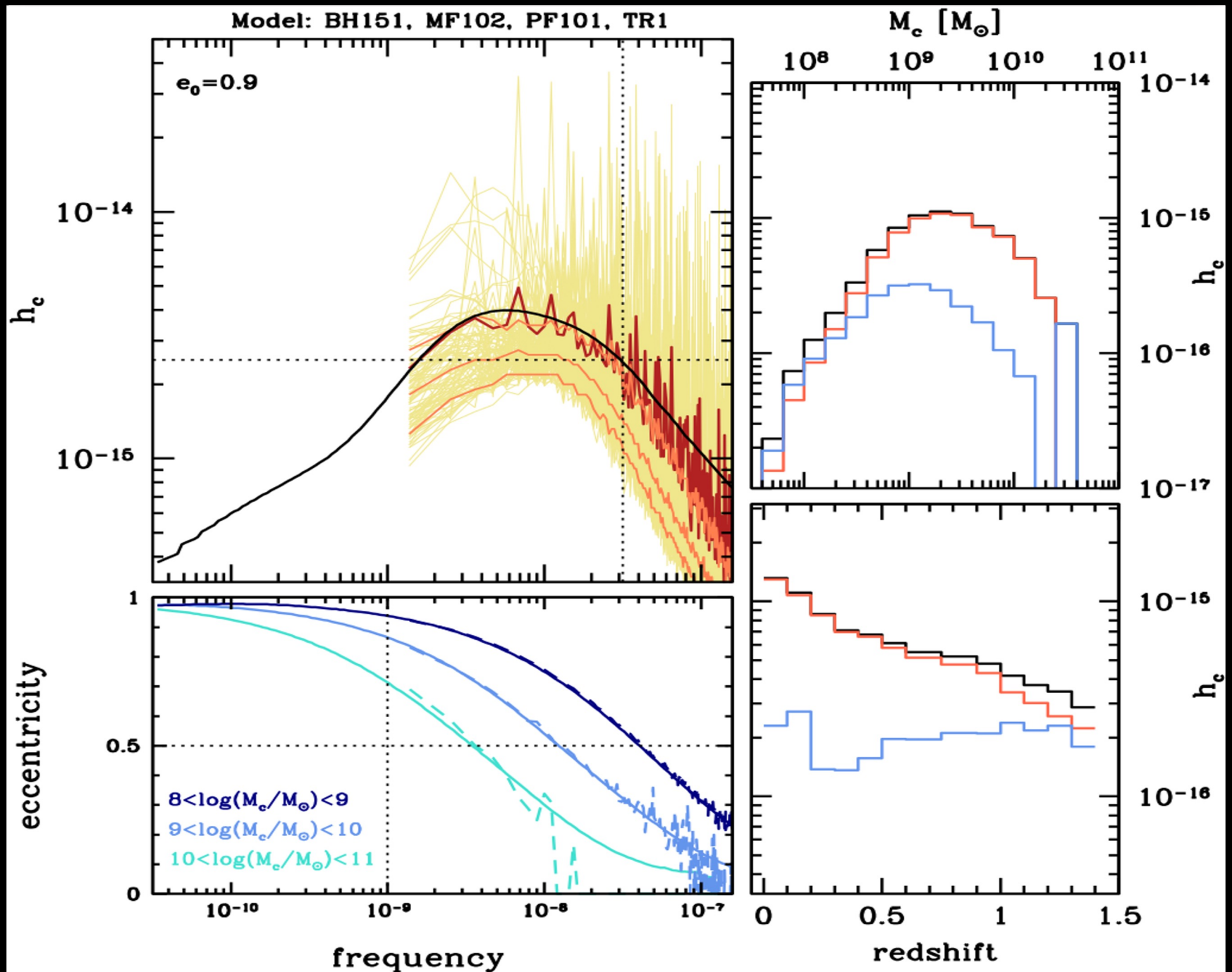
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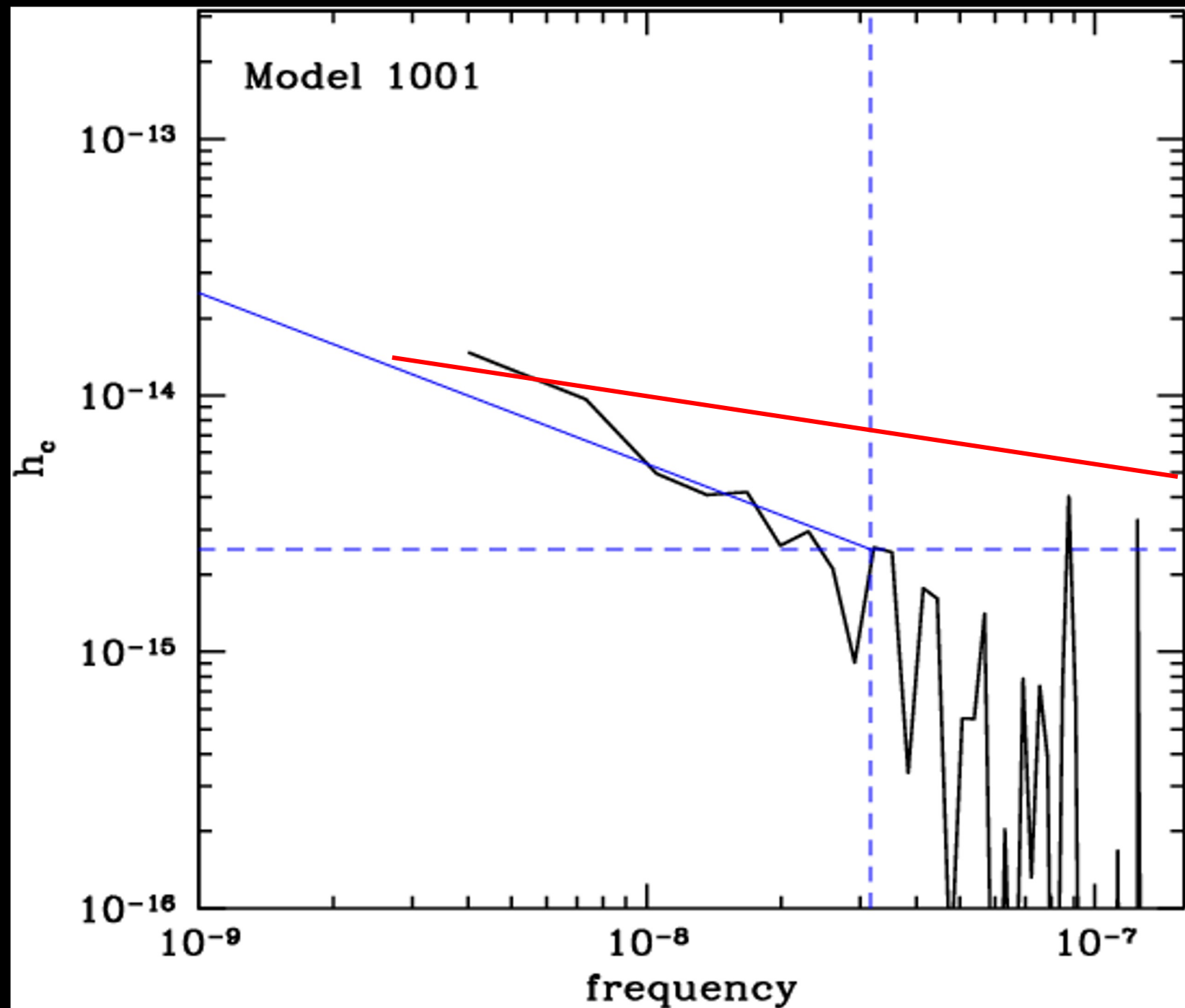


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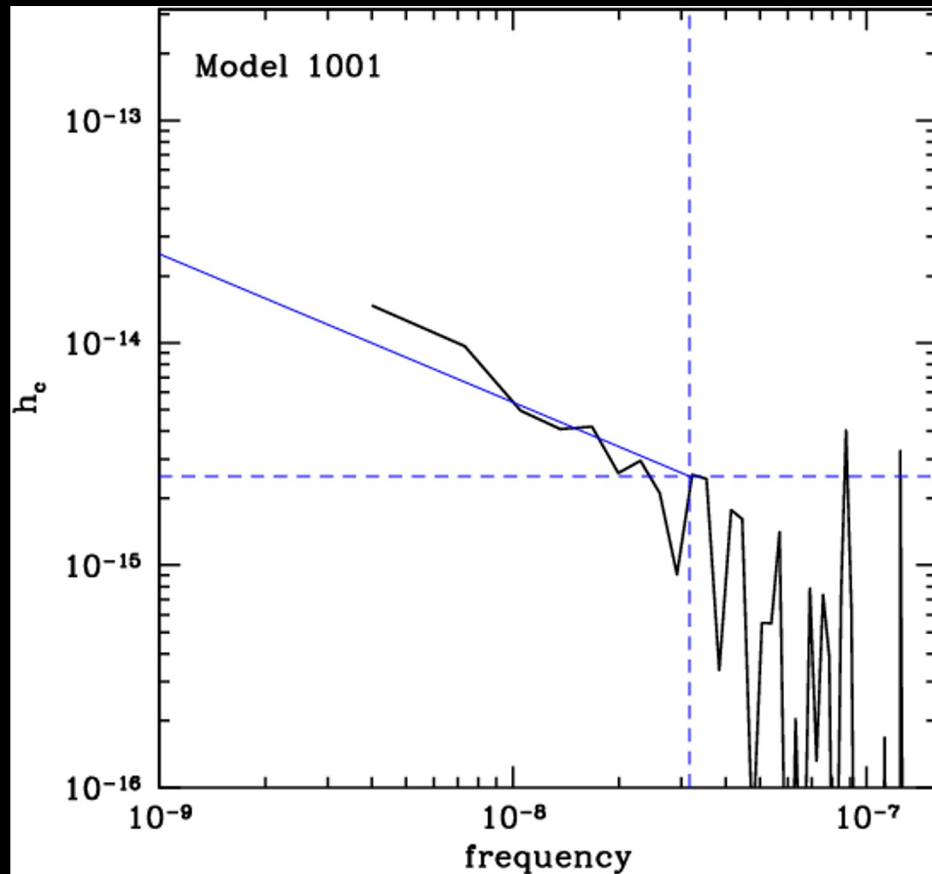
It might even be the dominant effect for flattening.

# *Variance of the signal*



me etc etc.

# Comparison with empirical models



Qualitative comparison with Rosado+15 n

-Merger rate determined observationally (S13) via galaxy mass function, pair fraction

-constrained by observations

-adding hardening via stars and eccentrici

324k MC realizations

-captures signal variance

-capture resolvable sources

$$h_c^2(f) = \int dM dq dz \frac{\partial^4 N}{\partial M \partial q \partial z \partial \ln f_p} h_s^2(f_p)$$

$$\frac{\partial^3 \eta_{\text{gal-gal}}}{\partial m_{\star 1} \partial q_{\star} \partial z} = \frac{\Psi(m_{\star 1}, z')}{m_{\star 1} \ln(10)} \frac{P(m_{\star 1}, q_{\star}, z')}{T_{\text{gal-gal}}(m_{\star 1}, q_{\star}, z')} \frac{\partial t}{\partial z'}$$

$$\Psi(m_{\star 1}, z) = \ln(10) \Psi_0 \cdot \left[ \frac{m_{\star 1}}{M_{\psi}} \right]^{\alpha_{\psi}} \exp\left(-\frac{m_{\star 1}}{M_{\psi}}\right)$$

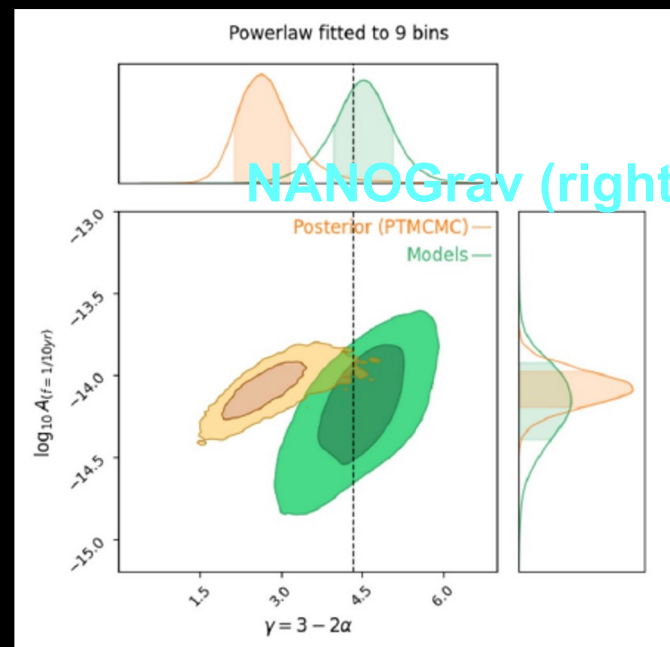
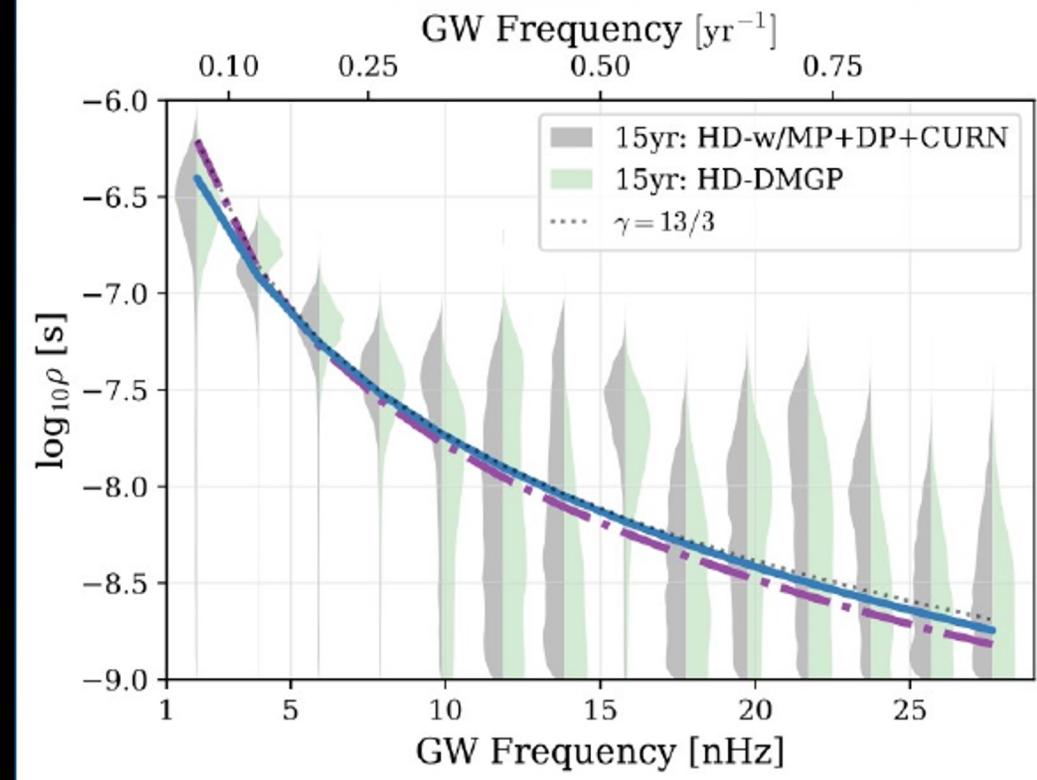
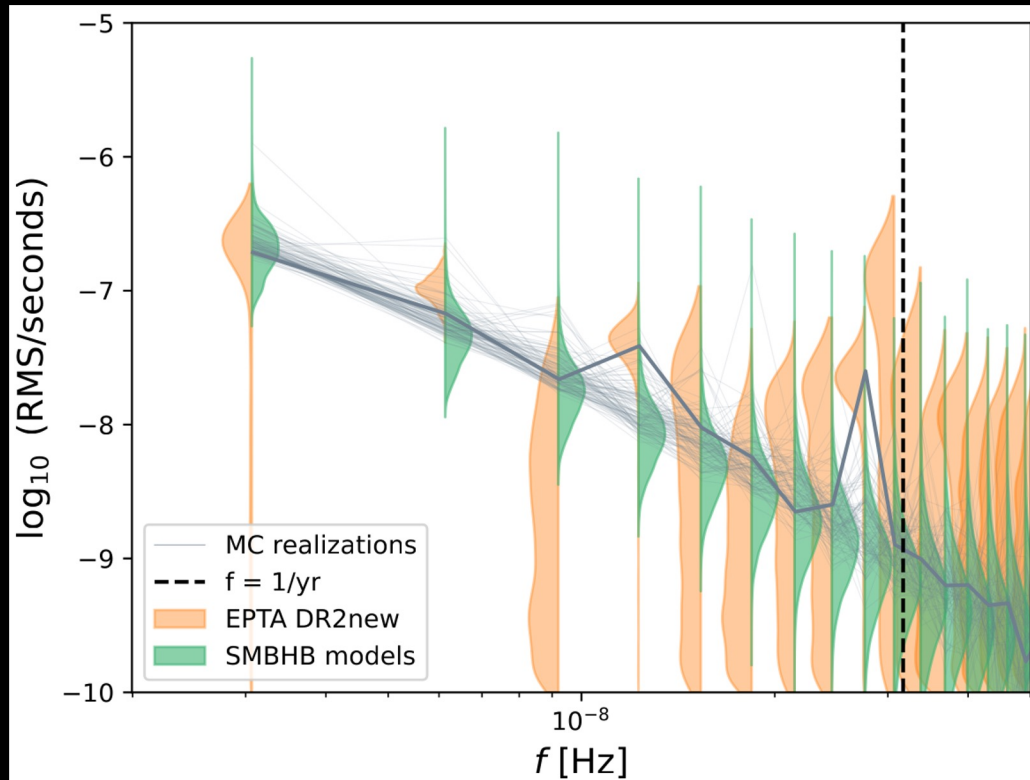
$$P(m_{\star 1}, q_{\star}, z') = P_0 \left( \frac{m_{\star 1}}{10^{11} M_{\odot}} \right)^{\alpha_p} (1+z)^{\beta_p} q^{\gamma_p}$$

$$T_{\text{gal-gal}}(m_{\star 1}, q_{\star}, z') = T_0 \left( \frac{m_{\star 1}}{10^{11} M_{\odot}/h} \right)^{\alpha_t} (1+z)^{\beta_t} q^{\gamma_t}$$

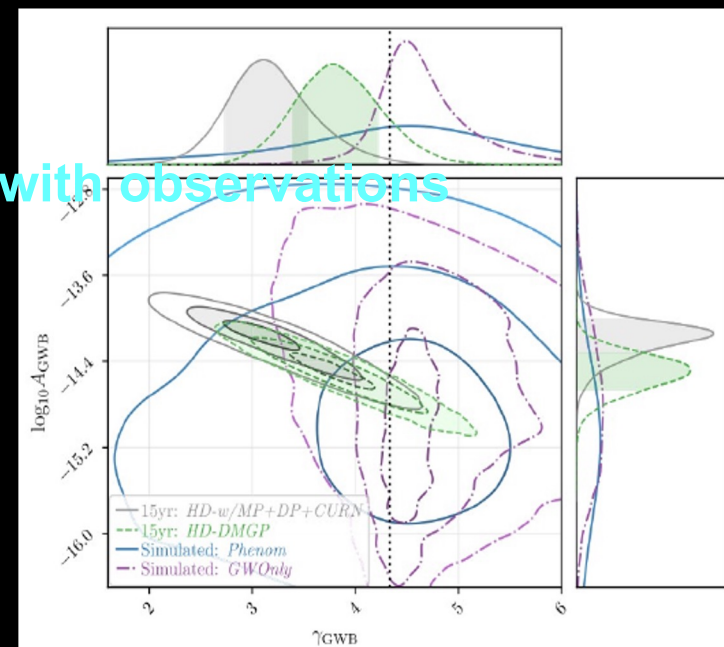
$$\log_{10}(M_{\text{BH}}/M_{\odot}) = \mu + \alpha_{\mu} \log_{10}\left(\frac{M_{\text{bulge}}}{10^{11} M_{\odot}}\right) + \mathcal{N}(0, \epsilon_{\mu})$$

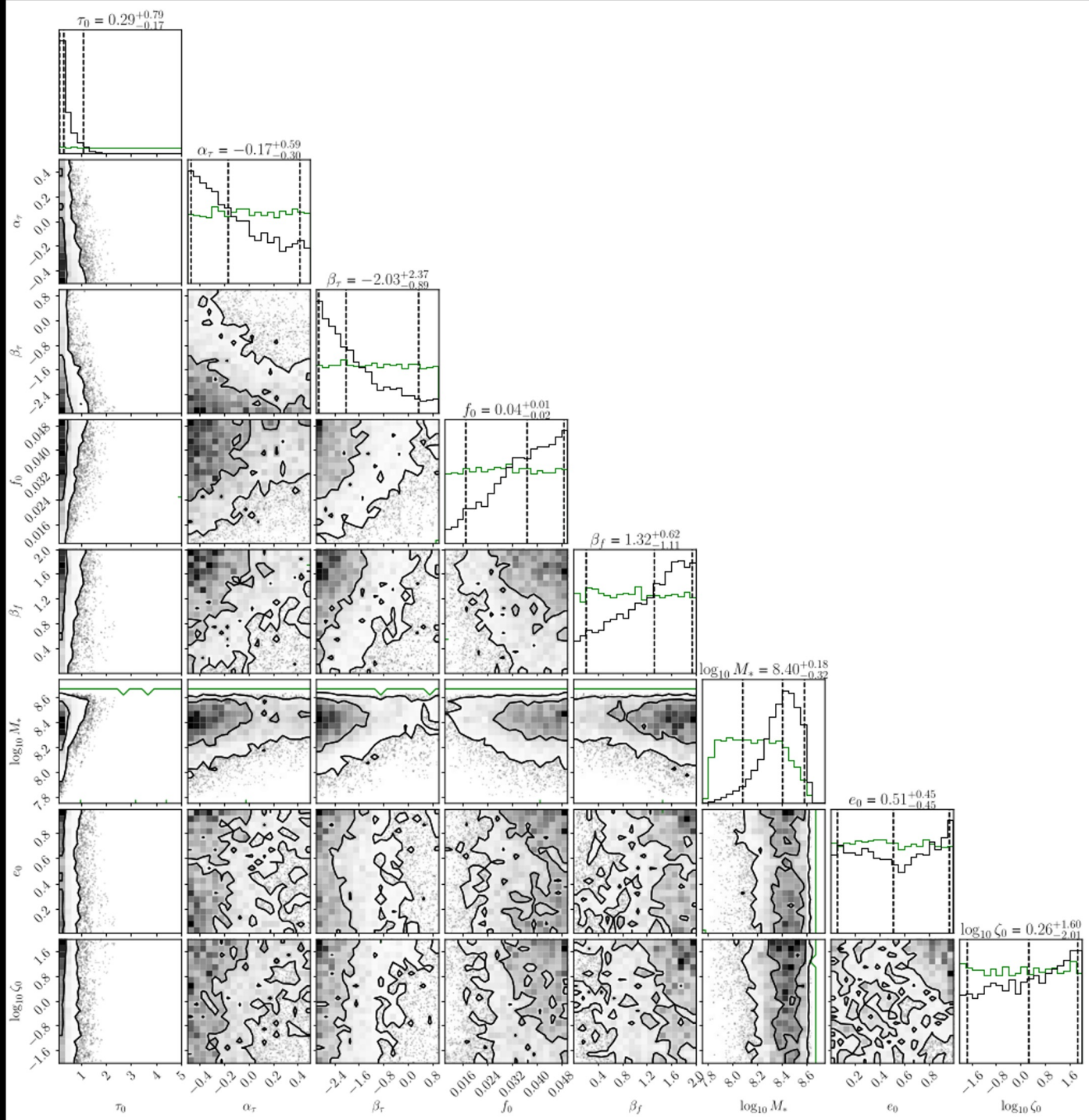


# Spectral comparison

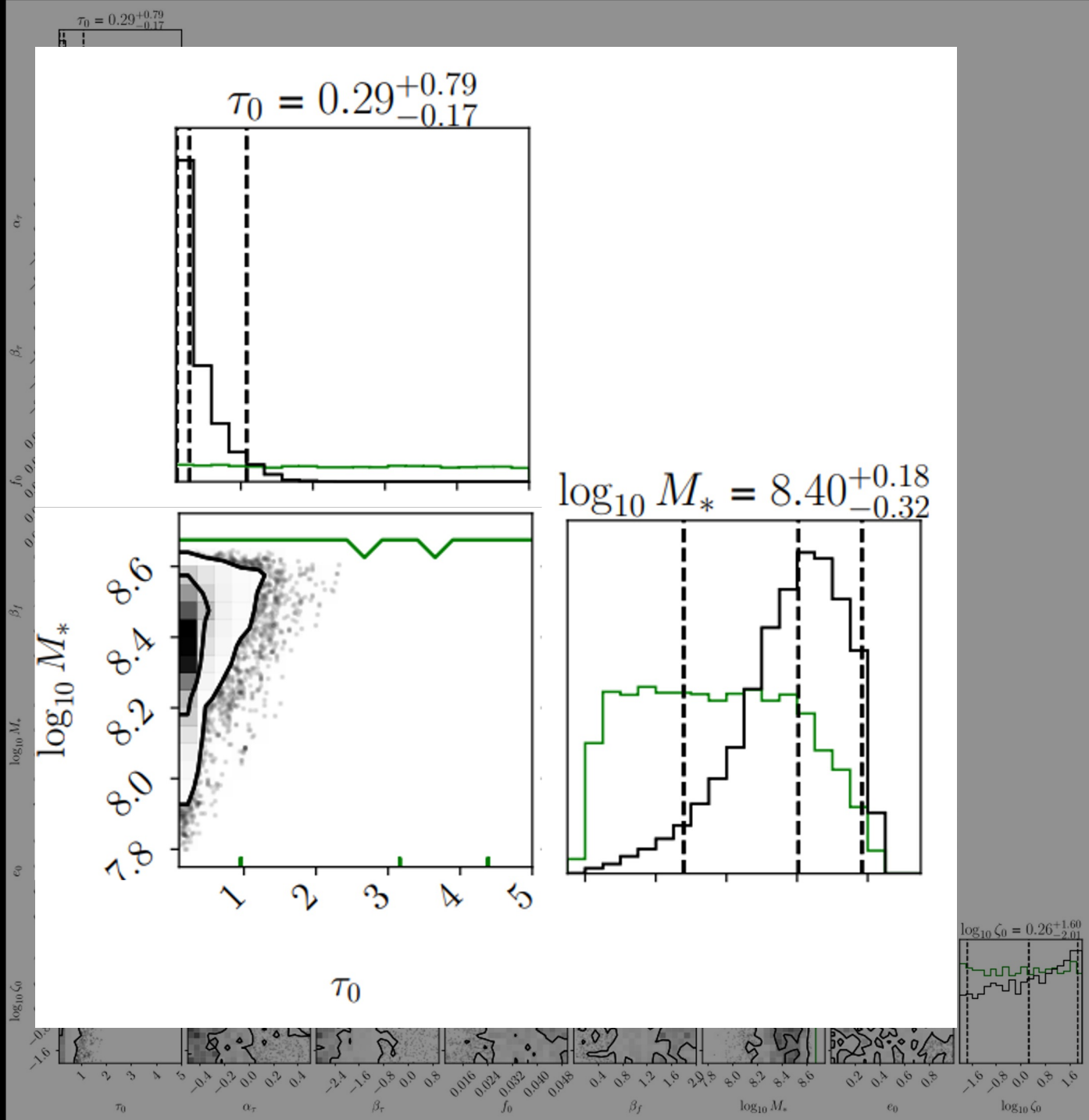


EPTA (left) and  
NANOGrav (right) results pretty compatible with observations  
(Agazie+23, Antoniadis+24)





- Astro constrained models (Chen et al. 2019)**
- generalization of **R**
  - informed by observations:
  - Galaxy mass function
  - Galaxy pair fraction
  - SMBHB merger timescale
  - SMBH-galaxy relation
  - eccentricity and environment



**Astro constrained models (Chen et al. 2019)**

- generalization of  $\Lambda$ CDM
- informed by observations:

- Galaxy mass function

- Galaxy pair fraction

- SMBHB merger timescale

- SMBH-galaxy relation

- eccentricity and environment

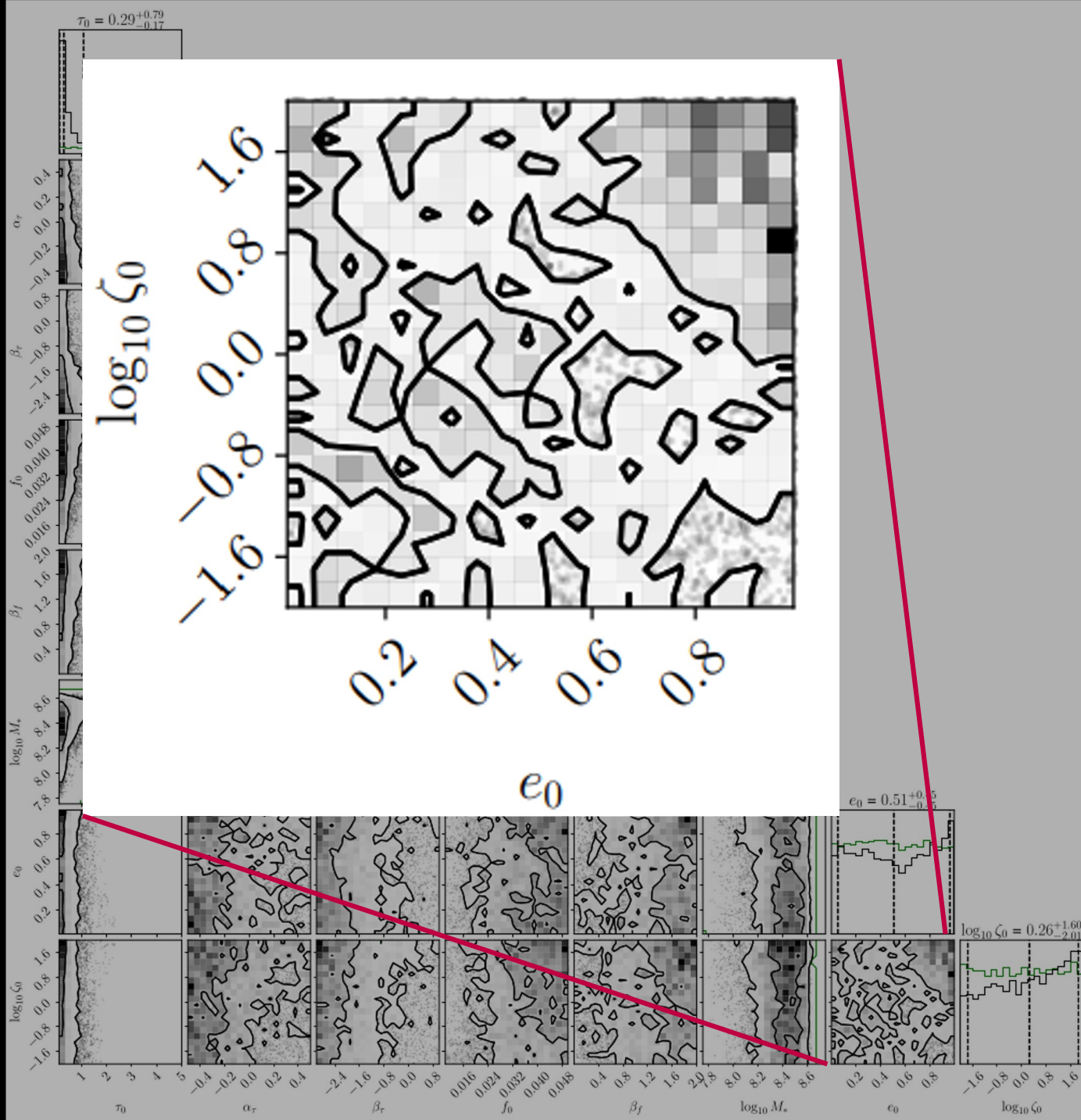
**Best constrains:**

- SMBHB time to merger

- SMBH –  $M_*$  relation

**SMBHB are massive and merge frequently**





**Astro constrained models (Chen et al. 2019)**

- generalization of  $\Lambda$ CDM
- informed by observations:

- Galaxy mass function
- Galaxy pair fraction
- SMBHB merger timescale
- SMBH-galaxy relation
- eccentricity and environment

**Best constrains:**

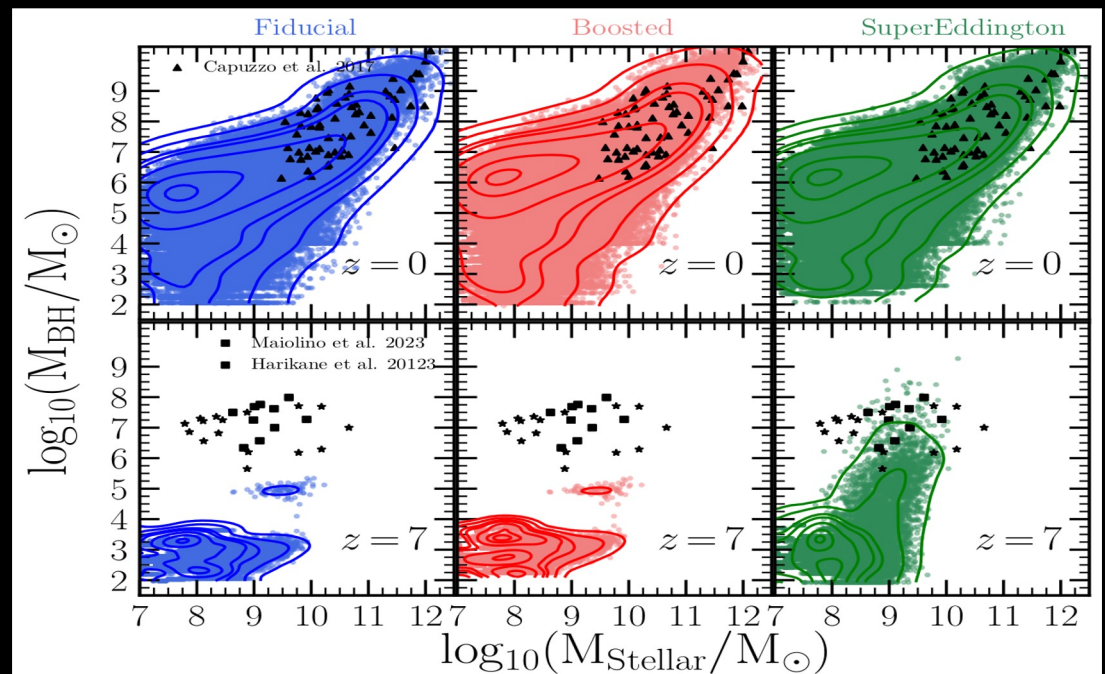
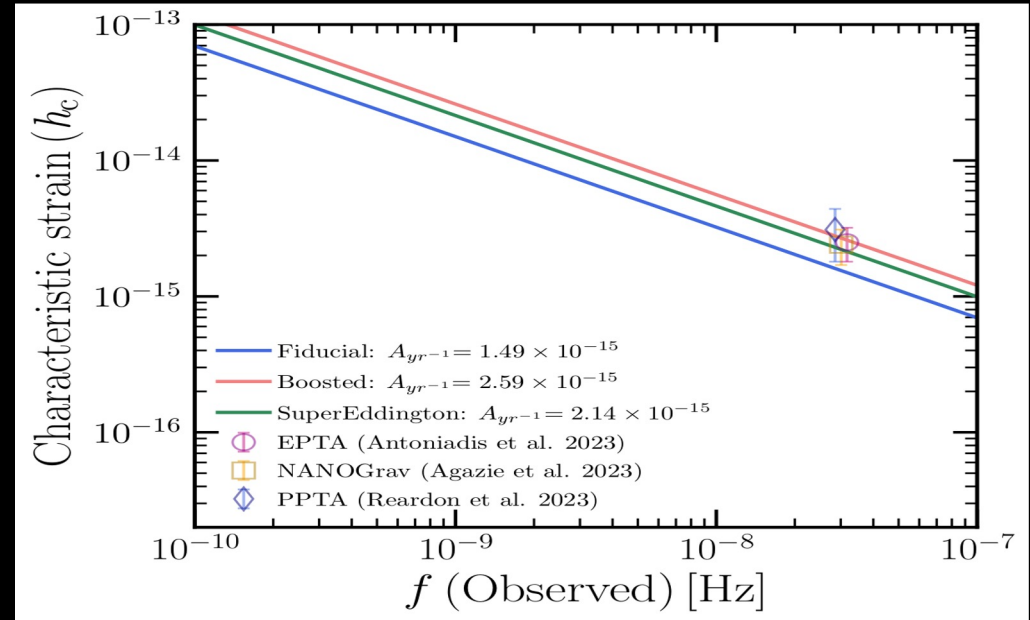
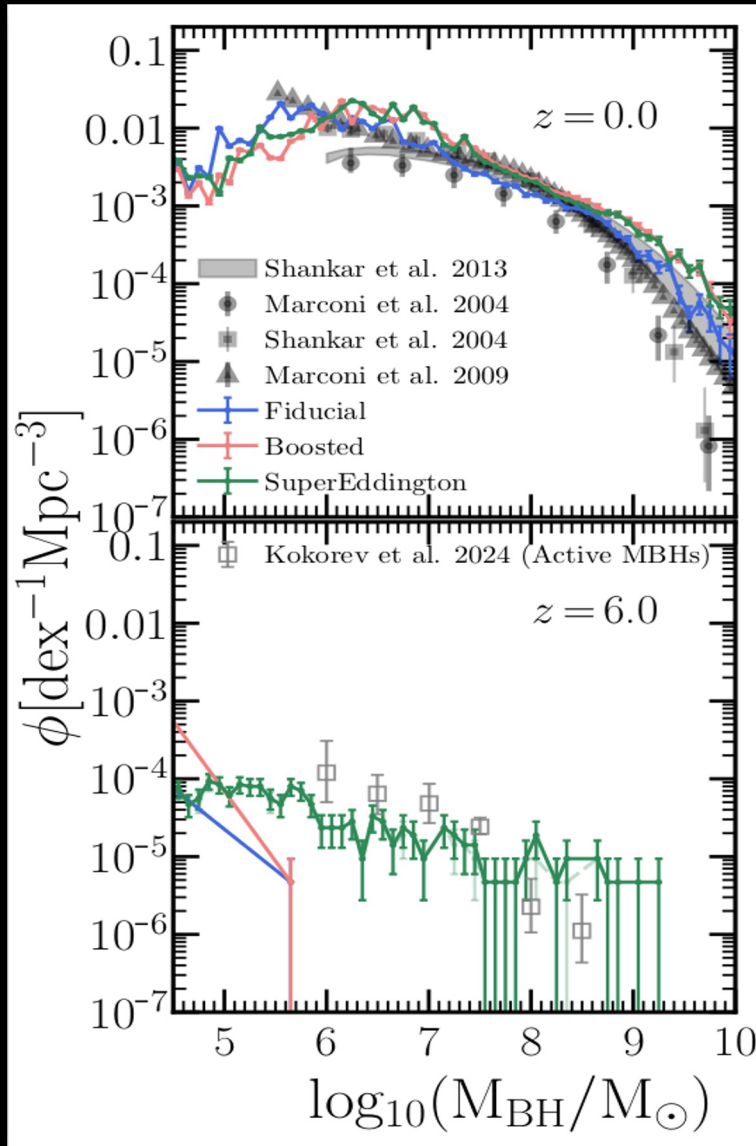
- SMBHB time to merger
- SMBH –  $M_*$  relation
- Slight preference for eccentric

**SMBHB are massive and merge frequently**

# Accommodating low and high $z$ constraints



Adding a short phase of supereddington accretion in the most



# Constraining the local MBH mass function

(Phinney 2001, Sato Polito+23,24, Liepold & Ma24)

$$h_c^2(f) = \frac{4G}{\pi f^2} \langle (1+z)^{-1/3} \rangle \int dM_{\text{BH}} \phi(M_{\text{BH}}) M_{\text{BH}} \langle \epsilon \rangle (M_{\text{BH}})$$

-MBH buildup merger driven

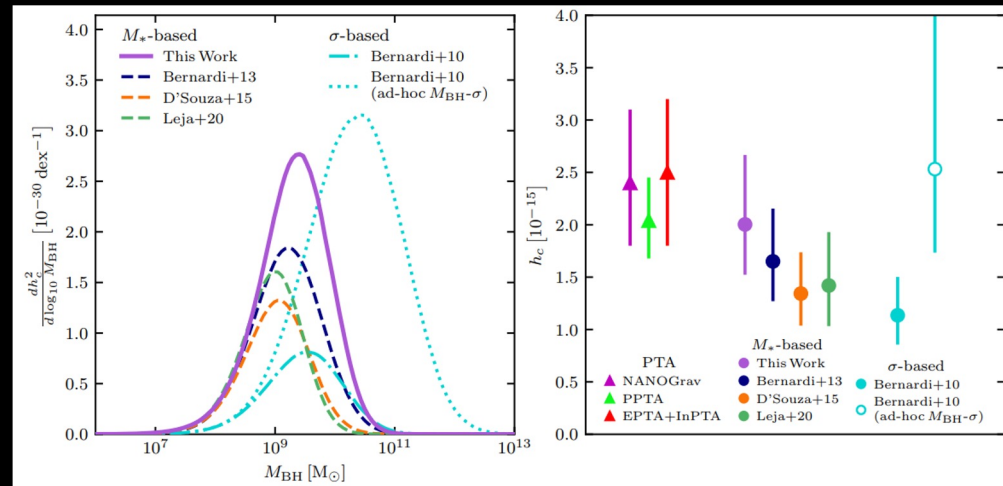
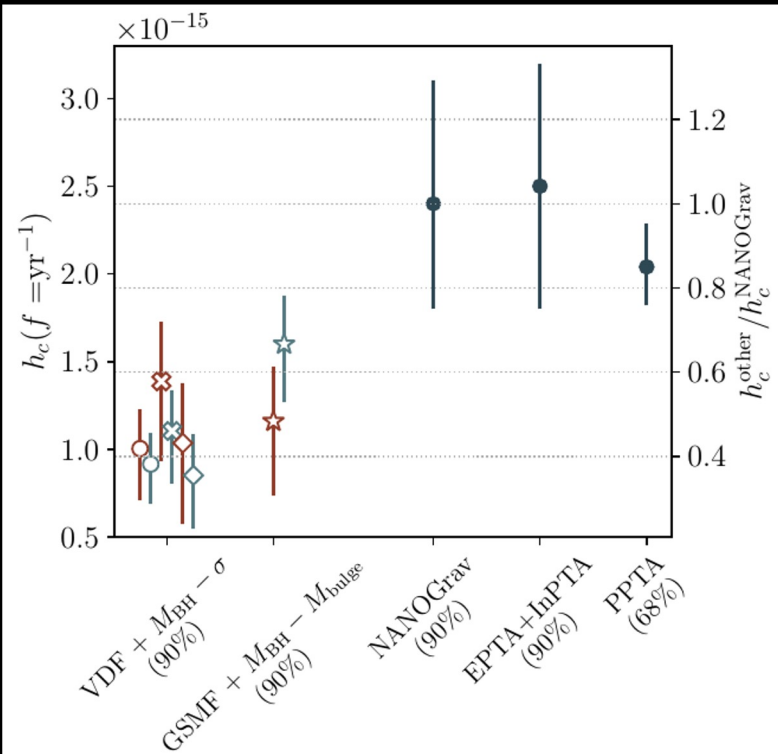
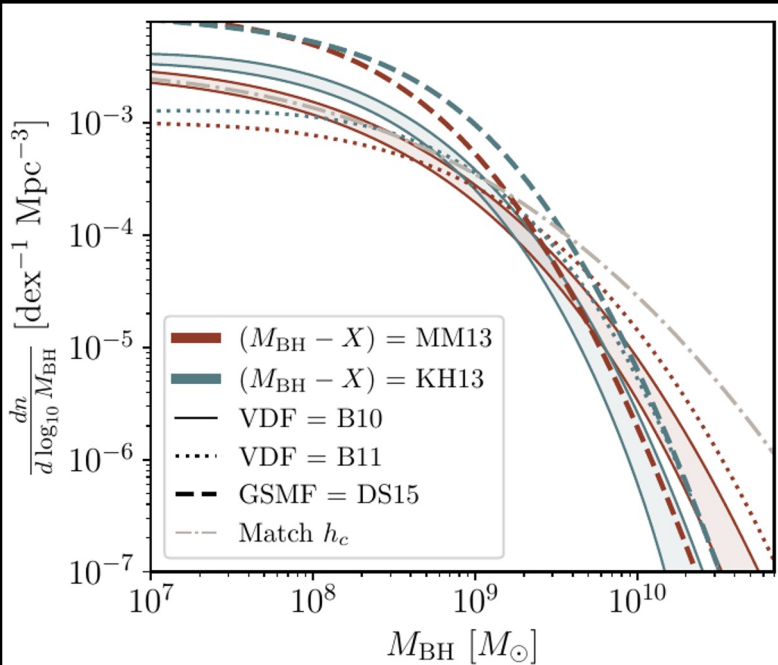
-GWB mostly determined by the local mass function

~2 discrepancy ( $2\sigma$ ):

-mild dependence on redshift and efficiency

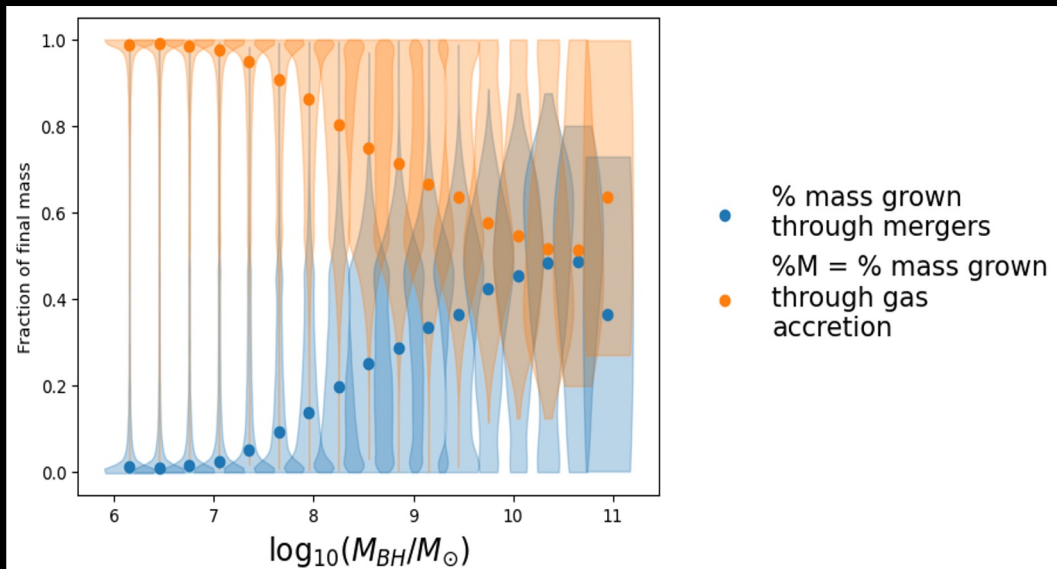
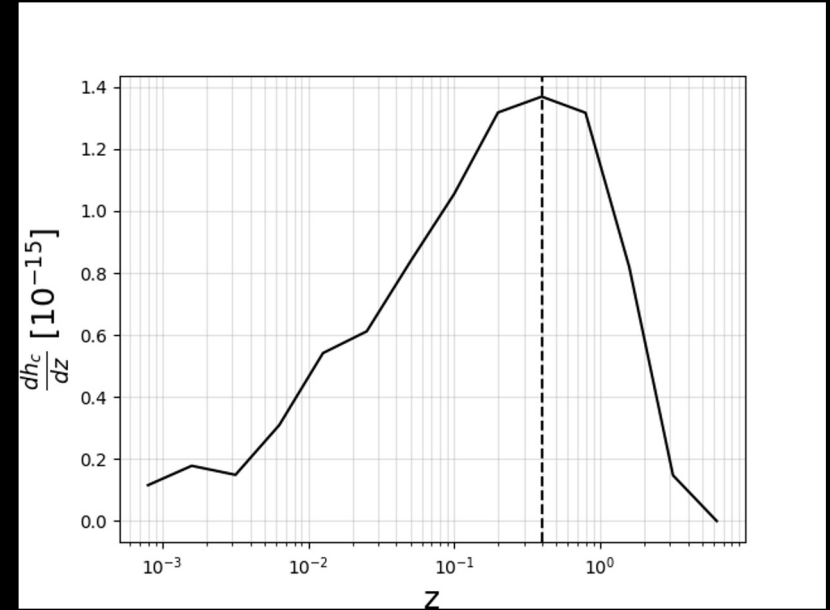
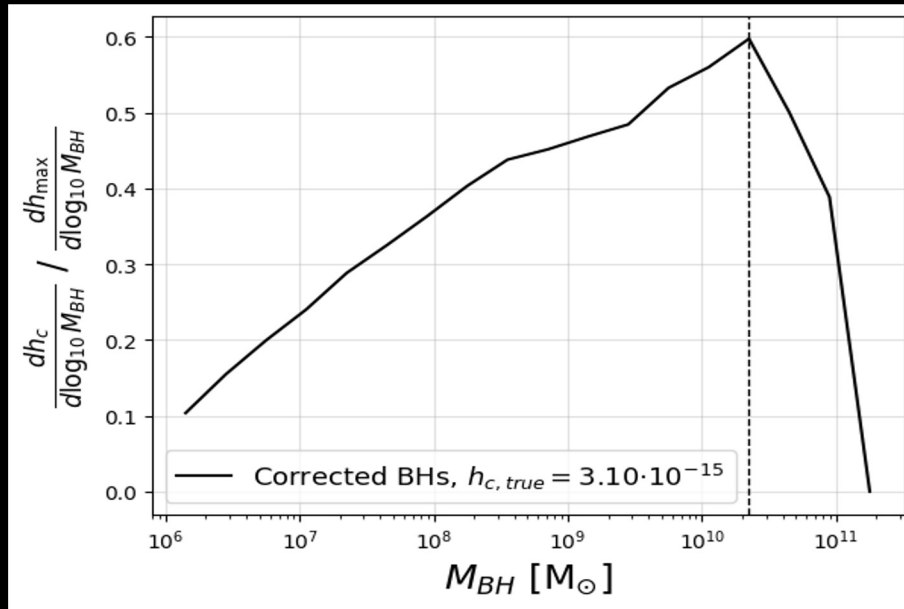
-effect of multiple mergers

PTA can determine the local mass MBH function?



Discrepancy can be accommodated within the uncertainty

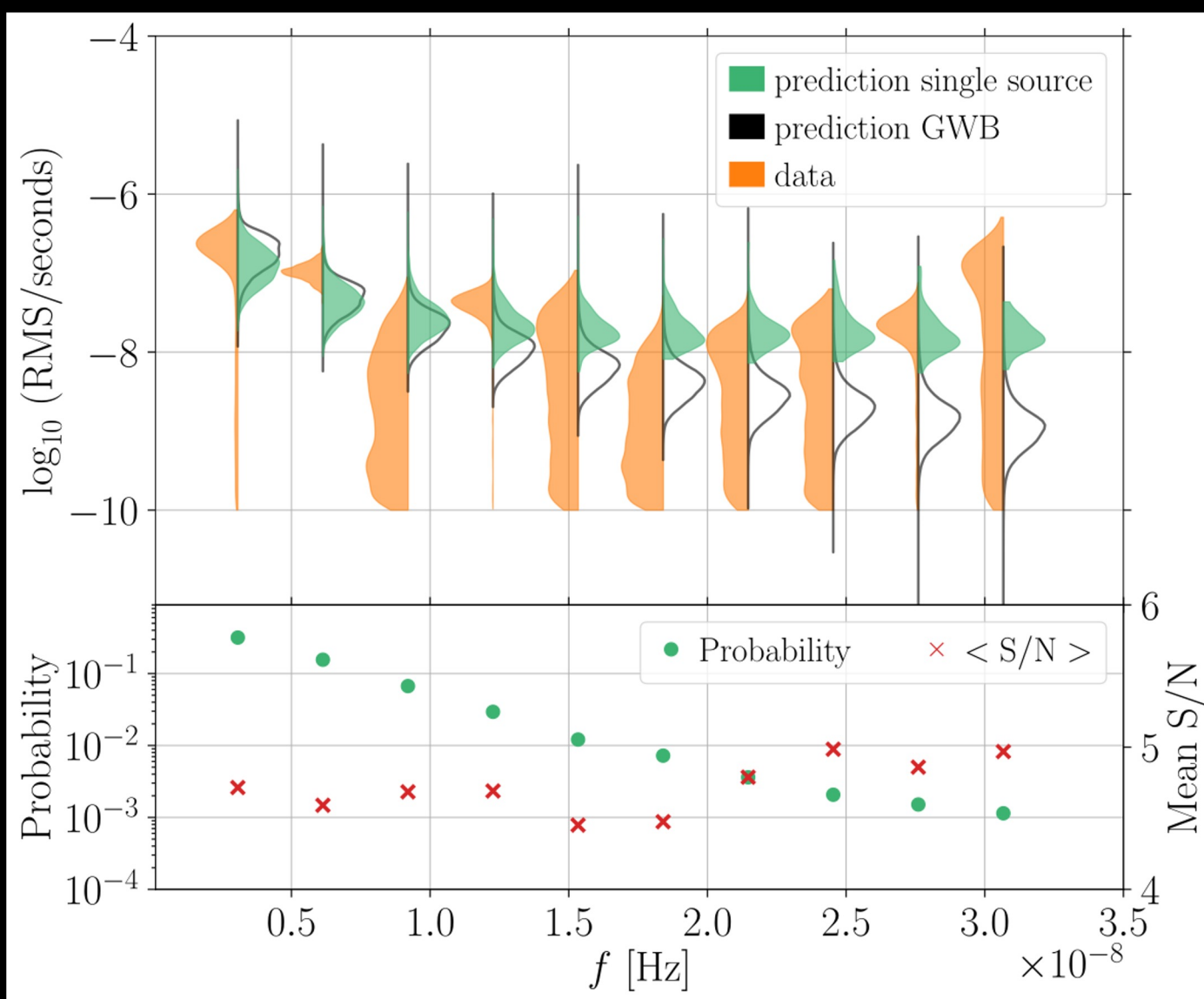
# The build-up of the GW signal



## The GWB from L-Galaxies (Ferranti+ in prep.)

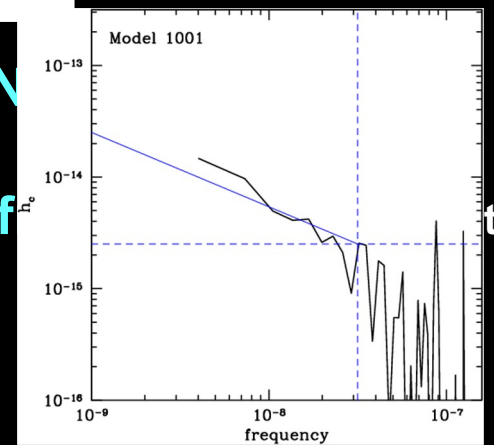
- The highest contribution to the GWB comes from low redshift
- MBHs at low  $z$  grow mostly by mergers
- 95% of the GWB comes from  $z < 1$





Models allow to compute CGW detection statistics (circular, SN)

~50% probability to have at least a CGW (mostly at the lowest f)



# *The future*



**MeerKAT, South Africa**

# *The future*



**FAST, China**

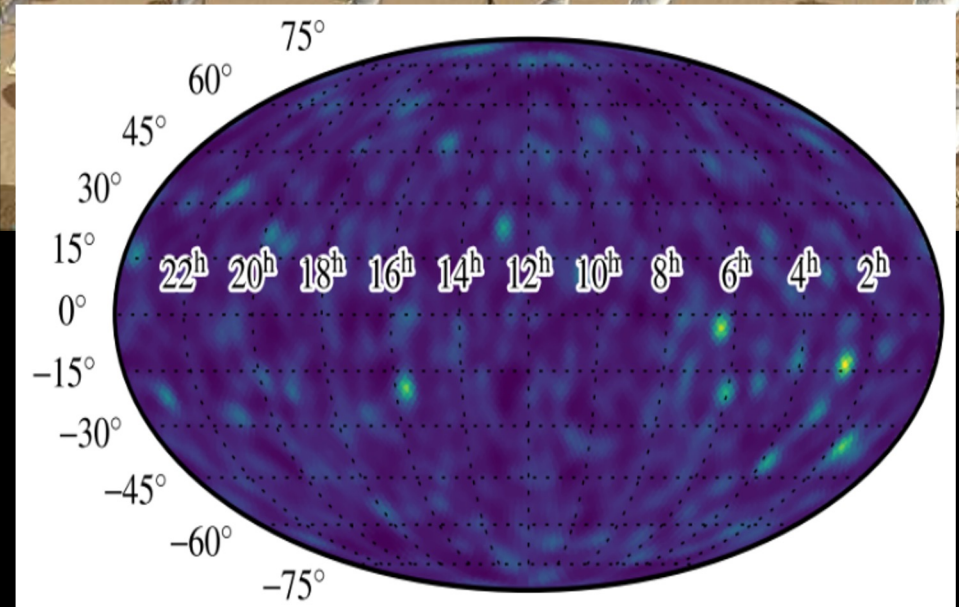
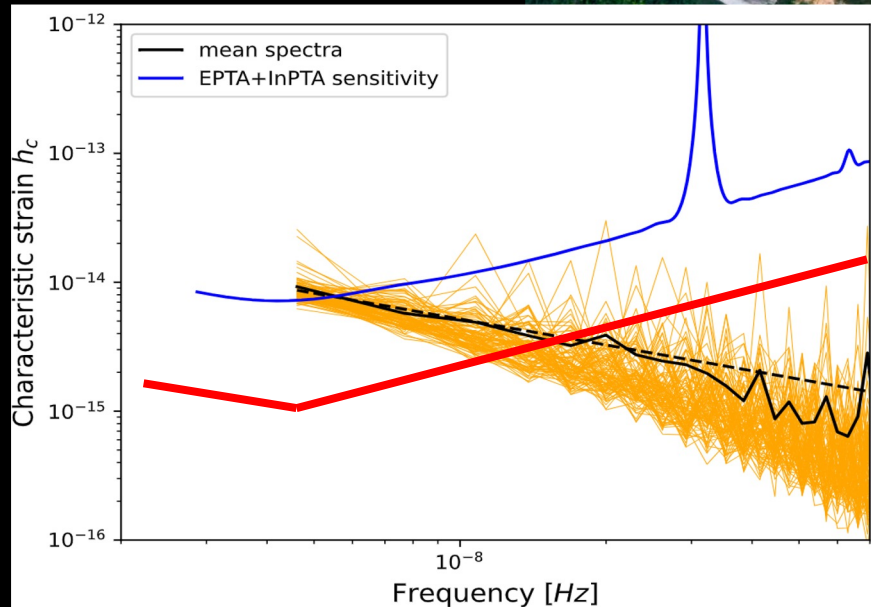
# *The future*



**Square Kilometre Array (SKA)**



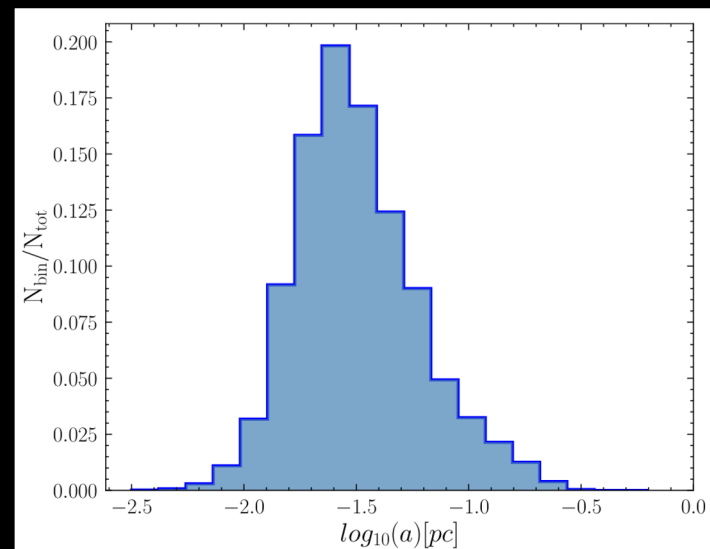
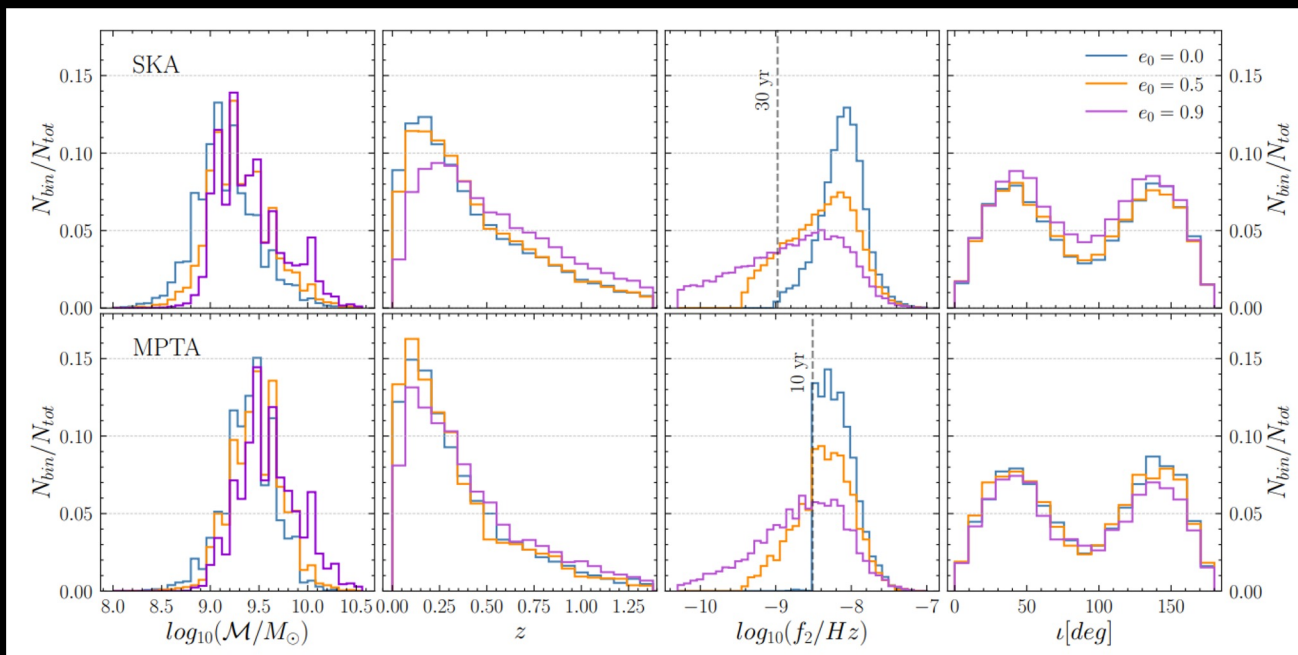
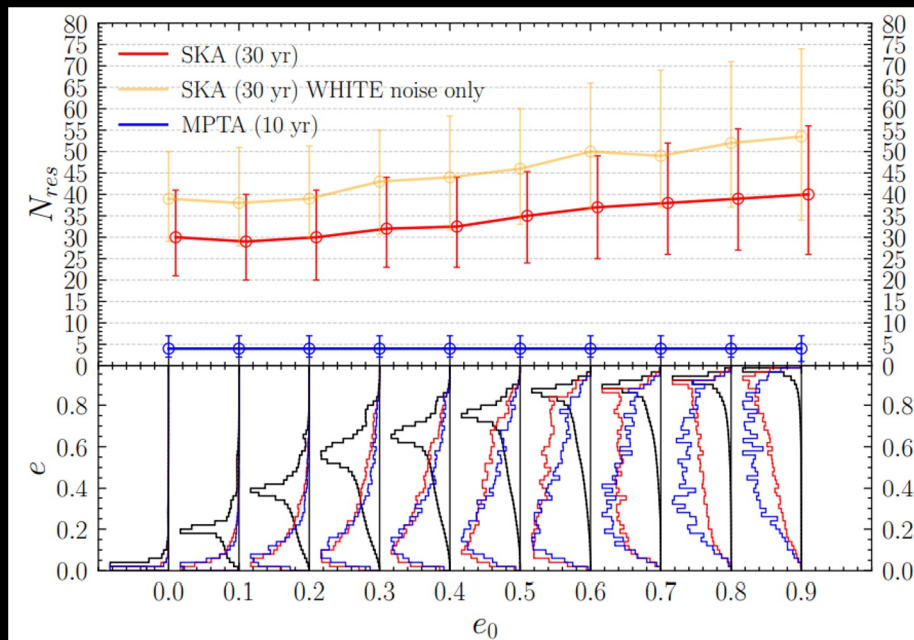
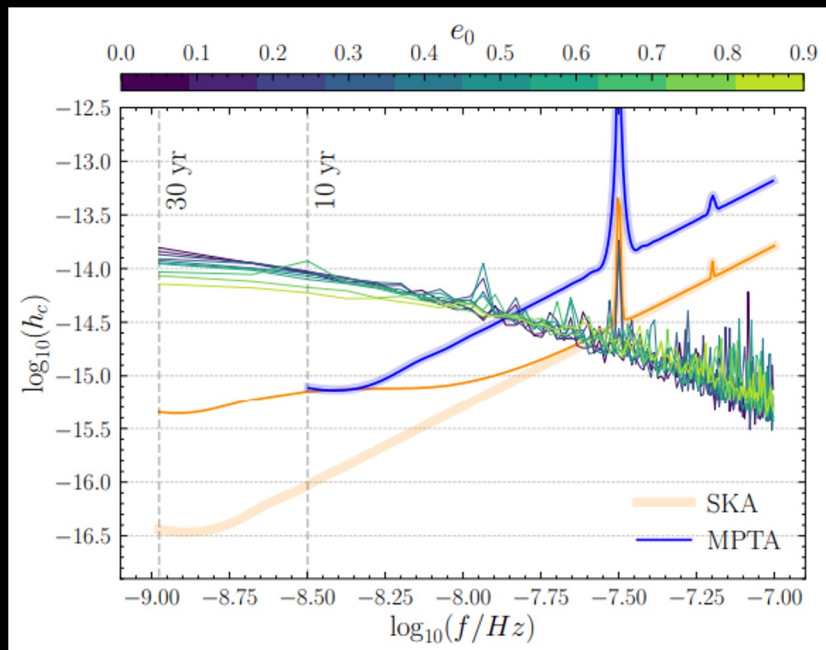
# The future



-x10 sensitivity in the next 20 yrs

-sky mapping the SMBH-z GW sky -tens of  
 → -AGN and accretion physics  
 -nHz multimessenger astronomy

# Resolvable sources?

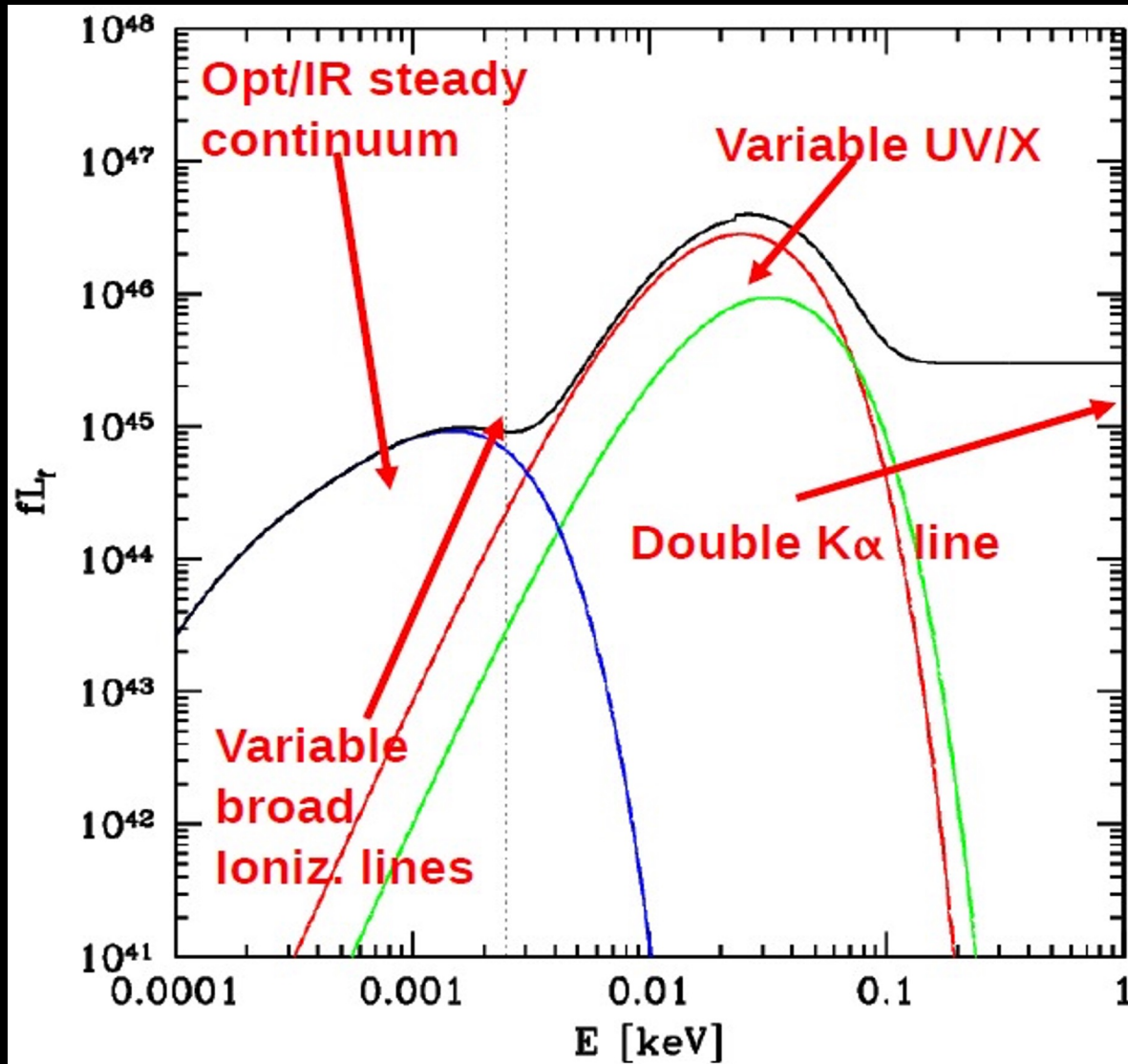


With 30 years of SKA we might id



# Associated electromagnetic signatures PTA

## MBH binary + circumbinary disk



## A variety of possibilities:

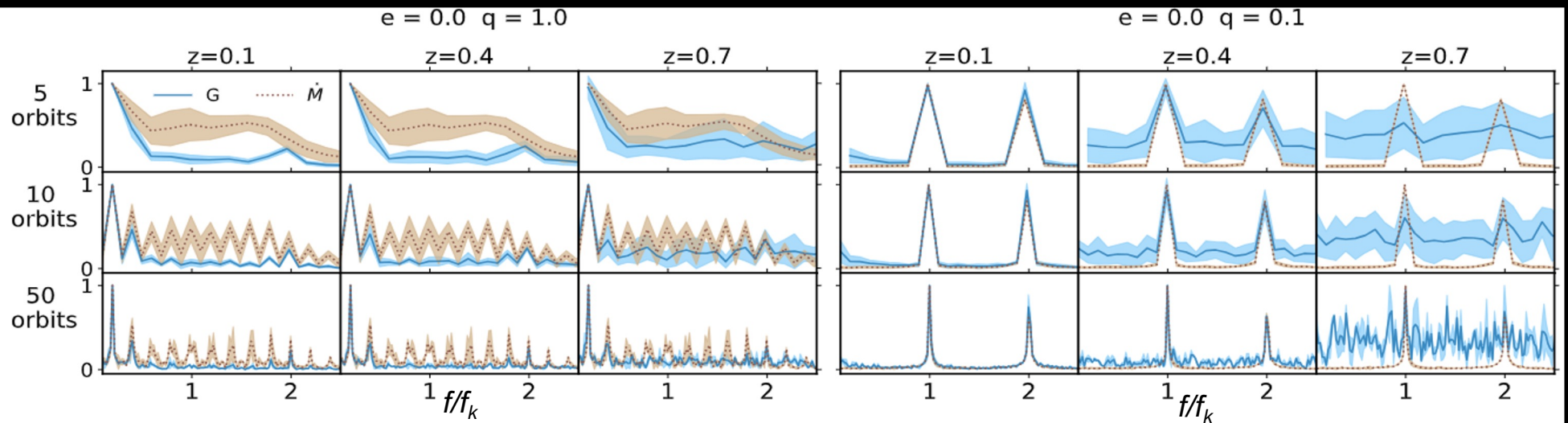
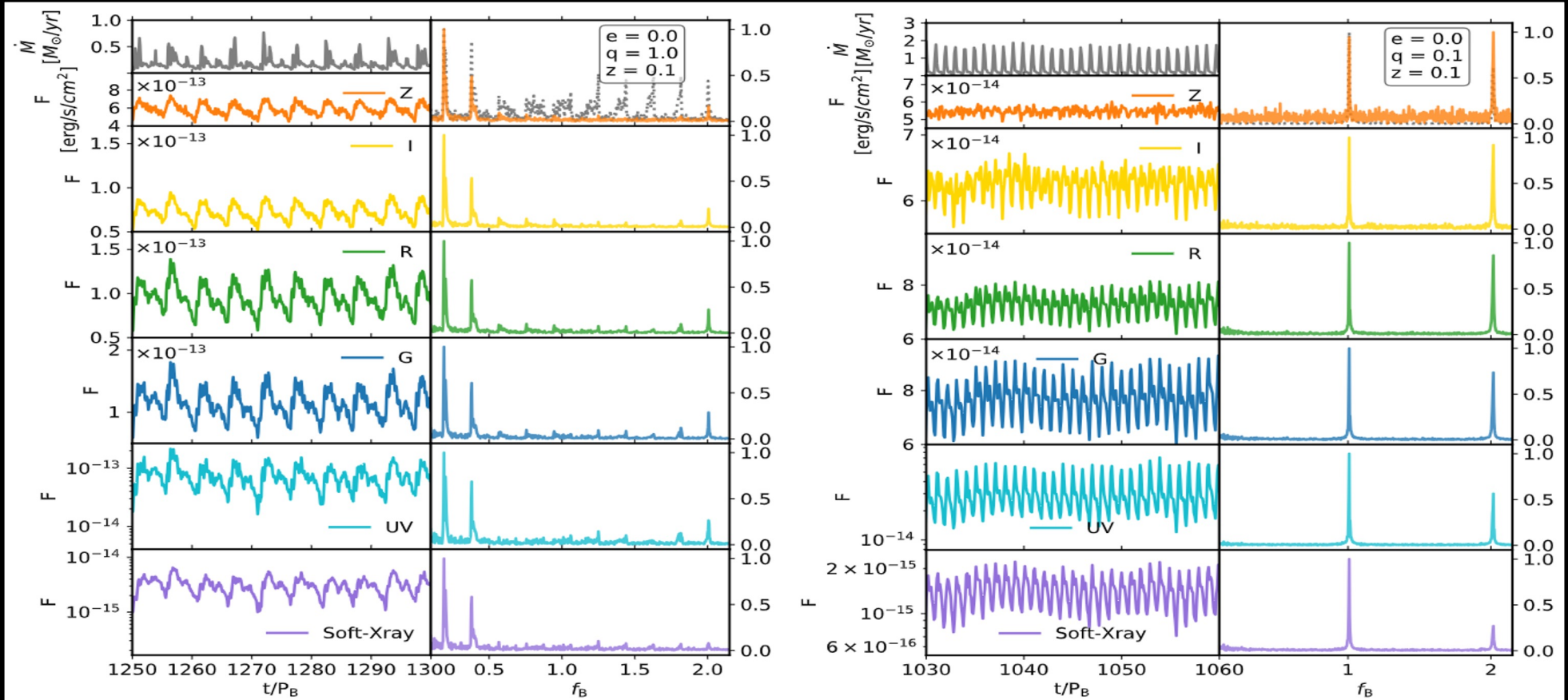
- Optical/IR dominated by the
- UV generated by inner stream
- X rays variable from periodic
- Variable broad emission line
- Double fluorescence lines?

et al. 2011, AS et al. 2012, Tanaka et al. 2012, Burke-Spolaor 2013,  
Farris+, D'Orazio+, Haiman+, Tang+,...)

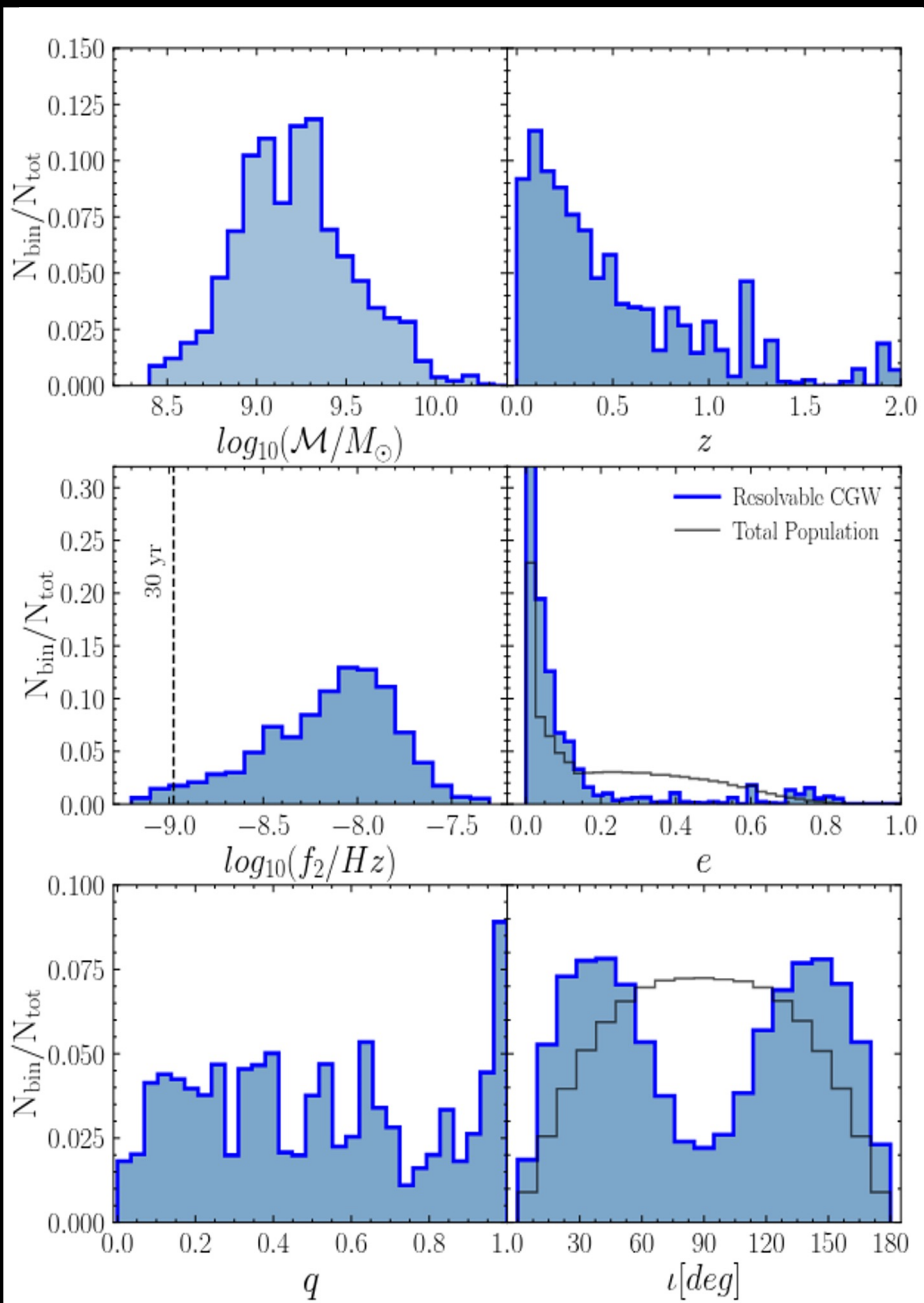




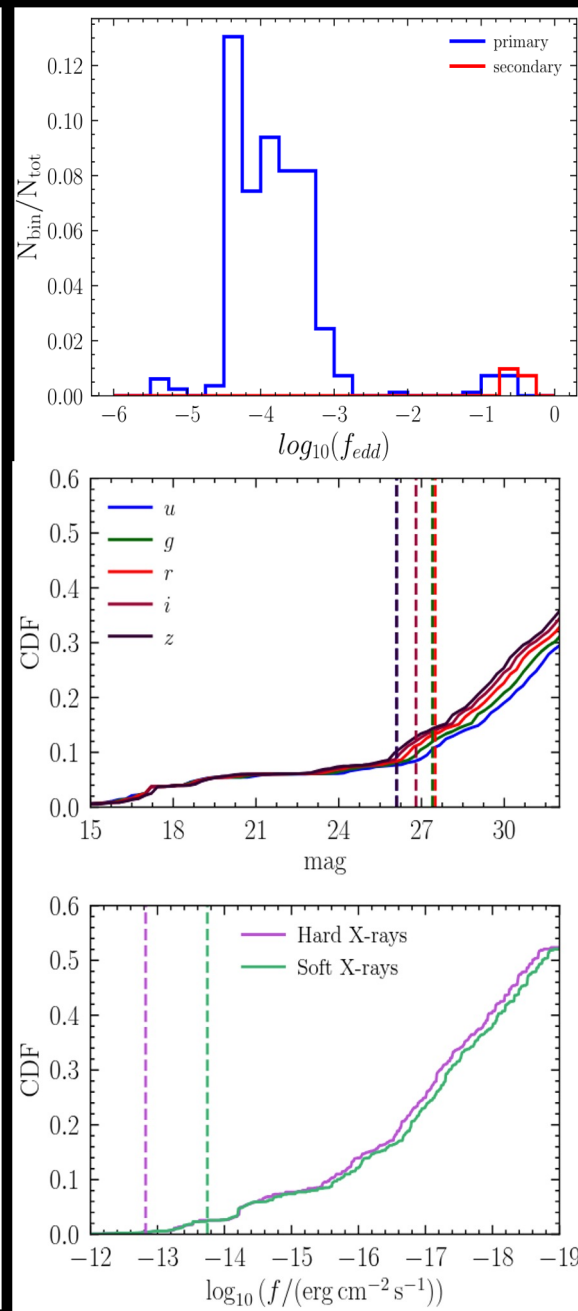
# Associated electromagnetic signatures PTA



# Properties of resolvable binaries



(Truant+25)



Pilot study with 10yr MeerKA

Universes simulated with *L Galaxies BH* (izquierdo villa)

~5 individually resolvable sources

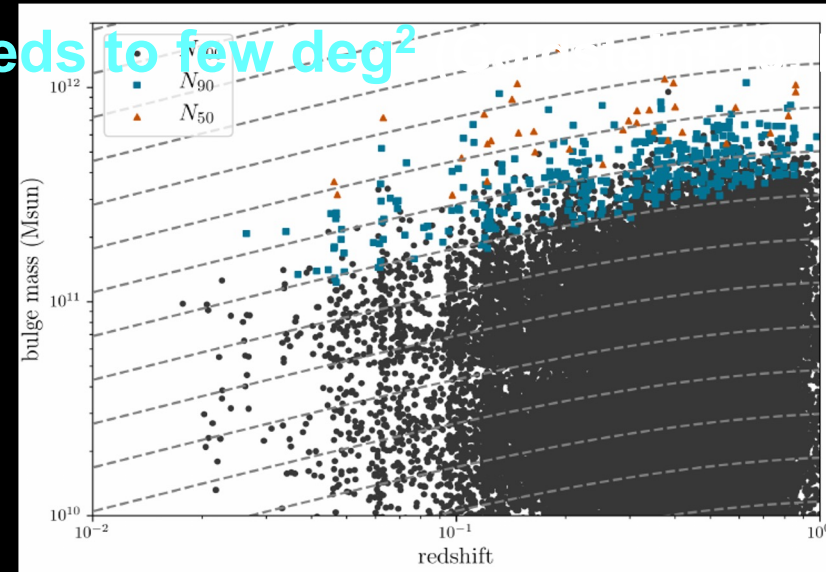
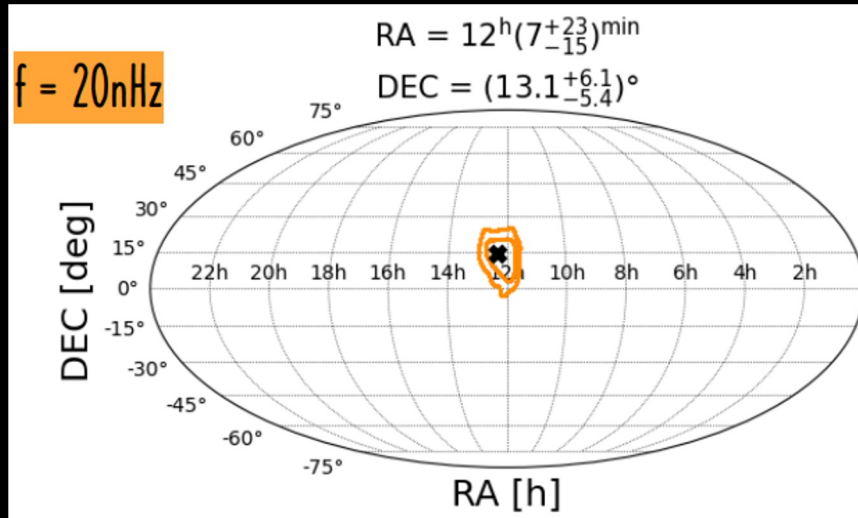
only ~2% of the systems are

Most of them have low Eddington

only 10% of the systems are

# MM opportunities: finding the right galaxy

PTA sky localization is from hundreds to few deg<sup>2</sup>



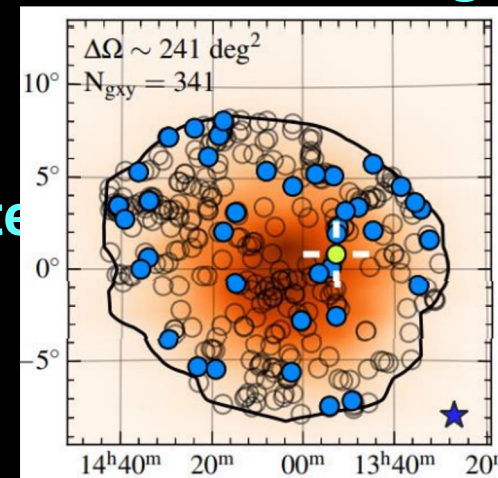
Ferranti+20

An individual PTA source must be mass

In general, PTA cannot break the distance-mass degeneracy ( $A \sim M^{5/3}/D$ )

$$A = 4 \frac{(G \mathcal{M}_z)^{5/3} (\pi f)^{2/3}}{D_1}$$

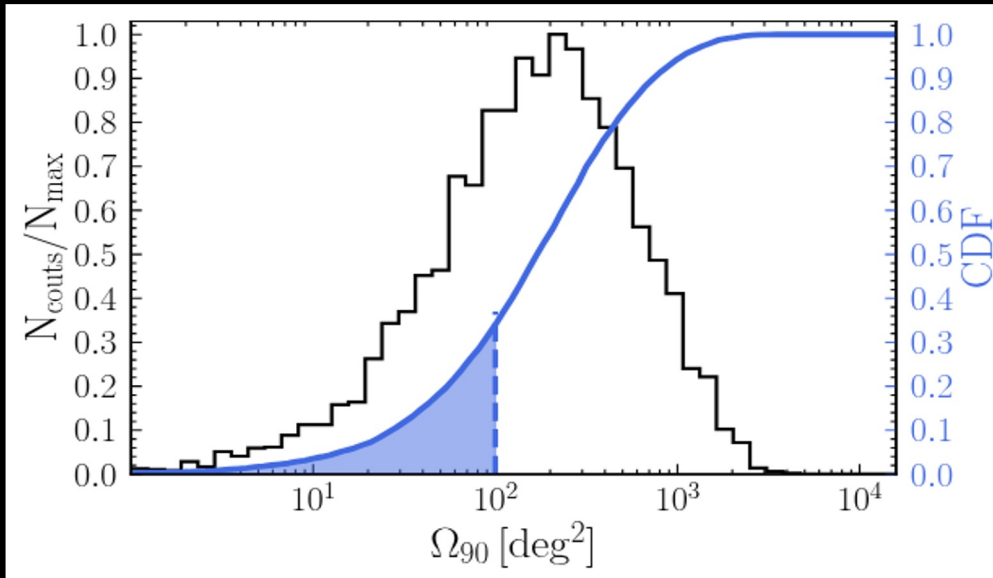
ns of deg<sup>2</sup> so te



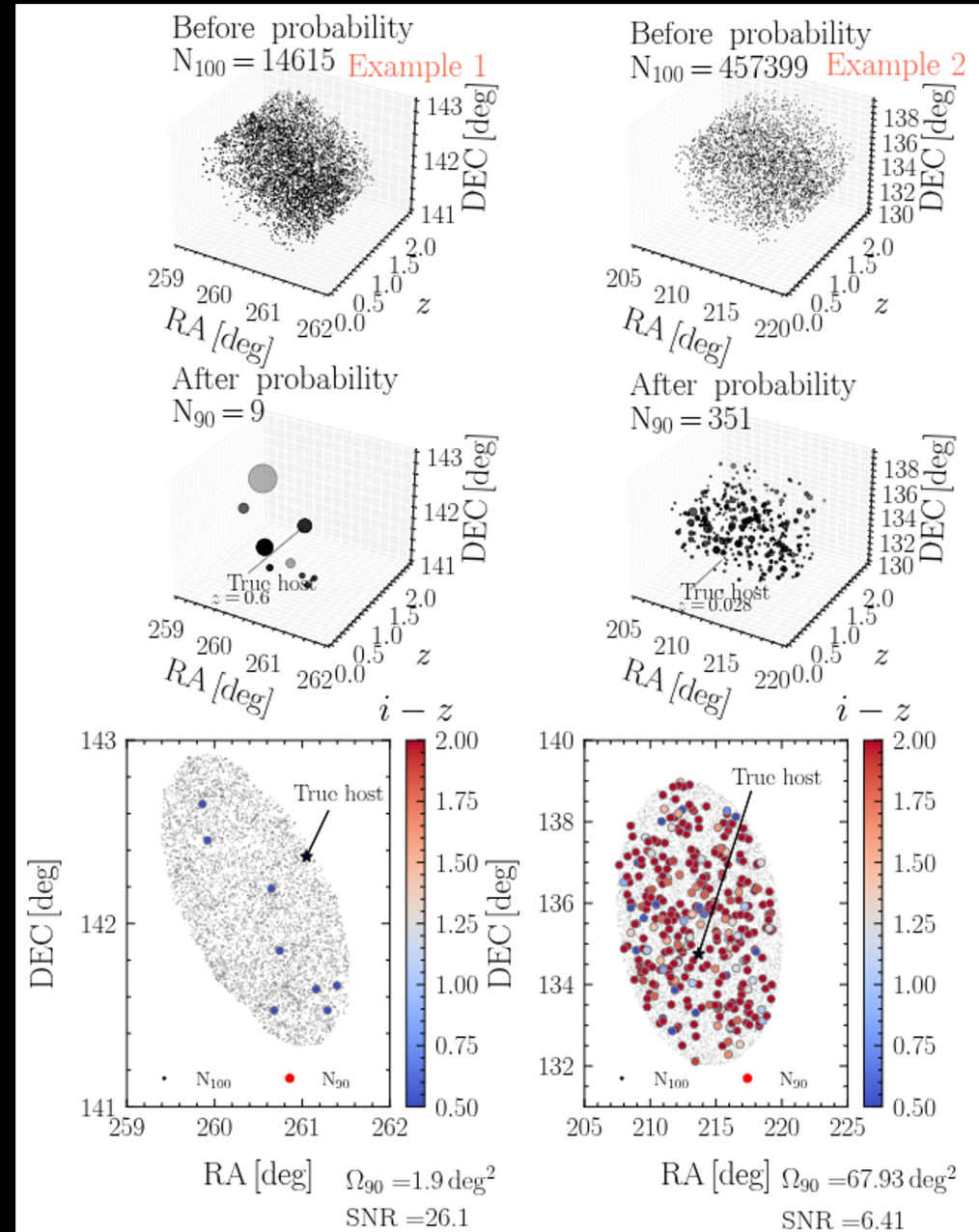
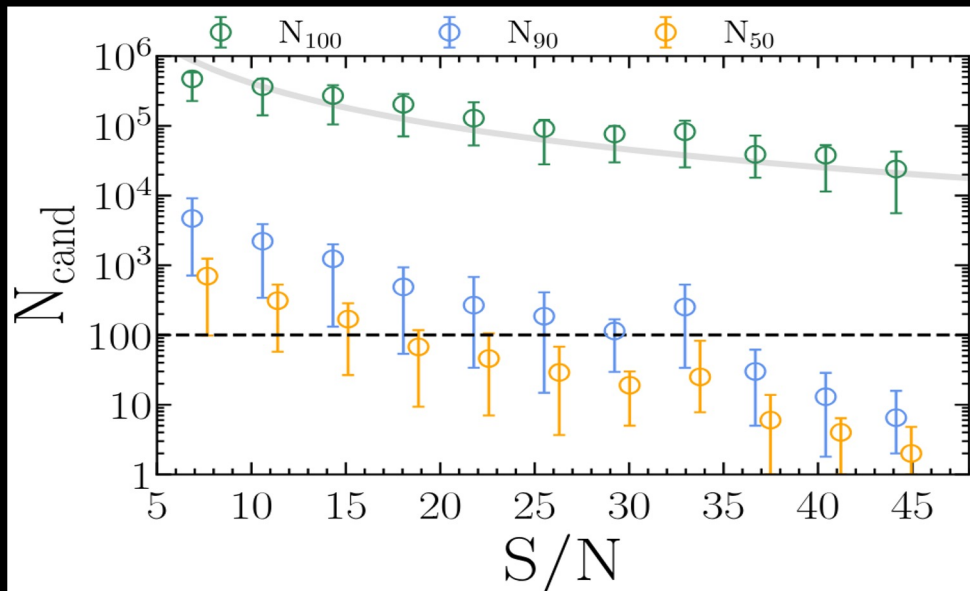
Only a handful of the  
of potential host gala



# MM opportunities: finding the right galaxy



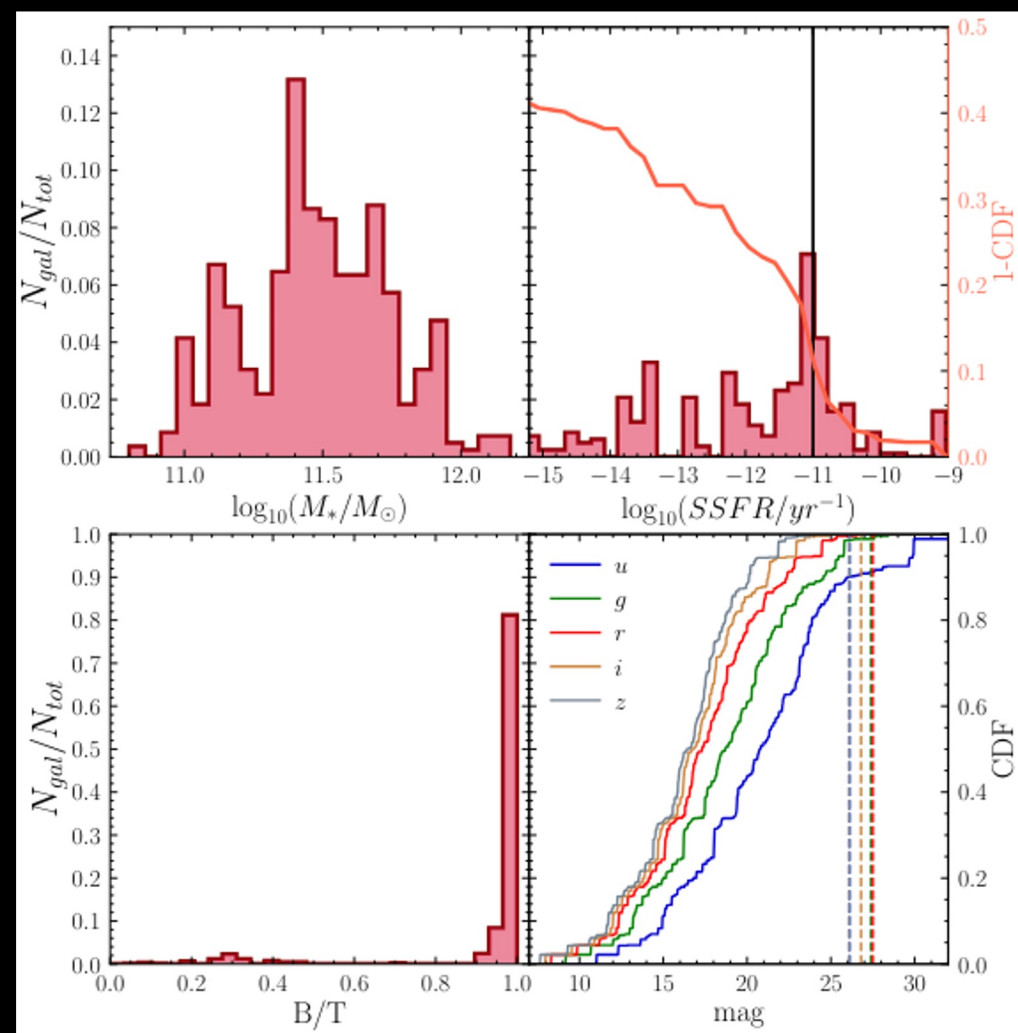
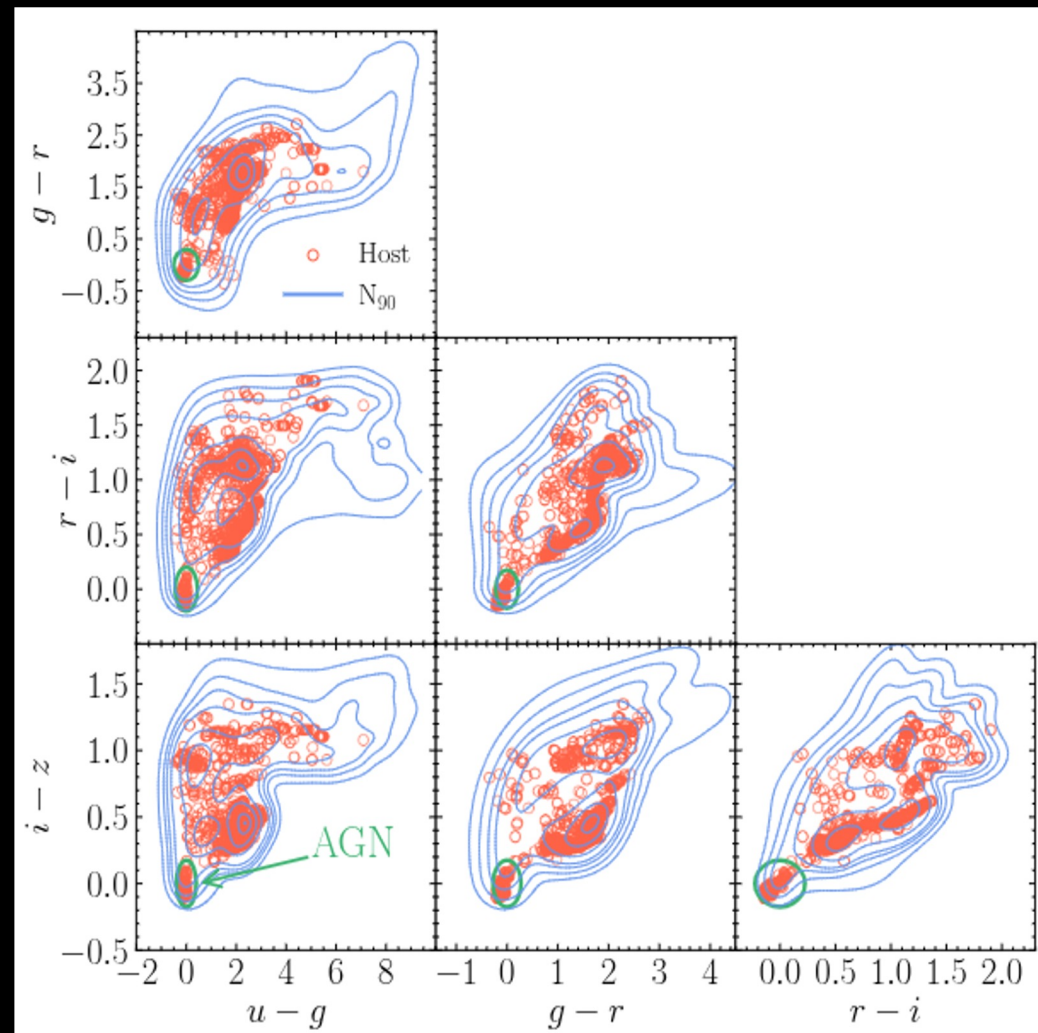
Sky localization sucks



Effective selection of host candidates



# MM opportunities: finding the right galaxy

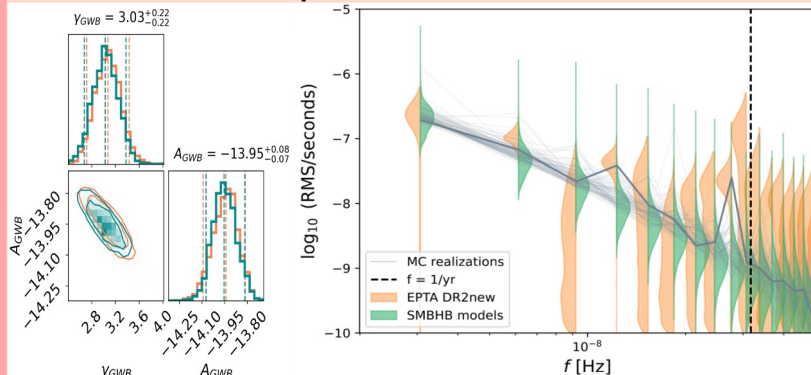


Host galaxies are regular ellipticals

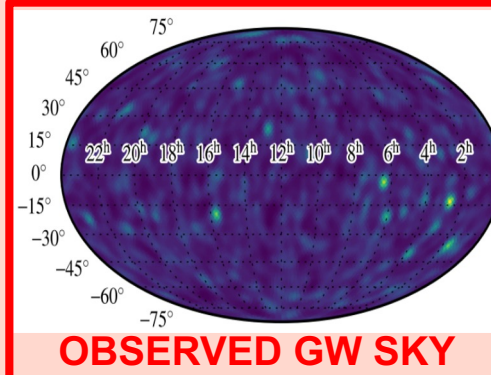
Identifying the host is going to be hard!!

## WP1: New generation of PTA data analysis (DA) pipelines

### Spectrum

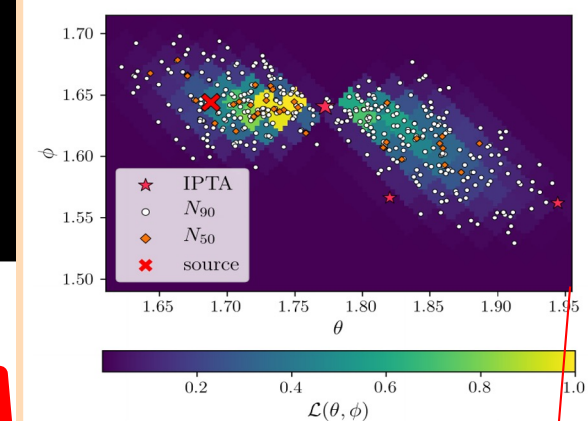


### Sky map

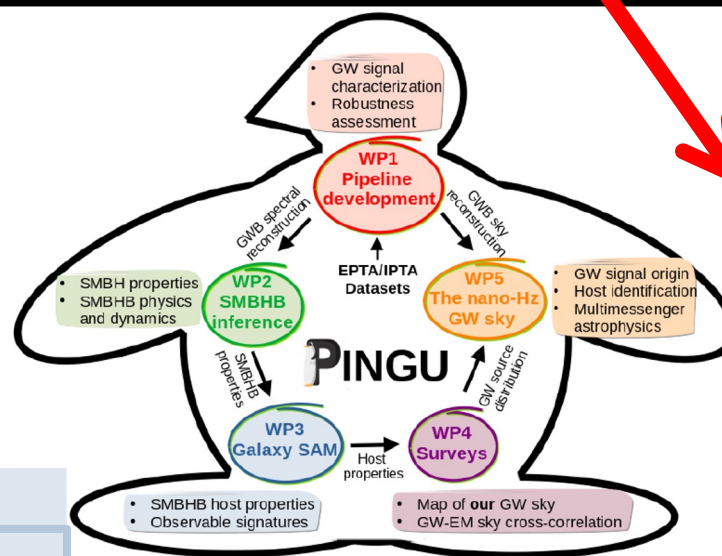
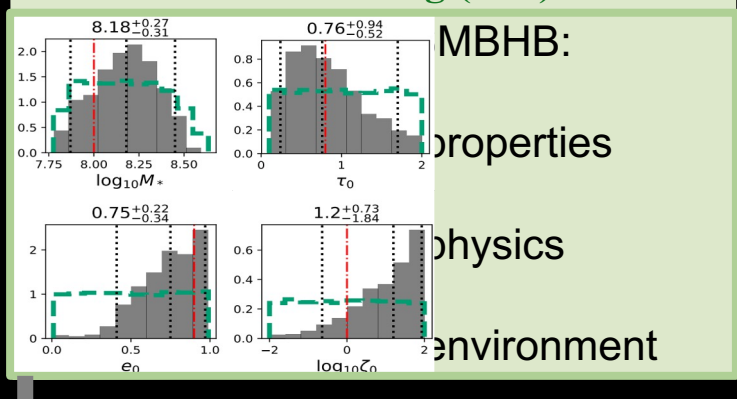


## WP5: the nano-Hz GW sky

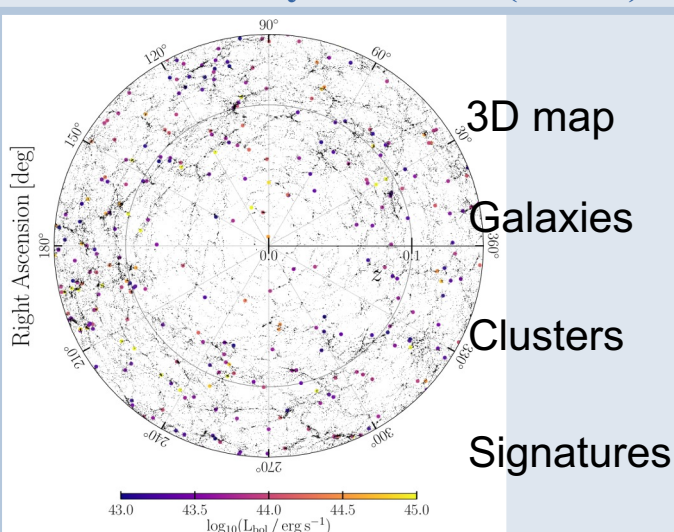
- Cross correlate predicted and
- Identify of CGW hosts



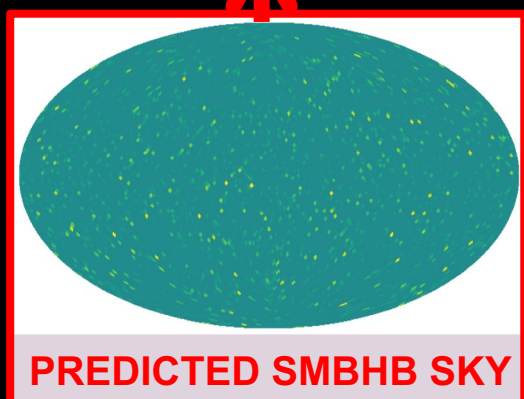
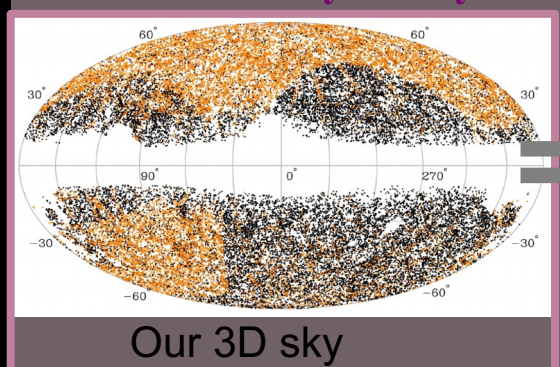
## WP2: machine learning (ML) inference



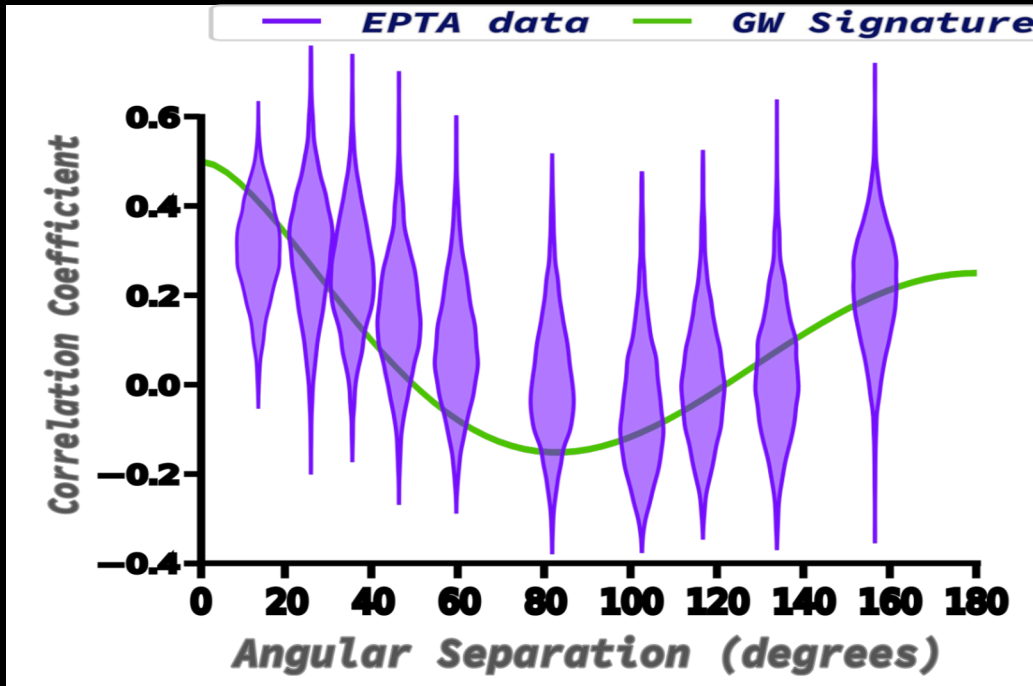
## WP3: semianalytic models (SAMs)



## WP4: All sky surveys

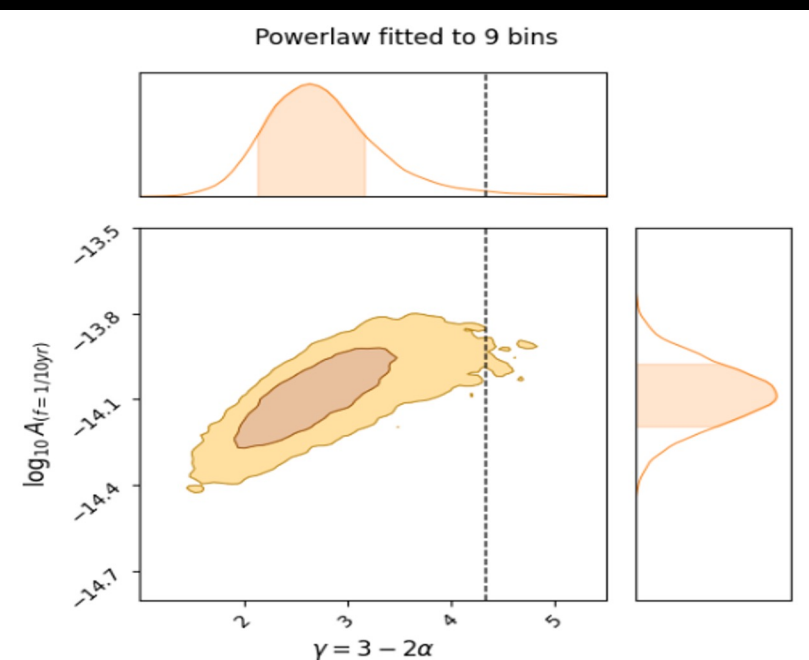
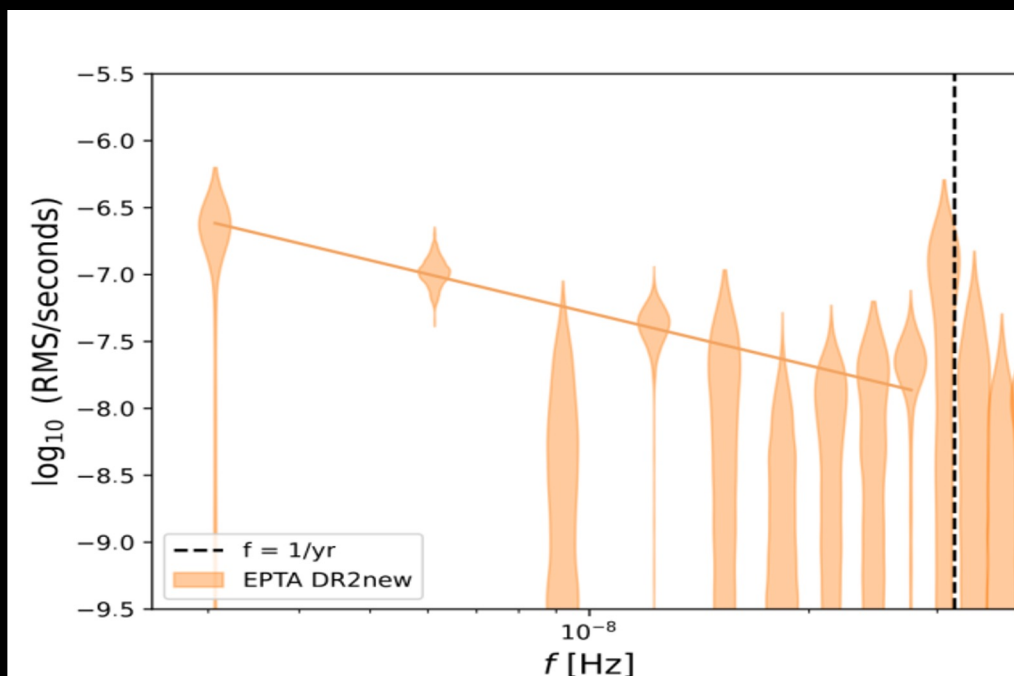


# 2023 a new dawn



(Antoniadis+23, Agazie+23, Reardon+23, Xu+23)

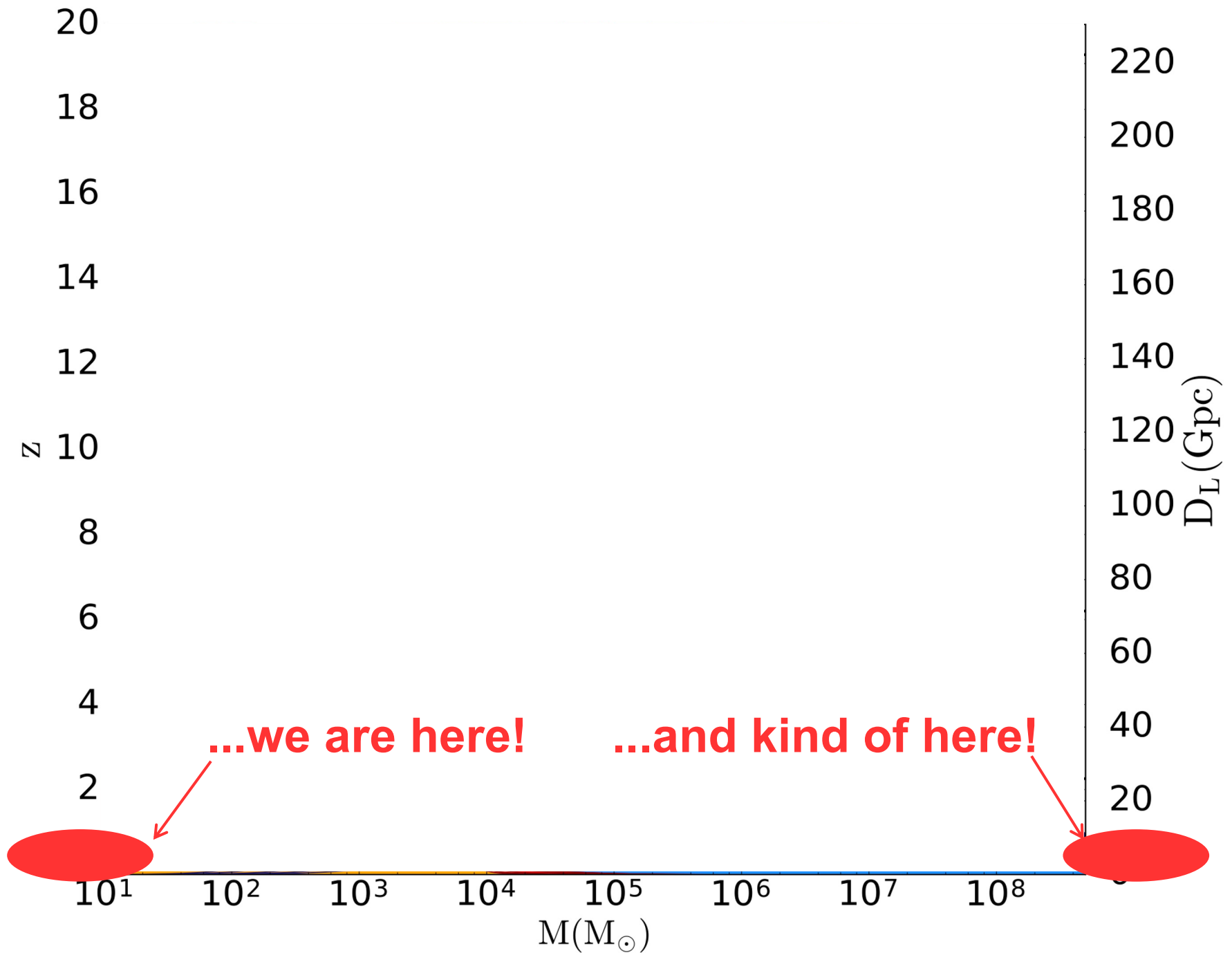
ID	Model	DR2full		DR2full+	DR2new		DR2new+
		ENTERPRISE	FORTYTWO	ENTERPRISE	ENTERPRISE	FORTYTWO	ENTERPRISE
1	PSRN + CURN	–	–	–	–	–	–
2	PSRN + GWB	4	5	4	60	62	65
3	PSRN + CLK	< 0.01	< 0.01	< 0.01	0.2	1.2	0.3
4	PSRN + EPH	< 0.01	$\sim 10^{-4}$	< 0.01	0.2	0.2	1.3
5	PSRN + CURN + CLK	2	1	2.7	0.8	2	1.6
6	PSRN + CURN + EPH	1	0.1	1	1	1	1.6
7	PSRN + GWB + CURN	3	3	4	27	13	25
8	PSRN + GWB + CLK	5	12	7	28	35	57
9	PSRN + GWB + EPH	3	3	3.6	33	29	43



Similar results as NANOgrav, PPTA, CPTA



***Today....***





# DOGGYBAG

- EPTA DR2 show a signal consistent with a GW origin (HD correlation)
- signal broadly consistent with SMBHB origin
- SMBHB are massive and merge quickly
- Signal informative for galaxy formation models
- Future PTAs will identify tens of SMBHBs
- Counterpart identification is going to be challenging



